

College Readiness Mathematics - IC

Scope and Sequence

Unit 1: Exploring the Real Number System through Public Health

Lesson	Objectives
Simplifying Expressions	<ul style="list-style-type: none">• Identify parts of an algebraic expression• Evaluate expressions using the order of operations and the field properties of real numbers.• Simplify expressions using the order of operations and the field properties of real numbers.
Rational Exponents	<ul style="list-style-type: none">• Evaluate numeric expressions using properties of rational exponents.• Simplify algebraic expressions using properties of rational exponents.
Performing Operations in Public Health Contexts	<ul style="list-style-type: none">• Perform multi-step mathematical operations on real numbers to solve real-life problems.• Estimate a real number solution to a real-life problem.• Assess the reasonableness of an estimate in the context of a real-life problem.
Adding and Subtracting Radicals	<ul style="list-style-type: none">• Identify like radicals.• Add and subtract radical expressions.
Multiplying Radicals	<ul style="list-style-type: none">• Perform multiplication of radical expressions.
Dividing Radicals	<ul style="list-style-type: none">• Perform division of radical expressions, rationalizing the denominator when necessary.
Dimensional Analysis	<ul style="list-style-type: none">• Use dimensional analysis to convert units and compare quantities, attending to limitations on the unit of measurement.

Unit 2: Interpreting Data

Lesson	Objectives
Relative Frequencies	<ul style="list-style-type: none">• Complete a two-way table, and calculate marginal and conditional distributions.•

Given a two-way table, calculate marginal and joint relative frequency distributions.

- Given a two-way table, calculate conditional relative frequency distributions.
- Create marginal relative frequency distributions.
- Create conditional relative frequency distributions.
- Interpret frequencies appropriately when given data from samples that differ considerably in sample size for two categorical variables.

Describing and Comparing Data with Dotplots and Stemplots

- Identify and/or describe a dotplot.
- Identify and/or describe a stemplot.
- Compare two distributions using dotplots or stemplots.

Describing and Comparing Data with Histograms

- Identify the patterns, shape, and spread of a distribution using histograms.
- Relate measures of center to the shape of a distribution using histograms.
- Compare two distributions using histograms.

Measures of Center and Location

- Calculate measures of center, given a data set or a graphical display.
- Interpret the measures of center.
- Analyze the effect of extreme values on the value of the mean and median.
- Analyze the relationship between center and shape.

Measures of Variability

- Calculate the range, standard deviation, or interquartile range of a univariate data set.
- Interpret the range, standard deviation, or interquartile range of a univariate data set.
- Compare the spread given graphical displays of two univariate data sets.
- Use a graphing calculator to compute the numerical summary of a univariate data set.

Boxplots and Outliers

- Identify if a univariate data set contains any outliers.
- Represent univariate data using a boxplot.

- Compare distributions presented in parallel box-plots.
- Identify the percent and number of values lying in each portion of a boxplot.
- Create a boxplot using a graphing calculator.

The Relationship between Two Quantitative Variables

- Identify the explanatory and response variable.
- Represent two quantitative variables using a scatterplot.
- Describe the direction, form, strength, and unusual observations given a scatterplot.
- Create a scatterplot using a graphing calculator.

Correlation

- Interpret the correlation of a linear relationship between two quantitative variables.
- Describe the effect of unusual observations on the correlation.
- Distinguish between correlation and causation.

Making Predictions from a Least-Squares Regression Line

- Interpret the slope and y -intercept of a linear model.
- Make a prediction using a linear model.

Calculating the Least-Squares Regression Line

- Explain why the line that is the best fit for a linear relationship is called the least-squares regression line.
- Compute a least-squares regression line and correlation using technology.
- Identify a least-squares regression line using computer output.

R-squared and s

- Determine r^2 using a graphing calculator or computer output.
- Interpret r^2 and s in context.
- Identify s .
- Describe the effect that influential points have on the least-squares regression line.

Unit 3: Calculating Probabilities of Compound Events

Introduction to Probability	<ul style="list-style-type: none"> • Interpret probability as the long-run relative frequency of an event. • Describe the law of large numbers. • Describe how a simulation is used to imitate a random process. • Conduct a simulation using a graphing calculator.
Probability Rules	<ul style="list-style-type: none"> • Identify a probability model to describe a random process. • Apply the basic probability rules, which indicate that the probability of an event is a number between 0 and 1 and that the sum of the probabilities of all outcomes in the sample space is 1. • Apply the complement rule and the addition rule for mutually exclusive events.
Applying Probability Rules	<ul style="list-style-type: none"> • Determine probabilities using a two-way table. • Determine probabilities using a Venn diagram.
Conditional Probabilities	<ul style="list-style-type: none"> • Calculate a conditional probability. • Interpret a conditional probability. • Determine if two events are independent.

Unit 4: Two- and Three-Dimensional Geometry

Lesson	Objectives
Application of Distance, Midpoint, and Slope	<ul style="list-style-type: none"> • Use the distance formula, midpoint formula, or slope to verify a geometric property. • Use coordinates to compute the area of a triangle, rectangle, or circle. • Use coordinates to compute the perimeter of a polygon or the circumference of a circle.
Figures in the Coordinate Plane	<ul style="list-style-type: none"> • Apply coordinate algebra proofs to triangles and quadrilaterals. • Calculate the perimeter of a triangle or quadrilateral given the coordinates of the vertices.
Area of Triangles and Parallelograms	<ul style="list-style-type: none"> • Solve problems involving areas of triangles and parallelograms.
Circumference and Arc Length	<ul style="list-style-type: none"> • Solve problems involving circumference of a circle.

- Determine the radian measure of a central angle.
- Solve problems involving arc length with central angles measured in degrees.
- Solve problems involving arc length with central angles measured in radians.

Area of a Circle and a Sector

- Solve problems involving area of a circle.
- Solve problems involving area of a sector with central angles measured in radians.
- Solve problems involving area of a sector with central angles measured in degrees.

Volume of Cylinders, Cones, and Spheres

- Write expressions to represent the volumes or unknown measures of cylinders and cones.
- Solve mathematical and real-world problems involving the volume of right and oblique cylinders.
- Solve mathematical and real-world problems involving the volume of right and oblique cones.
- Solve mathematical and real-world problems involving the volume of spheres.

Surface Area

- Solve mathematical and real-world problems involving lateral area of prisms, cylinders, pyramids, and cones.
- Solve mathematical and real-world problems involving surface area of prisms, cylinders, cones, spheres, and pyramids.
- Solve mathematical and real-world problems about lateral and surface areas of composite figures.

Application of Volume and Surface Area

- Derive the formula for the volume of a prism or a pyramid, or a cone.
- Derive the formula for the surface area of a prism, a pyramid, or a cone.
- Calculate the volume or surface area of a prism.
- Calculate the volume or surface area of a cone.
- Calculate the volume or surface area of a pyramid.

Lesson

Right Triangle Trigonometry

Objectives

- Use the Pythagorean theorem, and the trigonometric functions and their inverses to solve right triangles.
- Use special right triangle relationships to solve right triangles.

Trigonometric Ratios

- Given an acute angle of a right triangle, label the hypotenuse, opposite, and adjacent sides.
- Given an acute angle of a right triangle, write ratios for sine, cosine, and tangent.
- Relate trigonometric ratios of similar triangles and the acute angles of a right triangle.

Solving for Side Lengths of Right Triangles

- Write equations using trigonometric ratios that can be used to solve for unknown side lengths of right triangles.
- Solve for unknown side lengths of right triangles using trigonometric ratios.
- Apply trigonometric ratios to solve real-world problems.

Solving for Angle Measures of Right Triangles

- Write equations that can be used to solve for unknown angles in right triangles.
- Solve for unknown angles of right triangles using inverse trigonometric functions.
- Apply inverse trigonometric functions to solve real-world problems.

Unit 6: Building and Interpreting Functions in Authentic Situations: Part One

Lesson

Relations and Functions

Objectives

- Represent a relation in multiple ways, including equations, graphs, words, and tables of values.
- Determine if a relation is a function.
- Determine if the function is one-to-one.
- Determine the domain and range of a relation.
- Evaluate function rules.

Domain and Range

- Determine the domain and range of a function in both mathematical and real-world contexts.

Rate of Change	<ul style="list-style-type: none"> • Calculate the average rate of change of a function over a specified interval. • Interpret the average rate of change of a function over a specified interval. • Solve problems involving direct variation.
Linear Functions	<ul style="list-style-type: none"> • Determine if a function is linear. • Represent a linear relationship numerically, algebraically, and graphically.
Absolute Value Functions	<ul style="list-style-type: none"> • Analyze absolute value functions to determine key features of the graph. • Model and solve mathematical and real-world problems with absolute value functions.
Quadratic Functions	<ul style="list-style-type: none"> • Find the line of symmetry and vertex of a parabola given its function rule. • Identify a quadratic function from the function rule. • Use key attributes of a quadratic function to solve word problems.
Square Root Functions	<ul style="list-style-type: none"> • Find the inverse of a quadratic function. • Find the domain of a square root function.
The Cubing Function	<ul style="list-style-type: none"> • Graph the parent cubic function and translations of the parent cubic function. • Use technology to graph cubic functions. • Approximate solutions to cubic equations from graphs.
Graphing Radical Functions	<ul style="list-style-type: none"> • Relate transformations to the graphs of square root and cube root functions to their parent function. • Determine the domain and range of square root and cube root functions.
Application of Rational Functions	<ul style="list-style-type: none"> • Identify the graph of a rational function expressed algebraically. • Graph the parent function of a rational function that models a real-world scenario. • Analyze key characteristics of the graph of a rational function. •

Model key characteristics of the graph of a rational function.

Unit 7: Building and Interpreting Functions in Authentic Situations: Part Two

Lesson	Objectives
Rewriting Exponential Functions	<ul style="list-style-type: none">• Write exponential functions and expressions in equivalent forms, using the properties of exponents to justify steps.• Use alternative forms of an exponential function to highlight different information about that function and the real-world situation it models.
Graphing Exponential Functions	<ul style="list-style-type: none">• Identify exponential functions.• Determine the domain and range of exponential functions.• Graph exponential functions.
Graphing Logarithmic Functions	<ul style="list-style-type: none">• Identify logarithmic functions.• Determine the domain and range of logarithmic functions.• Identify and analyze the graphs of logarithmic functions.
Arithmetic Sequences	<ul style="list-style-type: none">• Find the common difference of an arithmetic sequence.• Determine if a sequence is arithmetic.• Apply the formula of an arithmetic sequence.• Find the terms of an arithmetic sequence.
Geometric Sequences	<ul style="list-style-type: none">• Find the common ratio of a geometric sequence.• Determine if a sequence is geometric.• Apply the formula of a geometric sequence.• Find terms of a geometric sequence.
Comparing Characteristics of Functions	<ul style="list-style-type: none">• Determine the similarities and differences in characteristics of multiple functions graphically.• Determine the similarities and differences in characteristics of multiple functions tabularly.• Determine the similarities and differences in characteristics of multiple functions symbolically.

- Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).

Functions and Transformations

- Graph a transformation of a function.
- Recognize even and odd functions.
- Write the equation of a transformed function given its graph.
- Describe the effect of one or more transformations on the graph of a function.

Modeling with Functions in Financial Contexts

- Analyze a function to make a decision about a financial investment.
- Interpret key characteristics of a function that represents a financial investment scenario.
- Graph a parent function that models a financial investment scenario.
- Identify the graph of a parent function that models a financial investment scenario.
- Classify a relation as a function, one-to-one and/or onto.

Unit 8: Analyzing Financial Investments: Part One

Lesson

Literal Equations

Objectives

- Solve a literal equation in terms of a given variable.
- Determine if expressions are equivalent.

Absolute Value and Linear Equations in Financial Contexts

- Create a linear or absolute value equation in one variable to represent a financial scenario.
- Use a linear or absolute value equation in one variable to solve a financial investment problem.

Absolute Value and Linear Inequalities in Financial Context

- Create a linear or absolute value equation in one variable to represent a financial scenario.
- Use a linear or absolute value equation in one variable to solve a financial investment problem.
- Use the solution to a linear or absolute value inequality to draw conclusions about a situation being modeled, including possible constraints.

Solving Linear Systems Graphically

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	<p>Solve systems of two-variable linear equations graphically.</p> <ul style="list-style-type: none"> • Classify systems of two-variable equations as dependent, independent, consistent, or inconsistent. • Solve systems of two-variable linear inequalities.
Solving Linear Systems by Elimination	<ul style="list-style-type: none"> • Solve systems of two-variable linear equations using elimination.
Solving Linear Systems by Substitution	<ul style="list-style-type: none"> • Solve systems of two-variable linear equations using substitution.
Modeling with Linear Systems	<ul style="list-style-type: none"> • Model and solve real-world problems using systems of linear equations and inequalities.
Quadratic Functions and Equations in Financial Context	<ul style="list-style-type: none"> • Use a quadratic function to solve a financial investment problem. • Use the solution to a quadratic equation to draw conclusions about a situation being modeled, including possible constraints.
Mixed Degree Systems	<ul style="list-style-type: none"> • Solve linear-quadratic systems of equations. • Solve quadratic-quadratic systems of equations.
Solving One-Variable Equations with Systems	<ul style="list-style-type: none"> • Solve a one-variable linear or quadratic equation by graphing a related system of equations.

Unit 9: Analyzing Financial Investments: Part Two

Lesson	Objectives
Rational Equations in Financial Contexts	<ul style="list-style-type: none"> • Create a rational equation in one variable to represent a financial scenario. • Use a rational equation to solve a financial investment problem.
Radical Equations and Extraneous Roots	<ul style="list-style-type: none"> • Model and solve mathematical and real-world problems using radical equations, and determine extraneous roots.
Exponential Equations in Financial Contexts	<ul style="list-style-type: none"> • Use an exponential equation to solve a financial investment problem. • Create an exponential equation in one variable to represent a financial scenario.
Solving Exponential and Logarithmic Equations	<ul style="list-style-type: none"> • Solve exponential and logarithmic equations using inverses, properties, and algorithms.

Modeling with Exponential and Logarithmic Equations • Model and solve real-world problems using exponential and logarithmic functions.

Unit 10: Capstone Project

Lesson

Completing a Capstone Project

Objectives

- Develop a topic and proposal for a course capstone project.
- Complete research.
- Draft and revise a capstone project.