Amity Regional High School

Entering College Algebra (Algebra 3) Essential Skills

Welcome to your College Algebra Success Problem-set! This packet is designed to help you review key concepts and strengthen your math skills before the next school year. It covers essential topics to reinforce what you've learned and preparing you for future lessons.

Complete each section carefully. Show all work and use the provided formulas when necessary. If you get stuck, you can look up the topics on the internet or ask for help. By working through this packet, you'll build confidence and stay sharp in math next year.

Let's get started—happy learning!

- **Exponents**
    a. Property of Exponents
        i. Negative exponent
        ii. Zero exponent
        iii. Product
        iv. Power
        v. Quotient
        vi. Products raised to powers
        vii. Quotients raised to powers
    b. Radicals
        i. Square roots
        ii. Simplifying radical expressions
        iii. Product rule for square roots
        iv. Quotient rule for square roots
        v. Rationalizing denominators
        vi. Other kinds of roots
    c. Rational Exponents
- **Polynomials**
    a. What is a polynomial
    b. Operations with polynomials
        i. Adding and subtracting
        ii. Multiplying
        iii. Product of two binomials
        iv. Special products
    c. Factoring polynomials
        i. Common factors
        ii. Factoring Trinomials

        iii.   Factoring perfect square trinomials

        iv.   Factoring the sum and difference of two cubes

        v.   Factoring expressions containing fractional and negative exponents

        vi.   Zeros

             1.   Multiplicity

        vii.   Long Division

        viii.   Synthetic Division

   d. Rational expressions

        i.   Simplifying rational expressions

        ii.   Multiplying rational expressions

        iii.   Adding and subtracting rational expressions

             1.   Same denominators

             2.   Different denominators

             3.   Complex rational expressions

             4.   Fractional expressions

- **Functions and Graphs**
  - a. 4a   Graphs of equations
    - i.   Interpreting a graph
  - b. Basic functions and their graphs
    - i.   Function notation
    - ii.   Vertical line test
    - iii.   Domain and range
    - iv.   Intercepts
    - v.   Difference quotients
    - vi.   Piecewise
    - vii.   Increasing and decreasing functions
    - viii.   Relative minima and maxima
    - ix.   Even and odd functions
  - c. 4b   Transformations
    - i.   Horizontal and vertical shifts
    - ii.   Horizontal and vertical stretching and shrinking
    - iii.   Sequence of transformations
    - iv.   Linear
      - 1.   Slope
      - 2.   Slope intercept form
      - 3.   Horizontal and vertical
      - 4.   Standard form
      - 5.   Parallel and perpendicular lines
  - d. 4c   Combination and composite functions
    - i.   Combination
    - ii.   Composite
    - iii.   Decomposing
- **Polynomials and Complex Numbers**
  - a. What is a polynomial
  - b. Operations with polynomials
    - i.   Adding and subtracting
    - ii.   Multiplying
    - iii.   Product of two binomials
    - iv.   Special products

    c. Factoring polynomials
-     i.   Common factors
-     ii.   Factoring Trinomials
-     iii.   Factoring perfect square trinomials
-     iv.   Factoring the sum and difference of two cubes
-     v.   Factoring expressions containing fractional and negative exponents
-     vi.   Zeros
  -     1. Multiplicity
-     vii.   Long Division
-     viii.   Synthetic Division

There are additional problems that you can access in deltamath.com using the following codes
- https://www.deltamath.com/students?code=X2G8-6RF8
- https://www.deltamath.com/students?code=7J4N-R5WZ
- https://www.deltamath.com/students?code=X296-28CS

Digital Resources Below is a list of search strings that will pull up multiple resources.
http://www.youtube.com/results?search_query=order+of+operations
http://www.youtube.com/results?search_query=simplifying+rational+expressions
http://www.youtube.com/results?search_query=Simplifying+Radicals
http://www.youtube.com/results?search_query=factoring
http://www.youtube.com/results?search_query=simplifying+expressions
http://www.youtube.com/results?search_query=solving+equations
http://www.youtube.com/results?search_query=solving+systems+of+linear+equations
http://www.youtube.com/results?search_query=solving+system+of+inequalities
http://www.youtube.com/results?search_query=slopes+of+linear+equations
http://www.youtube.com/results?search_query=slopes+of+parallel+and+perpendicular+lines
http://www.youtube.com/results?search_query=domain+and+range+of+radical+functions
http://www.youtube.com/results?search_query=find+horizontal%2C+vertical%2C+and+slant+asymptotes
http://www.youtube.com/results?search_query=find+and+sketch+inverse+functions
http://www.youtube.com/results?search_query=find+composition+of+functions
http://www.youtube.com/results?search_query=factoring+greatest+common+term
http://www.youtube.com/results?search_query=factoring+difference+of+squares
http://www.youtube.com/results?search_query=factoring+trinomials
http://www.youtube.com/results?search_query=simplyfyiing+polynomials
http://www.youtube.com/results?search_query=isosceles+triangle
http://www.youtube.com/results?search_query=properties+of+quadrilaterals+and+parallelograms
http://www.youtube.com/results?search_query=special+right+triangle
http://www.youtube.com/results?search_query=properties+of+circles
http://www.youtube.com/results?search_query=proving+traingles+congruent
http://www.youtube.com/results?search_query=proving+traingles+similar
http://www.youtube.com/results?search_query=right+traingle+trigonometry

Radicals:

To simplify means that 1) no radicand has a perfect square factor and

2) there is no radical in the denominator (rationalize).

Recall the **Product Property** $\sqrt{ab} = \sqrt{a} \bullet \sqrt{b}$ and the **Quotient Property** $\sqrt{\dfrac{a}{b}} = \dfrac{\sqrt{a}}{\sqrt{b}}$

Examples: Simplify $\sqrt{24} = \sqrt{4} \bullet \sqrt{6}$ find the perfect square factor

$$= 2\sqrt{6} \qquad \text{simplify}$$

Simplify $\sqrt{\dfrac{7}{2}} = \dfrac{\sqrt{7}}{\sqrt{2}} \bullet \dfrac{\sqrt{2}}{\sqrt{2}}$ multiply numerator & denominator by $\sqrt{2}$

$$= \dfrac{\sqrt{14}}{\sqrt{4}} = \dfrac{\sqrt{14}}{2} \qquad \text{multiply straight across and simplify}$$

If the denominator contains 2 terms, multiply the numerator and denominator by

conjugate of the denominator (the conjugate of $3 + \sqrt{2}$ is $3 - \sqrt{2}$)

Simplify each of the following.

1. $\sqrt{32}$

2. $\sqrt{(2x)^8}$

3. $\sqrt[3]{-64}$

4. $\sqrt{49m^2 n^8}$

5. $\sqrt{\dfrac{11}{9}}$

6. $\sqrt{60} \bullet \sqrt{105}$

7. $\left(\sqrt{5} - \sqrt{6}\right)\left(\sqrt{5} + \sqrt{2}\right)$

Rationalize.

8. $\dfrac{1}{\sqrt{2}}$

9a. $\dfrac{2}{\sqrt{3}}$

10a. $\dfrac{3}{2 - \sqrt{5}}$

Complex Numbers:

Form of complex number: $a + bi$

> Where a is the real part and the bi is the imaginary part
>
> Always make these substitutions $\sqrt{-1} = i$ and $i^2 = -1$
>
> To simplify: pull out the $\sqrt{-1}$ before performing any operation

Example: $\sqrt{-5} = \sqrt{-1} \cdot \sqrt{5}$ Pull out $\sqrt{-1}$ Example: $\left(i\sqrt{5}\right)^2 = i\sqrt{5} \cdot i\sqrt{5}$

$\qquad\qquad = i\sqrt{5}$ Make substitution $= i^2\sqrt{25} = (-1)(5) = -5$

> Treat i like any other variable when $+, -, \times, or \div$ (but always simplify $i^2 = -1$)

Example: $2i(3+i) = 2(3i) + 2i(i)$ Distribute

$\qquad\qquad\qquad = 6i + 2i^2$ Simplify

$\qquad\qquad\qquad = 6i + 2(-1)$ Substitute

$\qquad\qquad\qquad = -2 + 6i$ Simplify and rewrite in complex form

> Since $i = \sqrt{-1}$, no answer can have an 'i' in the denominator. RATIONALIZE!

Simplify.

9b. $\sqrt{-49}$

10b. $6\sqrt{-12}$

11. $-6(2-8i) + 3(5+7i)$

12. $(3-4i)^2$

13. $(6-4i)(6+4i)$
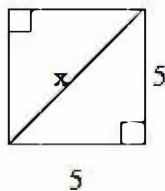
Rationalize.

14. $\dfrac{1+6i}{5i}$

Geometry:

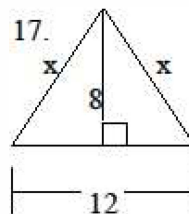Pythagorean Theorem (right triangles): $a^2 + b^2 = c^2$
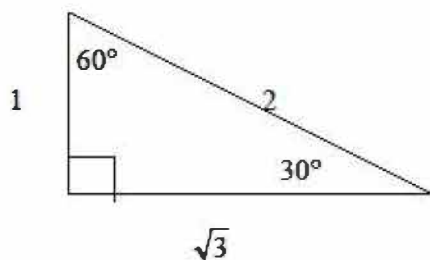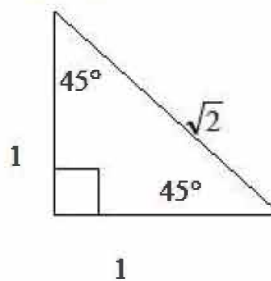
Find the value of x.

15.

9, x, 12

16.

x, 5, 5

17.

x, x, 8, 12
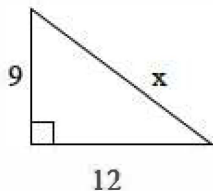
18. A square has perimeter 12 cm. Find the length of the diagonal.

* In $30° - 60° - 90°$ triangles, sides are in proportion $1, \sqrt{3}, 2$.

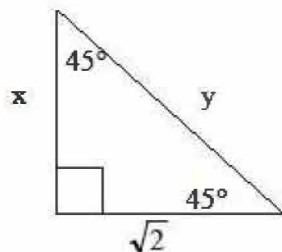60°, 1, 2, 30°, $\sqrt{3}$

*In $45° - 45° - 90°$ triangles, sides are in proportion $1, 1, \sqrt{2}$.

45°, 1, $\sqrt{2}$, 45°, 1

Solve for x and y.

19.

45°, x, y, 45°, $\sqrt{2}$

20.

45°, 4, x, 45°, y

4

21.

22.
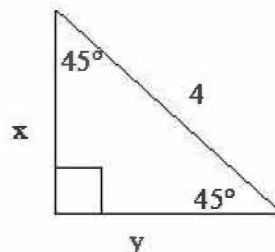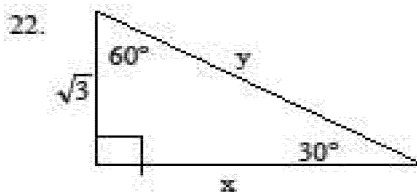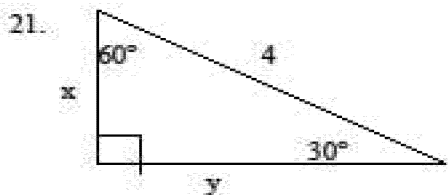

Equations of Lines:

Slope-intercept form: $y = mx + b$ Vertical line: $x = c$ *(slope is undefined)*

Point-slope form: $y - y_1 = m(x - x_1)$ Horizontal line: $y = c$ *(slope is zero)*

Standard Form: $Ax + By = C$ Slope: $m = \dfrac{y_2 - y_1}{x_2 - x_1}$

23.   State the slope and y-intercept of the linear equation: $5x - 4y = 8$

24.   Find the x-intercept and y-intercept of the equation: $2x - y = 5$

25.   Write the equation in standard form: $y = 7x - 5$

Write the equation of the line in slope-intercept form with the following conditions:
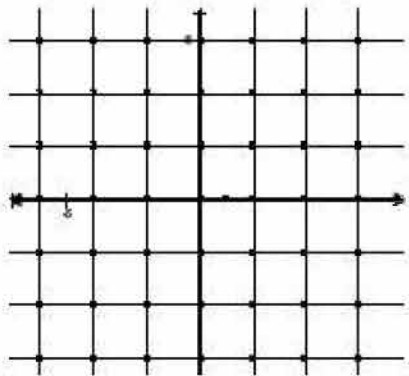
26.   slope = -5 and passes through the point (-3, -8)

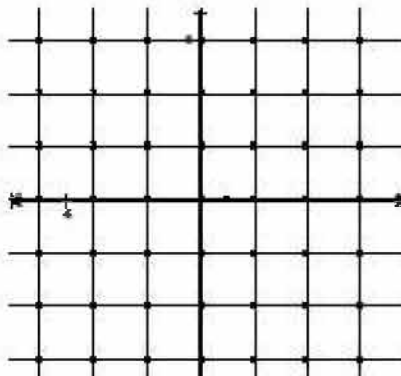27.   passes through the points (4, 3) and (7, -2)

28.   x-intercept = 3 and y-intercept =2

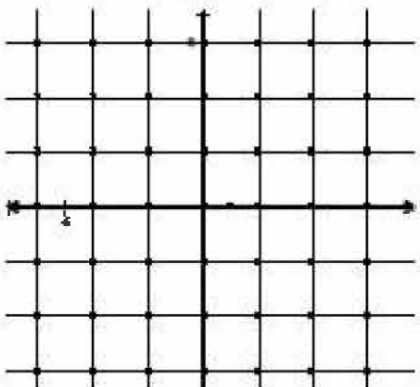**Graphing:** Graph each function, inequality, and/or system.
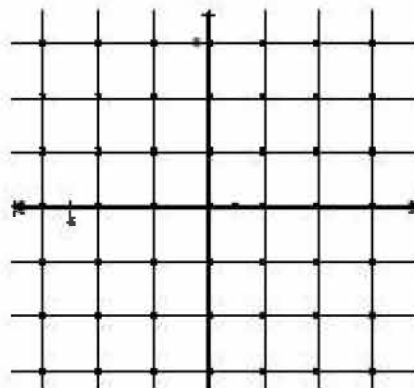
29. $3x - 4y = 12$

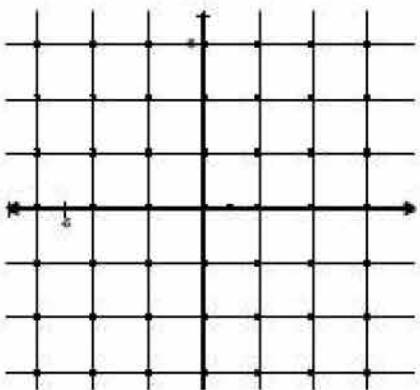30. $\begin{cases} 2x + y = 4 \\ x - y = 2 \end{cases}$

31. $y < -4x - 2$

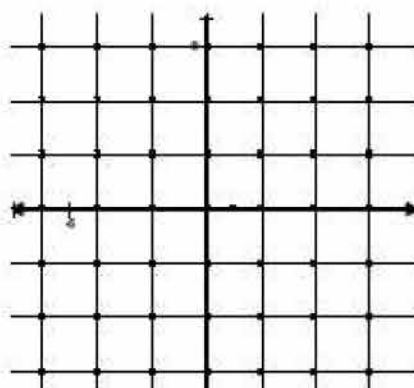32. $y + 2 = |x + 1|$

33. $y > |x| - 1$

34. $y + 4 = (x - 1)^2$

6

Systems of Equations:

$$\begin{cases} 3x + y = 6 \\ 2x - 2y = 4 \end{cases}$$

Substitution:

Solve 1 equation for 1 variable

Rearrange.

Plug into 2nd equation.

Solve for the other variable.

Elimination:

Find opposite coefficients for 1 variable

Multiply equation(s) by constant(s).

Add equations together (lose 1 variable)

Solve for variable.

Then plug answer back into an original equation to solve for the 2nd variable.

$y = 6 - 3x$	Solve 1st equation for y	$6x + 2y = 12$	Multiply 1st equation by 2
$2x - 2(6 - 3x) = 4$	Plug into 2nd equation	$2x - 2y = 4$	coefficients of y are opposite
$2x - 12 + 6x = 4$	Distribute	$8x = 16$	Add
$8x = 16$ and $x = 2$	Simplify	$x = 2$	Simplify.

Plug x=2 back into the original equation $\quad \begin{aligned} 6 + y &= 6 \\ y &= 0 \end{aligned}$

Solve each system of equations, using any method.

35. $\begin{cases} 2x + y = 4 \\ 3x + 2y = 1 \end{cases}$

36. $\begin{cases} 2x + y = 4 \\ 3x - y = 14 \end{cases}$

37. $\begin{cases} 2w - 5z = 13 \\ 6w + 3z = 10 \end{cases}$

Exponents:

Recall the following rules of exponents:

1. $a^1 = a$ — Any number raised to the power of one equals itself.

2. $1^a = 1$ — One raised to any power is one.

3. $a^0 = 1$ — Any nonzero number raised to the power of zero is one.

4. $a^m \cdot a^n = a^{m+n}$ — When multiplying two powers that have the same base, add the exponents.

5. $\dfrac{a^m}{a^n} = a^{m-n}$ — When dividing two powers with the same base, subtract the exponents.

6. $(a^m)^n = a^{mn}$ — When a power is raised to another power, multiply the exponents.

7. $a^{-n} = \dfrac{1}{a^n}$ and $\dfrac{1}{a^{-n}} = a^n$ — Any nonzero number raised to a negative power equals its reciprocal raised to the opposite positive power.

Express each of the following in simplest form. Answers should not have any negative exponents.

38. $5a^0$

39. $\dfrac{3c}{c^{-1}}$

40. $\dfrac{2ef^{-1}}{e^{-1}}$

41. $\dfrac{\left(n^3 p^{-1}\right)^2}{(np)^{-2}}$

Simplify.

42. $3m^2 \bullet 2m$

43. $\left(a^3\right)^2$

44. $(-b^3 c^4)^5$

45. $4m(3a^2 m)$

Polynomials:

To add/subtract polynomials, combine like terms.

EX: $8x - 3y + 6 - (6y + 4x - 9)$	*Distribute the negative through the parantheses.*
$= 8x - 3y + 6 - 6y - 4x + 9$	*Combine like terms with similar variables.*
$= 8x - 4x - 3y - 6y + 6 + 9$	
$= 4x - 9y + 15$	

Simplify.

46. $3x^3 + 9 + 7x^2 - x^3$

47. $7m - 6 - (2m + 5)$

To multiply two binomials, use FOIL.

EX: $(3x - 2)(x + 4)$	*Multiply the first, outer, inner, and last terms.*
$= 3x^2 + 12x - 2x - 8$	*Combine like terms together.*
$= 3x^2 + 10x - 8$	

Multiply.

48. $(3a + 1)(a - 2)$

49. $(s + 3)(s - 3)$

50. $(c - 5)^2$

51. $(5x + 7y)(5x - 7y)$

Factoring:

Follow these steps in order to factor polynomials.

STEP 1: Look for a GCF in ALL of the terms.

a) If you have one (other than 1) factor it out.

b) If you don't have one move on to STEP 2

STEP 2: How many terms does the polynomial have?

2 Terms a) is it the difference of two squares? $a^2 - b^2 = (a+b)(a-b)$

EX: $x^2 - 25 = (x+5)(x-5)$

b) Is it the sum or difference of two cubes?
$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$
$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

EX:
$$m^3 + 64 = (m+4)(m^2 - 4m + 16)$$
$$p^3 - 125 = (p-5)(p^2 + 5p + 25)$$

3 Terms   **EX:**

$x^2 + bx + c = (x+\_)(x+\_)$ $x^2 + 7x + 12 = (x+3)(x+4)$

$x^2 - bx - c = (x-\_)(x-\_)$ $x^2 - 5x + 4 = (x-1)(x-4)$

$x^2 + bx - c = (x-\_)(x+\_)$ $x^2 + 6x - 16 = (x-2)(x+8)$

$x^2 - bx - c = (x-\_)(x+\_)$ $x^2 - 2x - 24 = (x-6)(x+4)$

4 Terms---Factor by Grouping

a) Pair up first two terms and last two terms.

b) Factor out GCF of each pair of numbers.

c) Factor out front parentheses that the terms have in common.

d) Put leftover terms in parentheses.

$$Ex: x^3 + 3x^2 + 9x + 27 = \left(x^3 + 3x^2\right) + \left(9x + 27\right)$$
$$= x^2(x+3) + 9(x+3)$$
$$= (x+3)\left(x^2 + 9\right)$$

Factor completely.

52. $z^2 + 4z - 12$

53. $6 - 5x - x^2$

54. $2k^2 + 2k - 60$

55. $-10b^4 - 15b^2$

56. $9c^2 + 30c + 25$

57. $9n^2 - 4$

58. $27z^3 - 8$

59. $2mn - 2mt + 2sn - 2st$

To solve quadratic equations, try to factor first and set each factor equal to zero. Solve for your variable. If the quadratic does NOT factor, use the quadratic formula.

EX: $x^2 - 4x = 21$ *Set equal to zero FIRST.*

$x^2 - 4x - 21 = 0$ *Now factor.*

$(x + 3)(x - 7) = 0$ *Set each factor equal to zero.*

$x + 3 = 0$ $x - 7 = 0$ *Solve for each x.*

$x = -3$ $x = 7$

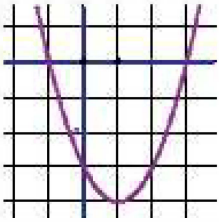**Solve each equation.**

60. $x^2 - 4x - 12 = 0$

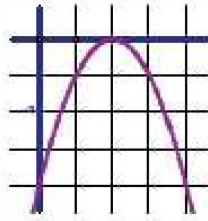61. $x^2 + 25 = 10x$

62. $x^2 - 14x + 40 = 0$

Discriminant: The number under the radical in the quadratic formula $(b^2 - 4ac)$ can tell you what kind of roots you will have.

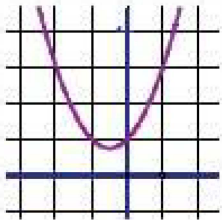If $b^2 - 4ac > 0$ you will have TWO real roots   If $b^2 - 4ac = 0$ you will have ONE real root (touches axis once)

(touches the x-axis twice)

If $b^2 - 4ac < 0$ you will have TWO imaginary roots. (Function does not cross the x-axis)

QUADRATIC FORMULA—allows you to solve any quadratic for all its real and imaginary roots.

$$5x^2 - 2x + 4 = 0 \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

EX: In the equation $x^2 + 2x + 3 = 0$, find the value of the discriminant, describe the nature of the roots, then solve.

$x^2 + 2x + 3 = 0$ *Determine the values of a, b, and c.*

$a = 1 \ b = 2 \ c = 3$ *Find the discriminant.*

$D = 2^2 - 4 \cdot 1 \cdot 3$

$D = 4 - 12$

$D = -8$ *There are two imaginary roots.*

Solve : $x = \dfrac{-2 \pm \sqrt{-8}}{2}$

$x = \dfrac{-2 \pm 2i\sqrt{2}}{2}$

$x = -1 \pm i\sqrt{2}$

Find the value of the discriminant, describe the nature of the roots, then solve each quadratic. Use EXACT values.

63. $x^2 - 9x + 14 = 0$

64. $5x^2 - 2x + 4 = 0$

Discriminant = _____

Type of Roots: _____

Exact Value of Roots: _____

Discriminant = _____

Type of Roots: _____

Exact Value of Roots: _____

<u>Long Division—can be used when dividing any polynomials.</u>
<u>Synthetic Division—can</u> ONLY be used when dividing a polynomial by a linear polynomial.

EX: $\dfrac{2x^3 + 3x^2 - 6x + 10}{x+3}$

      Long Division   **Synthetic Division**

$\dfrac{2x^3 + 3x^2 - 6x + 10}{x+3}$ $\dfrac{2x^3 + 3x^2 - 6x + 10}{x+3}$

$$x+3 \overline{\smash{\big)}\; 2x^3 + 3x^2 - 6x + 10} \quad\to\quad 2x^2 - 3x + 3 + \frac{1}{x+3}$$

Long Division:

$$2x^2 - 3x + 3 + \frac{1}{x+3}$$
$$x+3 \overline{\smash{\big)}\; 2x^3 + 3x^2 - 6x + 10}$$
$$(-)\left(2x^3 + 6x^2\right)$$
$$-3x^2 - 6x$$
$$(-)\left(-3x^2 - 9x\right)$$
$$3x + 10$$
$$(-)\;(3x + 9)$$
$$1$$

Synthetic Division:

$$\dfrac{2x^3 + 3x^2 - 6x + 10}{x+3}$$

-3	2	3	-6	10
		-6	9	-9
	2	-3	3	1

$$= 2x - 3x + 3 + \frac{1}{x+3}$$

Divide each polynomial using long division OR synthetic division.

65. $\dfrac{c^3 - 3c^2 + 18c - 16}{c^2 + 3c - 2}$

66. $\dfrac{x^4 - 2x^2 - x + 2}{x+2}$

To evaluate a function for the given value, simply plug the value into the function for x.

Evaluate each function for the given value.

67. $f(x) = x^2 - 6x + 2$

    $f(3) = $ _____

68. $g(x) = 6x - 7$

    $g(x + h) = $ _____

69. $f(x) = 3x^2 - 4$

    $5[f(x+2)] = $ _____

Composition and Inverses of Functions:

Recall: $(f \circ g)(x) = f(g(x))$ OR $f[g(x)]$ read "**f of g of x**" means to plug the inside function in for x in the outside function.

Example: Given $f(x) = 2x^2 + 1$ *and* $g(x) = x - 4$ find $f(g(x))$.

$f(g(x)) = f(x-4)$
$\qquad = 2(x-4)^2 + 1$
$\qquad = 2(x^2 - 8x + 16) + 1$
$\qquad = 2x^2 - 16x + 32 + 1$
$f(g(x)) = 2x^2 - 16x + 33$

Suppose $f(x) = 2x$, $g(x) = 3x - 2$, *and* $h(x) = x^2 - 4$. **Find the following:**

70. $f[g(2)] = $ _____

71. $f[g(x)] = $ _____

72. $f[h(3)] = $ _____

73. $g[f(x)] = $ _____

To find the inverse of a function, simply switch the x and the y and solve for the new "y" value.

Example: $f(x) = \sqrt[3]{x+1}$ Rewrite $f(x)$ as y

$y = \sqrt[3]{x+1}$ Switch x and y

$x = \sqrt[3]{y+1}$ Solve for your new y

$(x)^3 = \left(\sqrt[3]{y+1}\right)^3$ Cube both sides

$x^3 = y+1$ Simplify

$y = x^3 - 1$ Solve for y

$f^{-1}(x) = x^3 - 1$ Rewrite in inverse notation

Find the inverse, $f^{-1}(x)$, if possible.

74. $f(x) = 5x + 2$

75. $f(x) = \dfrac{1}{2}x - \dfrac{1}{3}$

Simplify Rational Algebraic Expressions:

Multiplying and Dividing: Factor numerator and denominator completely. Cancel any common factors in the top and bottom. If dividing, change divide to multiply and flip the second fraction.

EX: $\dfrac{x^2+10x+21}{5-4x-x^2} \bullet \dfrac{x^2+2x-15}{x^3+4x^2-21x}$ *Factor everything completely.*

$= \dfrac{(x+7)(x+3)}{(5+x)(1-x)} \bullet \dfrac{(x+5)(x-3)}{x(x-3)(x+7)}$ *Cancel out common factors in the top and bottom.*

$= \dfrac{(x+3)}{x(1-x)}$ *Simplify.*

76. $\dfrac{5z^3+z^2-z}{3z}$

77. $\dfrac{m^2-25}{m^2+5m}$

78. $\dfrac{10r^5}{21s^2} \bullet \dfrac{3s}{5r^3}$

79. $\dfrac{a^2-5a+6}{a+4} \bullet \dfrac{3a+12}{a-2}$

80. $\dfrac{6d-9}{5d+1} \div \dfrac{6-13d+6d^2}{15d^2-7d-2}$

Addition and Subtraction

First find the least common denominator. Write each fraction with that LCD. Add/subtract numerators as indicated and leave the denominators as they are.

EX: $\dfrac{3x+1}{x^2+2x}+\dfrac{5x-4}{2x+4}$ *Factor denominator completely.*

$\dfrac{3x+1}{x(x+2)}+\dfrac{5x-4}{2(x+2)}$ *Find LCD, which is $(2x)(x+2)$*

$\dfrac{2(3x+1)}{2x(x+2)}+\dfrac{x(5x-4)}{2x(x+2)}$ *Rewrite each fraction with the LCD in the denominator.*

$\dfrac{6x+2+5x^2-4x}{2x(x+2)}$ *Write as one fraction.*

$\dfrac{5x^2+2x+2}{2x(x+2)}$ *Combine like terms.*

81. $\dfrac{2x}{5}-\dfrac{x}{3}$

82. $\dfrac{b-a}{a^2b}+\dfrac{a+b}{ab^2}$

83. $\dfrac{2-a^2}{a^2+a}+\dfrac{3a+4}{3a+3}$

18

Complex Fractions: Eliminate complex fractions by multiplying the numerator and denominator by the LCD of each of the small fractions. Then simplify the result.

EX:
$$\dfrac{1+\dfrac{1}{a}}{\dfrac{2}{a^2}-1}$$
Find LCD: a^2

$$=\dfrac{\left(1+\dfrac{1}{a}\right)\bullet a^2}{\left(\dfrac{2}{a^2}-1\right)\bullet a^2}$$
Multiply top and bottom by LCD.

$$=\dfrac{a^2+a}{2-a^2}$$
Factor and simplify if possible.

$$=\dfrac{a(a+1)}{2-a^2}$$

84. $\dfrac{1-\dfrac{1}{2}}{2+\dfrac{1}{4}}$

85. $\dfrac{1+\dfrac{1}{z}}{z+1}$

86. $\dfrac{5+\dfrac{1}{m}-\dfrac{6}{m^2}}{\dfrac{2}{m}-\dfrac{2}{m^2}}$

87. $\dfrac{2+\dfrac{1}{x}-\dfrac{1}{x^2}}{1+\dfrac{4}{x}+\dfrac{3}{x^2}}$

Solving Rational Equations:

Multiply each term by the LCD of all the fractions. This should eliminate all of our fractions. Then solve the equation as usual.

$$\frac{5}{x+2}+\frac{1}{x}=\frac{5}{x}$$
        Find LCD first $x(x+2)$

$$x(x+2)\frac{5}{x+2}+x(x+2)\frac{1}{x}=\frac{5}{x}x(x+2)$$
        Multiply each term by the LCD.

$$5x+1(x+2)=5(x+2)$$
        Simplify and solve.

$$5x+x+2=5x+10$$

$$6x+2=5x+10$$

$$x=8 \quad \leftarrow \textit{Check your answer! Sometimes they do not check!}$$

Check:
$$\frac{5}{8+2}+\frac{1}{8}=\frac{5}{8}$$

$$\frac{5}{10}+\frac{1}{8}=\frac{5}{8}$$

$$\frac{5}{8}=\frac{5}{8}$$

Solve each equation. Check your solutions.

88. $\dfrac{12}{x}+\dfrac{3}{4}=\dfrac{3}{2}$

89. $\dfrac{x+10}{x^2-2}=\dfrac{4}{x}$

90. $\dfrac{5}{x-5}=\dfrac{x}{x-5}-1$

Summer Review Packet for College Algebra

Solutions to Odd Exercises

1. $4\sqrt{2}$ **3.** -4 **5.** $\dfrac{\sqrt{11}}{3}$ **7.** $5+\sqrt{10}-\sqrt{30}-2\sqrt{3}$ **9a.** $\dfrac{2\sqrt{3}}{3}$

9b. $7i$ **11.** $3+69i$ **13.** 52 **15.** 15 **17.** 10 **19.** $\sqrt{2}$

21. $x=2$ $y=2\sqrt{3}$ **23.** $m=\dfrac{5}{4}$ $b=-2$ **25.** $7x-y=5$ **27.** $y=-\dfrac{5}{3}x+\dfrac{29}{3}$

29, 31, 33 graphs **35.** (7, -10) **37.** $\left(\dfrac{89}{36},\ -\dfrac{29}{18}\right)$ **39.** $3c^2$ **41.** n^8

43. a^6 **45.** $12a^2 m^2$ **47.** $5m-11$ **49.** s^2-9

51. $25x^2-49y^2$ **53.** $-(x+6)(x-1)$ **55.** $-5b^2(2b^2+3)$ **57.** $(3n-2)(3n+2)$

59. $2(m+s)(n-t)$ **61.** $x=5$ **63.** 25; 2 *real*; 7 *and* 2 **65.** $(c-6)+\dfrac{38c-28}{c^2+3c-2}$

67. -7 **69.** $15x^2+60x+40$ **71.** $6x-4$ **73.** $6x-2$

75. $f^{-1}(x)=2x+\dfrac{2}{3}$ **77.** $\dfrac{m-5}{m}$ **79.** $3(a-3)$ **81.** $\dfrac{x}{15}$ **83.** $\dfrac{4a+6}{3a(a+1)}$

85. $\dfrac{1}{z}$ **87.** $\dfrac{2x-1}{x+3}$ **89.** $x=4,\ -\dfrac{2}{3}$

21