

## “I Can” Mascoma Standards High School Math

### I Can Use Complex Numbers to Help Me Understand Math

- I can recognize a complex number  $i$  where  $i^2 = -1$  and  $i = \sqrt{-1}$  (NQ.9-12. CN. 1)
- I can represent every complex number in the form  $a + bi$ , where  $a$  and  $b$  are real numbers. (NQ.9-12. CN. 1)
- I can add and subtract complex numbers using the commutative and associative properties. (NQ.9-12. CN. 2)
- I can multiply complex numbers using the commutative, associative, and distributive properties. (NQ.9-12. CN. 2)
- I can use the equation  $i^2 = -1$  to prove that  $i^4 = i^8 = i^{4k}$  where  $k$  is a positive integer. (NQ.9-12. CN. 2)
- I can use the equation  $i^2 = -1$  to prove that  $i^{-5} = i^{-9} = i^{-4k-3}$  where  $k$  is a positive integer.. (NQ.9-12. CN. 2)
- I can determine the conjugate of a complex number and determine the quotients of a set of complex numbers by using the conjugate of the denominator. (NQ.9-12. CN. 3)
- I can use the equations  $(\sqrt{a^2 + b^2} = r)$  to determine the modulus,  $r$ , of a complex number. (NQ.9-12. CN. 3)

Keywords: complex number,  $a+bi$ , commutative, associative, distributive, properties, conjugate, modulus, quotient

- I can represent complex numbers on the complex plane in rectangular form. (NQ. 9-12. CN. 4)
- I can represent complex numbers on the complex plane in polar form. (NQ. 9-12. CN. 4)
- I can explain why rectangular and polar forms of a complex number represent the same number. (NQ. 9-12. CN.4)

- I can represent addition, subtraction, multiplication, and conjugation of complex numbers geometrically on a complex plane. (NQ. 9-12. CN.5)
- I can use properties of this representation for computing, for example,  $(-1 + \sqrt{3}i)^3 = 8$  because  $(-1 + \sqrt{3}i)$  has modulus 2 and argument  $120^\circ$ . (NQ. 9-12. CN.5)
- I can determine whether it is desirable to use polar or rectangular form to add, subtract, multiply, or divide complex numbers. (NQ. 9-12. CN.4)
- I can calculate the distance between numbers in the complex plane as the modulus of the difference, and the midpoint of a segment as the average of the numbers at its endpoints. (NQ. 9-12. CN.5)

Keywords: complex number,  $a+bi$ , commutative, associative, distributive, properties, conjugate, modulus, quotient, polar, rectangular, form, plane

- I can determine if a quadratic equation with real coefficients has complex roots. (NQ. 9-12. CN.7)
- I can solve quadratic equations with real coefficients and present the solution as a complex number. (NQ. 9-12. CN.7)
- I can extend polynomial identities to the complex numbers such as rewriting  $x^2 + 4$  as  $(x + 2i)(x - 2i)$ . (NQ. 9-12. CN.8)
- I can understand the Fundamental Theorem of Algebra showing that it is true for quadratic polynomials. (NQ. 9-12. CN.9)

$$\begin{aligned}
 & y = x^2 + 2x - 3 \\
 & \frac{-2 \pm \sqrt{(2)^2 - 4(1)(-3)}}{2(1)} \\
 & \quad \downarrow \\
 & \frac{-2 \pm \sqrt{4 + 12}}{2} \rightarrow \frac{-2 \pm \sqrt{16}}{2} \\
 & \frac{-2 \pm 4}{2} \rightarrow \begin{cases} \frac{-2+4}{2} \rightarrow \frac{2}{2} \rightarrow 1 \\ \frac{-2-4}{2} \rightarrow \frac{-6}{2} \rightarrow -3 \end{cases}
 \end{aligned}$$

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Keywords: complex number,  $a+bi$ , polynomial, coefficient, solution, Fundamental Theorem, quadratic equation

## I Can Use Quantities to Help Me Understand Math

I can apply units consistently when solving a multi-step problem and consistently label each unit to maintain accuracy. (NQ.9-12.Q.1)

I can select appropriate units when solving real world problems. (NQ.9-12.Q.1)

Provides:	Nominal	Ordinal	Interval	Ratio
"Counts," aka "Frequency of Distribution"	✓	✓	✓	✓
Mode, Median		✓	✓	✓
The "order" of values is known		✓	✓	✓
Can quantify the difference between each value			✓	✓
Can add or subtract values			✓	✓
Can multiply and divide values				✓
Has "true zero"				✓

I can scale graphs and data displays appropriately when solving problems. (NQ.9-12.Q.2)

I can define relevant quantities when examining a set of data. (NQ.9-12.Q.2)

I can choose relevant units of measure for each variable or quantity in a set of data. (NQ.9-12.Q.2)

I can decide on the level of specificity of measurement data appropriate for a given measurement tool. (NQ.9-12.Q.3)

Keywords: quantity, measurement, unit, convert, graph, data scale, modeling, accuracy

## I Can Use the Real Number System to Help Me Understand Math

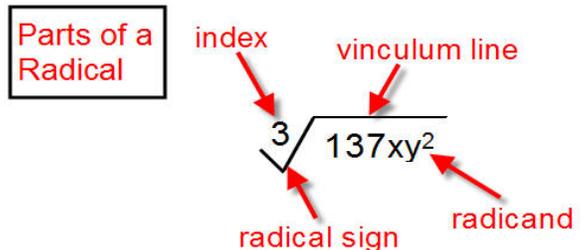
I can explain how the definition of the meaning of rational exponents follows from extending the properties on integer exponents of those values. (NQ.9-12.RN.1)

I can understand the properties of exponents and use them to simplify expressions containing radical exponents. (NQ.9-12.RN.1)

I can understand the properties of exponents and use them to simplify expressions containing integer exponents. (NQ.9-12.RN.2)

I can demonstrate my understanding that for  $n$  (2, 3, 4, ...),  $(x^{1/n})^n = x$ , and I can show why this is true. (NQ.9-12.RN.2)

I can demonstrate my understanding that  $x^{1/n} = \sqrt[n]{x}$  because  $(\sqrt[n]{x})^n$  and  $(x^{1/n})^n = x$ , as well. (NQ.9-12.RN.2)



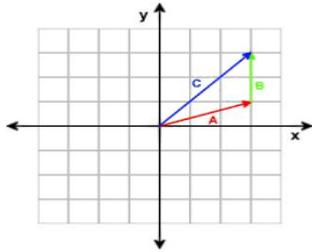
I can rewrite radical expressions as expressions with radical exponents, and vice-versa. (NQ.9-12.RN.2)

I can understand the definitions of rational and irrational numbers and explain why the sum of two rational numbers is rational, the sum of a rational and irrational number is irrational, and the product of a nonzero rational number and irrational number is irrational. (NQ.9-12.RN.3)

Keywords: rational, irrational, exponent, expression, integer, property, radical, root, real

### I Can Use Vector and Matrix Quantities to Help Me Understand Math

I can recognize both vector quantities of magnitude/length and direction/angle, and can represent vector quantities by directed line segments, such as  $\vec{v} = \overline{RT}$ , where R is the initial point and T is the terminal point. (NQ.9-12.VM.1)



I can use appropriate symbols for vectors and their magnitudes ( $v$ ,  $\vec{v}$ ,  $|v|$ ,  $||v||$ , etc.). (NQ.9-12.VM.1)

I can subtract coordinates of an initial point,  $R$ , from the coordinates of a terminal point,  $T$ , to find the components of a vector as follows:  
 $v = \langle v_1, v_2 \rangle = \langle T_1 - R_1, T_2 - R_2 \rangle$ . (NQ.9-12.VM.2)

I can solve problems where quantities can be represented by vectors and decide if these vectors can be represented by components, or by magnitude/length and direction/angle. (NQ.9-12.VM.3)

I can understand and solve real-world problems involving vectors. (NQ.9-12.VM.3)

I can solve problems involving velocity, force and other quantities by performing operations with vectors such as addition, subtraction, and scalar multiplication. (NQ.9-12.VM.3)

Keywords: vectors, velocity, force, magnitude, length, direction, angle, scalar multiplication, addition, subtraction, x axis, y axis, point, initial, terminal, coordinates

I can add vectors end-to-end. (NQ.9-12.VM.4)

I can add vectors component-wise. (NQ.9-12.VM.4)

- I can add vectors using the parallelogram rule. (NQ.9-12.VM.4)
- I can understand that the magnitude of a sum of two vectors is typically not the sum of the magnitudes. (NQ.9-12.VM.4)
- I can determine the magnitude and direction of the sum of two vectors presented in magnitude and direction form. (NQ.9-12.VM.4)
- I can understand vector subtraction  $v-w$  as  $v + (-w)$ , where  $-w$  is the additive inverse of  $w$ , with the same magnitude as  $w$  and pointing in the opposite direction. (NQ.9-12.VM.4)
- I can perform vector subtraction component-wise. (NQ.9-12.VM.4)
- I can represent vector subtraction graphically by connecting the tips in the correct order. (NQ.9-12.VM.4)

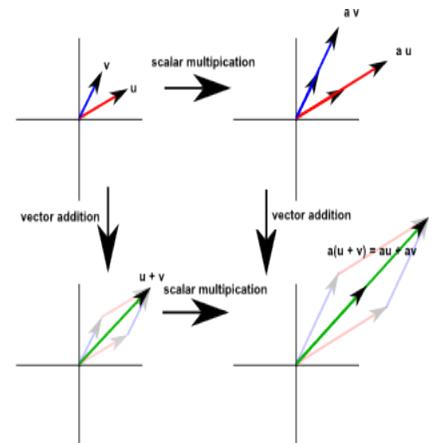
Keywords: vectors, velocity, force, magnitude, length, direction, angle, subtraction, x axis, y axis, point, initial, terminal, coordinates

- I can represent scalar multiplication graphically by scaling vectors and possibly reversing their direction. (NQ.9-12.VM.5)

- I can perform scalar multiplication component wise (for example,  $c(v_x, v_y) = (cv_x, cv_y)$ ). (NQ.9-12.VM.5)

- I can compute the magnitude of a scalar  $cv$  using  $\|cv\| = |c|v$ . (NQ.9-12.VM.5)

- I can compute the direction of  $cv$  knowing that when  $|c|v \neq 0$ , the direction of  $cv$  is either along  $v$  (for  $c > 0$ ) or against  $v$  (for  $c < 0$ ). (NQ.9-12.VM.5)



- I can perform operations on matrices and use matrices in applications. (NQ.9-12.VM.5)

Keywords: vectors, velocity, force, magnitude, length, direction, angle, scalar, multiplication, x axis, y axis, point, initial, terminal, coordinates, matrix (matrices)

- I can use matrices to represent and manipulate data. For example, I can represent payoffs or incidence relationships in a network. (NQ.9-12.VM.6)
- I can multiply matrices by scalars to produce new matrices. (NQ.9-12.VM.7)
- I can manipulate matrices to solve real world problems. (NQ.9-12.VM.7)
- I can add, subtract, and multiply matrices of appropriate dimensions (NQ.9-12.VM.8)
- I can explain why matrix multiplication for square matrices is not a commutative operation. (NQ.9-12.VM.9)
- I can explain why matrix multiplication for square matrices still satisfies the associative and distributive properties. (NQ.9-12.VM.9)

Keywords: vectors, velocity, force, magnitude, length, direction, angle, scalar, multiplication, x axis, y axis, point, initial, terminal, coordinates, matrix (matrices), commutative, associative, distributive

- I can explain how the role of zero and identity matrices behave in adding and multiplying matrices similarly to the role of 0 and 1 in real numbers. For example, I can explain that, as  $x+0=x$ , and  $x(1)=x$ , *Matrix*  $M+0=$  *Matrix*  $M$ , and *Matrix*  $M(1) =$  *Matrix*  $M$ . (NQ.9-12.VM.10)

**Reminder from lesson 1**

- Note that any matrix multiplied by the identity matrix is itself.

$$\begin{pmatrix} 2 & 1 & -6 \\ -3 & 1 & 8 \\ 6 & 9 & 3 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 2 & 1 & -6 \\ -3 & 1 & 8 \\ 6 & 9 & 3 \end{pmatrix}$$

- And any matrix multiplied by the zero matrix is the zero matrix.

$$\begin{pmatrix} 2 & 1 & -6 \\ -3 & 1 & 8 \\ 6 & 9 & 3 \end{pmatrix} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

- I can calculate the determinate of a square matrix. (NQ.9-12.VM.10)
- I can calculate the multiplicative inverse of a square matrix. (NQ.9-12.VM.10)
- I can understand that when the determinant of a square matrix equals 0, the matrix does not have a multiplicative inverse. (NQ.9-12.VM.10)
- I can multiply a vector (expressed as a one column matrix) by a matrix of suitable dimensions to produce another vector. (NQ.9-12.VM.11)
- I can use matrices to transform vectors by adding and multiplying them. (NQ.9-12.VM.11)
- I can calculate the transformation that is represented by a matrix, and the matrix that will produce a composite transformation. (NQ.9-12.VM.12)
- I can work with 2 x 2 matrices as transformations of the plane. (NQ.9-12.VM.12)

- I can interpret the absolute value of the determinant in terms of area. (NQ.9-12.VM.12)

Keywords: vectors, velocity, force, magnitude, length, direction, angle, scalar, multiplication, x axis, y axis, point, initial, terminal, coordinates, matrix (matrices), determinant, square, transformation, multiplicative inverse

## I can use the Building of Functions to Me Understand Math

- I can distinguish between and explicit and recursive expression of a function. (F.9-12.BF.1)
  - I can write an explicit expression of a function to describe a real world scenario. (F.9-12.BF.1)
  - I can write a recursive expression of a function to describe a real-world scenario. (F.9-12.BF.1)
- I can determine the steps for calculation for a real world scenario. (F.9-12.BF.1)
- I can combine standard function types using arithmetic operations for real world scenarios. (F.9-12.BF.1)
- I can compose functions to express real world scenarios. (F.9-12.BF.1)

**Recursive functions Examples**

$f(x) = f(x-1) + 3$   
refers to  $f$  in its own definition

$h(t) = 3h(t-1) + 11$   
refers to  $h$  in its own definition

$v(x) = 2v(x-1) + 3v(x-2)$   
refers to  $v$  in its own definition

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Keywords: equation, variable, function,  $f(x)$ , quantity, compose, build, operations

- I can distinguish between and explicit and recursive formula, and know what each will reveal about a given sequence. (F.9-12.BF.2)
  - I can distinguish between arithmetic and geometric sequences. (F.9-12.BF.2)
  - I can write explicit formulas for arithmetic and geometric sequences. (F.9-12.BF.2)
  - I can write recursive formulas for arithmetic and geometric sequences. (F.9-12.BF.2)

### Series Formulas

Arithmetic  
Series

$$S_n = \frac{n}{2} (a_1 + a_n)$$

Geometric  
Series

$$S_n = \frac{a_1 \cdot (1 - r^n)}{(1 - r)}$$

- I can identify when a real world scenario models an arithmetic sequence. (F.9-12.BF.2)
- I can identify when a real world scenario models a geometric sequence. (F.9-12.BF.2)
- I can translate between the recursive and explicit forms of both arithmetic and geometric sequences. (F.9-12.BF.2)

Keywords: equation, variable, function,  $f(x)$ , quantity, compose, build, operations, recursive, explicit, geometric, arithmetic, model, sequence, translate

- I can explain the effect of  $f(x) + k$  on the original graph  $f(x)$  for both a positive and negative value for  $k$  and find the value of  $k$  given the graphs. (F.9-12.BF.3)
- I can explain the effect of  $kf(x)$  on the original graph  $f(x)$  for both a positive and negative value for  $k$  and find the value of  $k$  given the graphs. (F.9-12.BF.3)
- I can explain the effect of  $f(kx)$  on the original graph  $f(x)$  for both a positive and negative value for  $k$  and find the value of  $k$  given the graphs. (F.9-12.BF.3)
- I can explain the effect of  $f(x+k)$  on the original graph  $f(x)$  for both a positive and negative value for  $k$  and find the value of  $k$  given the graphs. (F.9-12.BF.3)
- I can use technology to illustrate the effects of transforming a function. (F.9-12.BF.3)
- I can recognize an even function from both its graph as well as its algebraic expression. (F.9-12.BF.3)
- I can recognize an odd function from both its graph as well as its algebraic expression. (F.9-12.BF.3)

Keywords: equation, variable, function,  $f(x)$ , quantity, compose, build, operations, transformation, graphing, even, odd

I can solve an equation of the form  $f(x) = c$  for a simple function  $f$  that has an inverse and write an expression for the inverse. (F.9-12.BF.4)

I can verify by composition that one function is the inverse of another. (F.9-12.BF.4)

I can understand how the horizontal line test can help me determine if a function has an inverse, and can use the test. (F.9-12.BF.4)

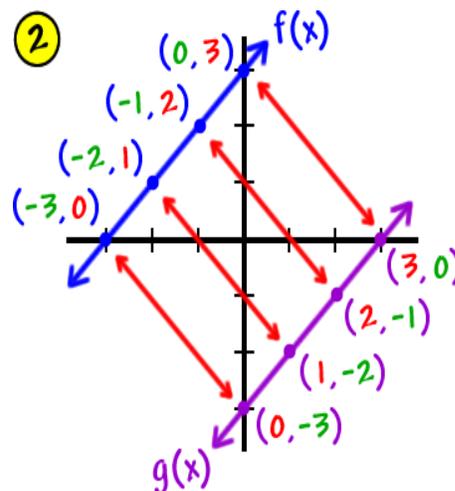
I can read values of an inverse function from a graph or table, given the function has an inverse. (F.9-12.BF.4)

I can understand how the vertical line test can help me determine if a function is represented in a given graph. (F.9-12.BF.4)

I can use the vertical line test to restrict the domain of a relation. (F.9-12.BF.4)

I can use the horizontal line test to restrict the domain of a relation. (F.9-12.BF.4)

I can produce an invertible function from a non-invertible function. (F.9-12.BF.4)



Keywords: equation, variable, function,  $f(x)$ , quantity, compose, build, operations, transformation, graphing, domain, invertible, non-invertible, horizontal, vertical

I can distinguish between exponential and logarithmic functions. (F.9-12.BF.4)

I can use the inverse relationship between exponential and logarithmic functions to solve problems involving them. (F.9-12.BF.4)

Keywords: equation, variable, function,  $f(x)$ , quantity, compose, build, logarithm, exponent

- I can explain the difference between domain and range. (F.9-12.IF.1)
- I can understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. (F.9-12.IF.1)
- I can explain that, if  $f$  is a function and  $x$  is an element of its domain, then  $f(x)$  denotes the output of  $f$  corresponding to the input  $x$ . (F.9-12.IF.1)
- I can explain that the graph of  $f$  is the graph of the equation  $y = f(x)$ . (F.9-12.IF.1)

$$f(x) = x + 1$$

↑ └───┘  
input                      output

- I can assign letters other than  $f$  to label and organize multiple, separate functions such as  $h(x)$  and  $g(x)$ . (F.9-12.IF.1)
- I can understand function notation and recognize how the input of a function,  $x$ , corresponds to its output,  $f$ . (F.9-12.IF.1)

- I can utilize function notation to describe data in a table or graph. (F.9-12.IF.2)
- I can understand how function notation can be applied to real world problems. (F.9-12.IF.2)

Keywords: equation, variable, function,  $f(x)$ , graph, domain, range,  $y=f(x)$ , notation, input, output

- I can analyze a set of integers (a sequence) and create a function whose domain is a subset of the integers. (F.9-12.IF.3)
- I can analyze a set of integers (a sequence) and generate additional integers according to the function whose domain is a subset of the integers. (F.9-12.IF.3)
- I can determine any element of a sequence by inputting its position into a given formula. (F.9-12.IF.3)
- I can interpret functions as they arise in real world applications. (F.9-12.IF.3)

□ I can interpret key features of graphs and tables in terms of the quantities for a function that models a relationship between two quantities. Thus, I can understand how relationships between two quantities are conveyed through:

$X$ and $Y$ intercepts	Ordered pairs	Increasing intervals
Decreasing intervals	Positive intervals	Negative intervals
Relative maximums	Negative minimums	Symmetries
Positive end behavior	Negative end behavior	Periodicity

(F.9-12.IF.4)

□ I can recognize key information in written problems as components of an underlying function and sketch a graph that conveys this information and indicates all key features of the underlying function. (F.9-12.IF.4)

Keywords: equation, variable, function,  $f(x)$ , graph, domain, range,  $y=f(x)$ , notation, input, output, sequence, integer

□ I can describe how the domain of a function is conveyed in graph form and, where applicable, to the quantitative relationship it describes. (F.9-12.IF.5)

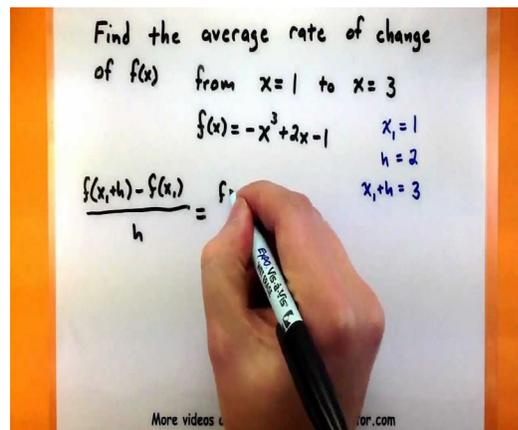
□ I can relate the domain of a function to its graph in real world scenarios. (F.9-12.IF.5)

□ I can calculate and interpret the average rate of change of a function presented symbolically over a specified interval. (F.9-12.IF.6)

□ I can calculate and interpret the average rate of change of a function presented in a table over a specified interval (F.9-12.IF.6)

□ I can calculate and interpret the average rate of change of a function presented in functional notation over a specified interval (F.9-12.IF.6)

□ I can estimate the rate of change from a graph . (F.9-12.IF.6)



Keywords: equation, variable, function,  $f(x)$ , graph, domain, range,  $y=f(x)$ , rate, change, slope, interval

I can decide how best to display a function graphically, either by hand or by using technology. (F.9-12.IF.7)

I can graph linear functions  $f(x)=x$  and understand:

- point-slope form as  $y-y_1=m(x-x_1)$
- slope-intercept form as  $f(x)=mx+b$
- standard form as  $Ax+By=C$

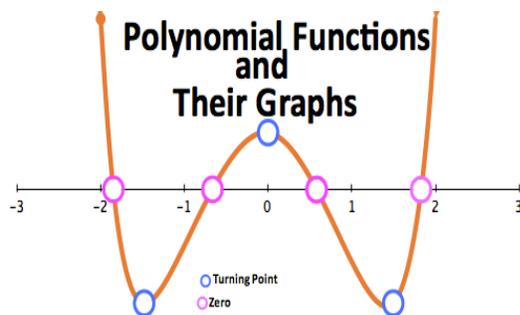
and determine the  $x$ - and  $y$ - intercepts for each graph. (F.9-12.IF.7)

I can graph quadratic functions  $f(x) = x^2$ , can understand that the vertex of a quadratic function is either the maximum or the minimum, and can identify which it will be by analyzing the equation. I can determine the  $x$ - and  $y$ - intercepts for a quadratic. (F.9-12.IF.7)

I can graph square root functions  $f(x) = \sqrt{x}$ , cube root functions  $f(x) = \sqrt[3]{x}$ , and piecewise-defined functions. (F.9-12.IF.7)

I can graph step functions by substituting values for  $x$  and plotting the points. (F.9-12.IF.7)

I can graph absolute value function  $f(x) = |x|$ , and can understand the vertex of an absolute value function is either the maximum or the minimum, and can identify which it will be by analyzing the equation. I can determine the  $x$ - and  $y$ - intercepts for an absolute value. (F.9-12.IF.7)



I can graph polynomial functions, identifying zeros when suitable factorizations are available, and showing end behavior. (F.9-12.IF.7)

I can explain rational functions as the ratio of two polynomials, and graph them, identifying zeros. (F.9-12.IF.7)

**Keywords:** graph, function, linear, quadratic, square root, cube root, piecewise, step, absolute value, polynomial, factorization, end behavior, x-intercept, y-intercept, slope

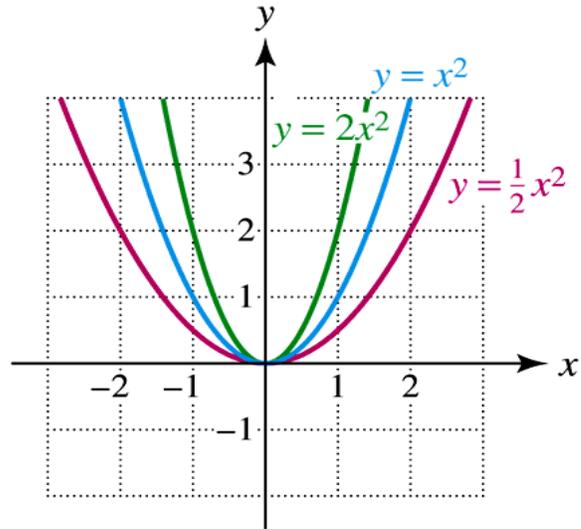
I can explain that, for a quadratic function, standard form is  $f(x) = ax^2 + bx + c$ ; that vertex form is  $f(x) = a(x-h)^2 + k$  where point  $(h,k)$  is the location of the vertex; and that factored form is  $f(x) = a(x-x_1)(x-x_2)$  where  $x_1$  and  $x_2$  are x-intercepts. (F.9-12.IF.8)

I can explain that all quadratic functions result in graphs that are parabolas. (F.9-12.IF.8)

I can determine if a quadratic has x-intercepts by analyzing the equation and use x-intercepts of a quadratic to find the axis of symmetry. (F.9-12.IF.8)

I can use the axis of symmetry to determine the vertex of a quadratic. (F.9-12.IF.8)

I can convert a quadratic in one form to another form. (F.9-12.IF.8)



I can understand and interpret a quadratic function in a real-world problem or scenario. (F.9-12.IF.8)

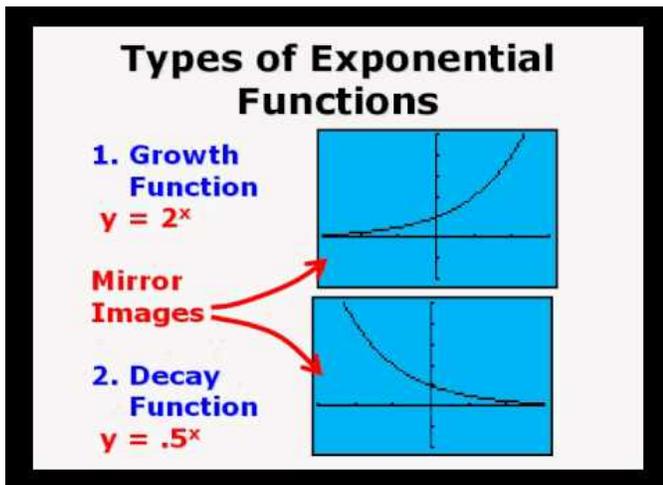
I can classify exponential models that represent exponential growth and exponential decay. (F.9-12.IF.8)

I can use properties of exponents to interpret expressions for exponential functions. (F.9-12.IF.8)

I can compare properties of two functions, each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). (F.9-12.IF.9)

Keywords: graph, function, linear, quadratic, x-intercept, y-intercept, slope, parabola, exponent, growth, decay, percentage

- I can distinguish between linear functions and exponential functions. (F.9-12.LQE.1)
- I can prove that a linear function has a constant slope over equal intervals. (F.9-12.LQE.1)
- I can prove that an exponential functions grows by a constant multiplier over equal intervals. (F.9-12.LQE.1)
- I can recognize situations (real world as well as theoretical) in which a quantity grows or decays by a constant rate per unit interval relative to another. (F.9-12.LQE.1)



- I can recognize situations (real world as well as theoretical) in which a quantity grows or decays by a constant percent rate per unit interval relative to another. (F.9-12.LQE.1)
- I can explain why a function is linear or exponential from data presented in a graph, a table, or a written description. (F.9-12.LQE.1)

- I can construct linear and exponential functions including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table). (F.9-12.LQE.2)

Keywords: equation, variable, function,  $f(x)$ , quantity, composition, build, operations

- I can distinguish use graphs and tables to show and compare the different output values and rates of change for linear, quadratic, exponential, and polynomial functions. (F.9-12.LQE.3)
- I can understand that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or as a polynomial function. (F.9-12.LQE.3)
- I can describe the inverse relationship of exponential and logarithmic functions. (F.9-12.LQE.4)

- I can rewrite an exponential equation in logarithmic form and explain why it is equivalent. (F.9-12.LQE.4)
- I can evaluate a logarithm using technology such as a calculator. (F.9-12.LQE.4)
- I can interpret and understand the quantities, rates of change, and other values of a linear function  $f(x) = mx + b$  in the context of a real-world scenario. (F.9-12.LQE.5)
- I can interpret and understand the quantities, rates of change, and other values of an exponential function  $f(x) = b^x + c$ . (F.9-12.LQE.5)

Keywords: equation, variable, function,  $f(x)$ , graph, table, linear, quadratic, exponential, polynomial, logarithm

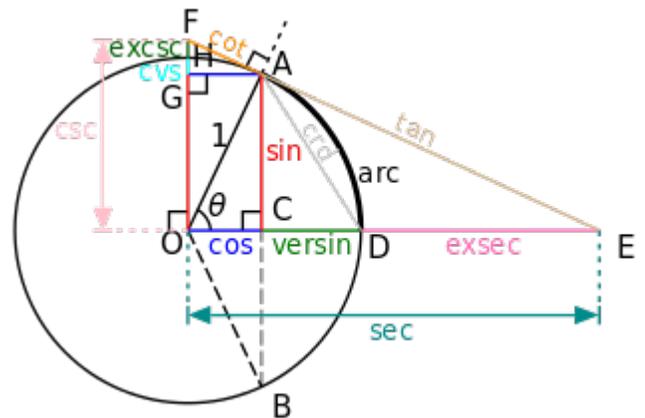
- I can define unit circle, radian measure of an arc, and intercepted arc. (F.9-12.TF.1)
- I can understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle. (F.9-12. TF.1)
- I can define cosine and sine of angles on the unit circle to be the x-coordinates and y-coordinates respectively, where the terminal rays of the angle cross the circle. (F.9-12. TF.2)

□ I can distinguish between the right triangle definitions of sine and cosine and the unit circle definitions of sine and cosine. (F.9-12. TF.3)

□ I can define and identify co-terminal angles and can express the measure of an angle as a radian. (F.9-12. TF.3)

□ I can create a right isosceles triangle in quadrant one of a unit circle and use it to determine cosine, sine, and tangent of  $\pi/4$ . (F.9-12. TF.3)

□ I can create an equilateral triangle centered on the positive x-axis of the unit circle to determine cosine, sine, and tangent of  $\pi/6$ . (F.9-12. TF.3)



I can combine geometric reflection with the values of cosine, sine, and tangent of  $\pi/6$  to determine cosine, sine, and tangent of  $\pi/3$ . (F.9-12. TF.3)

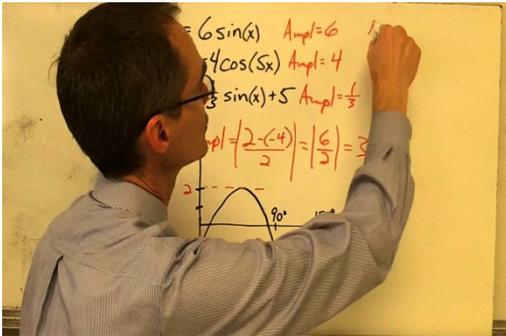
I can employ reference angles, reflections and rotations to find the values of sine, cosine, and tangent for  $x$ ,  $\pi+x$ , and  $2\pi-x$  in terms of their values for  $x$ . (F.9-12. TF.3)

Keywords: circle, radian, pi, triangle, unit, coordinate, plane, x-axis, y-axis, isosceles, equilateral, reference, arc, angle, geometric, reflection, rotation, sine, cosine, tangent

I can define unit circle, radian measure of an angle, and periodicity. (F.9-12. TF.4)

I can show why cosine functions are even and the sine and tangent functions are odd by using angle measurements and their coordinates on the unit circle. (F.9-12. TF.4)

I can demonstrate why the period for tangent is  $\pi$  and for cosine and sine is  $2\pi$  by referencing the unit circle. (F.9-12. TF.4)



I can show why cosine functions are even and sine and tangent functions are odd by using reflections. (F.9-12. TF.4)

I can understand amplitude, frequency and midline. (F.9-12. TF.5)

I can create a trigonometric function that models a real-world scenario given the amplitude, frequency, and mid-line of periodic phenomena. (F.9-12. TF.5)

Keywords: circle, radian, pi, triangle, unit, coordinate, plane, x-axis, y-axis, arc, geometric, reflection, rotation, sine, cosine, tangent, periodic, phenomena, amplitude, frequency, midline

I can define horizontal line test and restrict the domain of a trigonometric function by removing values of  $x$  that do not pass the horizontal line test. (F.9-12. TF.6)

I can show why trigonometric functions do not have inverses using graphs of the functions from  $0$  to  $2\pi$ . (F.9-12. TF.6)

- I can create a trigonometric function that models a real-world scenario given the amplitude, frequency, and midline of periodic phenomena. (F.9-12. TF.7)
- I can use inverse functions to solve trigonometric equations that arise in modeling contexts. (F.9-12. TF.7)
- I can create a real-world problem scenario, write a trigonometric function to model the scenario, solve the equation and interpret the solutions in terms of the scenario. (F.9-12. TF.7)

Keywords: circle, radian, pi, triangle, unit, coordinate, plane, x-axis, y-axis, arc, geometric, reflection, rotation, sine, cosine, tangent, periodic, phenomena, amplitude, frequency, midline, horizontal line test, restrict, domain, model, real world

- I can prove the Pythagorean identity  $\sin^2(\theta) + \cos^2(\theta) = 1$  by combining the Pythagorean Theorem with the unit circle definitions of cosine and sine. (F.9-12. TF.8)

- I can use the Pythagorean identity  $\sin^2(\theta) + \cos^2(\theta) = 1$  to find  $\sin^2(\theta)$  or  $\cos^2(\theta)$  provided I am given  $\sin^2(\theta)$  or  $\cos^2(\theta)$  and the quadrant of the angle. (F.9-12. TF.8)

- I can calculate  $\tan(\theta)$  by applying the quotient identity. (F.9-12. TF.8)

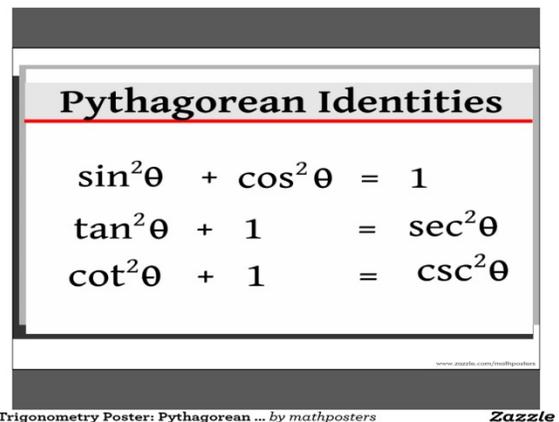
- I can prove the sum of angles identities for cosine and sine with right angles. (F.9-12. TF.8)

- I can derive the difference of angles identities from the sum of angles identities. (F.9-12. TF.9)

- I can determine angle identity for tangent with the sum and difference formulas for sine and cosine. (F.9-12. TF.9)

- I can use the addition and subtraction formulas for sine, cosine, and tangent to derive the values of trigonometric functions of different angles. (F.9-12. TF.9)

Keywords: circle, radian, pi, triangle, unit, coordinate, plane, x-axis, y-axis, arc, geometric, reflection, rotation, sine, cosine, tangent, periodic, phenomena, amplitude, frequency, midline



# I can Use Algebra to Help Me Understand Math

- I can explain the distinguishing factors of a term, a factor, a co-efficient, and an expression. (A.9-12.SSE.1)
- I can understand the context of expressions that represent a quantity. (A.9-12.SSE.1)
- I can interpret an expression functioning as one or more single entities containing multiple components. (A.9-12.SSE.1)
- I can rewrite the structure of an expression by identifying common factors, terms, and other similarities. (A.9-12.SSE.2)
- I can identify equivalent expressions according to their common factors, terms, and other similarities. (A.9-12.SSE.2)

Keywords: expression, term, factor, factoring, coefficient, equation

- I can factor a quadratic expression to reveal the zeros of the function it defines. (A.9-12.SSE.3)

*this makes it Quadratic*

$$5x^2 - 3x + 3 = 0$$

- I can complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines. (A.9-12.SSE.3)

- I can use the properties of exponents to transform expressions for exponential functions. For example, I can rewrite the expression  $1.15t$  as  $(1.151/12) 12t \approx 1.01212t$  to reveal the approximate equivalent monthly interest rate if the annual rate is 15%. (A.9-12.SSE.3)
- I can explain what finite geometric series and common ratios are. (A.9-12.SSE.4)
- I can express the sum of a finite geometric series when the common ratio is not one. (A.9-12.SSE.4)
- I can determine the formula of a sum of finite geometric series to solve real world math problems. (A.9-12.SSE.4)

Keywords: expression, term, factor, factoring, coefficient, equation, geometric, sequence, finite, series, common, ratio

- I can understand the definition of a polynomial and show how adding, subtracting, and multiplying two polynomials always produces a polynomial. (A.9-12.APR.1)
- I can add polynomials. (A.9-12. APR.1)
- I can subtract polynomials. (A.9-12. APR.1)
- I can multiply polynomials. (A.9-12. APR.1)

Keywords: polynomial, add, subtract, multiply, integer, definition

- I can divide polynomials using long division. (A.9-12.APR.2)
- I can understand and apply the Remainder Theorem to show that, for polynomial  $p(x)$  and a number  $b$ , the remainder on division by  $x-b$  is  $p(b)$ , so  $p(b) = 0$  if and only if  $(x-b)$  is a factor of  $p(x)$  . (A.9-12. APR.2)

$$\begin{array}{r}
 2x + 1 \\
 x-3 \overline{) 2x^2 - 5x - 1} \\
 - 2x^2 - 6x \\
 \hline
 0 + 1x - 1 \\
 - \quad x - 3 \\
 \hline
 0 + 2 \text{ Remainder}
 \end{array}$$

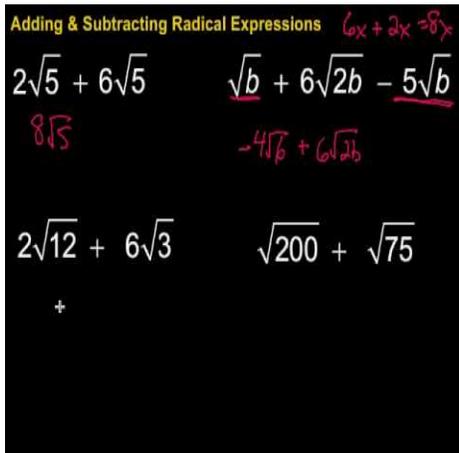
- I can identify zeros of polynomials when suitable factorizations are available. (A.9-12. APR.3)
- I can use zeros of polynomials to construct a rough graph of the function defined by the polynomial. (A.9-12. APR.3)

Keywords: polynomial, definition, divide, Remainder Theorem, zero, graph, function

- I can prove polynomial identities and use them to describe numerical relationships. For example, I can show how the polynomial identity  $(x^2+y^2)^2 = (x^2 - y^2)^2 + (2xy)^2$  can be used to generate Pythagorean triples . (A.9-12. APR.4)
- I can factor polynomials by applying polynomial identities. (A.9-12. APR.4)
- I can know and apply the Binomial Theorem for the expansion of  $(x + y)^n$  in powers of  $x$  and  $y$  for a positive integer  $n$ , where  $x$  and  $y$  are any numbers  $(x + y)^n = {}_nC_0a^n b^0 + {}_nC_1a^{n-1}b^1 + {}_nC_2a^{n-2}b^2 + \dots + {}_nC_n a^0 b^n$ . (A.9-12. APR.5)

Keywords: polynomial, identity, Pythagorean, triple, factoring, binomial, theorem

- I can rewrite simple rational expressions in different forms. (A.9-12. APR.6)
- I can write a rational expression  $\frac{a(x)}{b(x)}$  in the form  $q(x) + \frac{r(x)}{b(x)}$ , where  $a(x)$ ,  $b(x)$ ,  $q(x)$ , and  $r(x)$  are polynomials with the degree of  $r(x)$  less than the degree of  $b(x)$ . (A.9-12. APR.6)
- I can simplify radical expressions using inspection. (A.9-12. APR.6)
- I can simplify radical expressions using long division. (A.9-12. APR.6)



- I can simplify radical expressions using a computer-based algebra program. (A.9-12. APR.6)
- I can explain why adding, subtracting, multiplying two rational expressions, and dividing a rational expression by a non-zero rational expression always yields a rational expression. (A.9-12. APR.7)
- I can add, subtract, multiply, and divide rational expressions. (A.9-12. APR.7)

Keywords: polynomial, identity, rational, expression, addition, subtraction, multiplication, division

- I can create equations and inequalities (arising from linear functions, quadratic functions, simple rational functions, and exponential functions) in one variable and use them to solve problems, including real-world problems. (A.9-12. CED.1)
- I can create equations in two or more variables to represent relationships between quantities, as well as graph equations on coordinate axes with labels and scales. (A.9-12. CED.2)
- I can represent constraints by equations or inequalities. (A.9-12. CED.3)
- I can represent constraints by systems of equations and/or inequalities. (A.9-12. CED.3)
- I can determine which solutions are appropriate for the context of a given real-world problem. (A.9-12. CED.3)

I can rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations, such as rearranging Ohm's Law  $V=IR$  to highlight resistance, or  $R$ . (A.9-12. CED.4)

Keywords: equation, inequality, variable, linear, quadratic, rational, exponential, function, graph, formula

I can understand solving equations as a process of reasoning and explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step. (A.9-12. REI.1)

I can construct a viable argument to justify the solution method I have chosen. (A.9-12. REI.1)

I can explain what extraneous solutions are, and how they may arise while solving equations. (A.9-12. REI.1)

I can solve simple rational equations in one variable. (A.9-12. REI.2)

I can solve radical equations in one variable. (A.9-12. REI.2)

$$\left(\frac{2x + 3}{6}\right)^6 = \left(\frac{3x + 1}{6}\right)^6$$

$$2x + 3 - 1 = 3x + 1 - 1$$

$$2x + 2 - 2x = 3x - 2x$$

$$2 = x$$

Keywords: equation, inequality, variable, argument, solution, method, extraneous, radical

I can solve linear equations in one variable, including equations with coefficients represented by letters. (A.9-12. REI.3)

I can solve linear inequalities in one variable, including equations with coefficients represented by letters. (A.9-12. REI.3)

I can identify and factor a perfect square trinomial. (A.9-12. REI.3)

I can complete the square to transform any quadratic equation in  $x$  into an equation of the form  $(x-p)^2 = q$  that has the same solutions. (A.9-12. REI.4)

I can derive the quadratic formula by completing the square of  $ax^2 + bx = c$ . (A.9-12. REI.4)

I can solve quadratic equations by inspection, taking square roots, completing the square, and/or by the quadratic formula and factoring, as appropriate to the initial form of the equation. (A.9-12. REI.4)

I can solve recognize when the quadratic formula gives complex solutions and write them as  $a \pm bi$  for real numbers  $a$  and  $b$ . (A.9-12. REI.4)

**Keywords:** equation, inequality, variable, linear, quadratic, rational, exponential, function, trinomial, square, complex, i, factor

I can show that when an equation is multiplied by the same quantity on both sides of the equal sign, an equivalent equation results. (A.9-12. REI.5)

I can demonstrate that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solution. (A.9-12. REI.5)

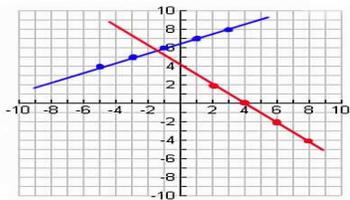
I can solve systems of linear equations exactly and approximately (for example, with graphs, where I can estimate the point of intersection between each line), focusing on pairs of linear equations in two variables. (A.9-12. REI.6)

**Keywords:** equation, inequality, variable, linear, quadratic, rational, exponential, function, graph, formula

#### Choosing a Linear, Quadratic, and Exponential Model

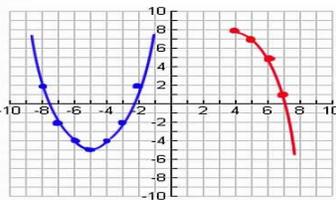
**Linear**

$$y = mx + b$$



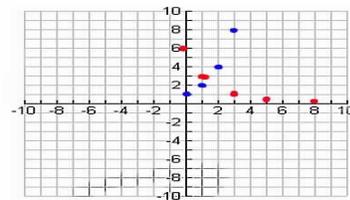
**Quadratic**

$$y = ax^2 + bx + c$$



**Exponential**

$$y = ab^{x-h} + k$$



I can explain the difference between linear and quadratic equations. (A.9-12. REI.7)

I can solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. (A.9-12. REI.7)

I can solve systems of linear equations exactly and approximately (for example, with graphs, where I can estimate the point of intersection between each line), focusing on pairs of linear equations in two variables. (A.9-12. REI.8)

I can represent a system of linear equations as a single matrix equation in a vector variable. (A.9-12. REI.8)

I can define the inverse of a matrix and calculate it, if it exists. (A.9-12. REI.9)

I can use the inverse of a matrix to solve systems of linear equations (using technology for matrices of dimension  $3 \times 3$  or greater. (A.9-12. REI.9)

Keywords: equation, variable, linear, quadratic, matrix, inverse, graph, solution

I can understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane (as represented by point variables  $x, y$ ). (A.9-12. REI.10)

I can explain why the  $x$ -coordinates of the points where the graphs of the equations  $y = f(x)$  and  $y = g(x)$  intersect are the solutions of the equation  $f(x) = g(x)$ . (A.9-12. REI.11)

I can approximate the solutions of the equations  $f(x) = g(x)$  by recognizing that the intersections of the graphs of the equations  $y = f(x)$  and  $y = g(x)$  will indicate a solution. (A.9-12. REI.11)

I can use appropriate tools (such as a computer or a graphing calculator) to solve systems of equations  $f(x) + g(x)$ , including cases where  $f(x)$  and/or  $g(x)$  are linear, polynomial, rational, absolute value, exponential, and logarithmic functions. (A.9-12. REI.11)

I can graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality). (A.9-12. REI.12)

- I can graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes. (A.9-12. REI.12)

Keywords: equation, variable, linear, quadratic, graph, solution, x-coordinate, y-coordinate, plane, intersect, inequality, plane, polynomial, rational, absolute, value, exponential, logarithm

## I can Use Geometry to Understand Math

- I can explain the characteristics of the undefined notions of point, line, distance along a line, and distance around a circular arc, and use these notions as a basis for defining other geometric elements. (G.9-12. CO.1)

- I can precisely define angle, circle, perpendicular line, parallel line, and line segment. (G.9-12. CO.1)

- I can draw transformations in the plane using transparencies, graph paper, computers or white boards. (G.9-12. CO.2)

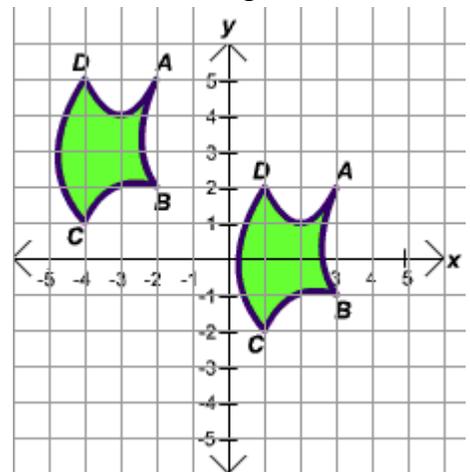
- I can describe transformations as functions that take points in the plane as inputs (pre-image) and other points as outputs (image). (G.9-12. CO.2)

- I can distinguish between transformations that preserve distance and angle to those that do not. (G.9-12. CO.2)

- I can distinguish between a rectangle, parallelogram, trapezoid, or regular polygon. (G.9-12. CO.3)

- I can describe the rotations and reflections a rectangle, parallelogram, trapezoid, or regular polygon carries onto itself. (G.9-12. CO.3)

Keywords: point, line, distance, segment, perpendicular, parallel, circle, angle, definition, transformation, plane, function, input, output, draw, graph, rectangle, parallelogram, trapezoid, polygon

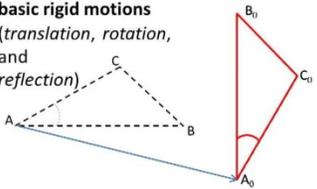


- I can explain the definition of rotation in terms of angles, circles, perpendicular lines, parallel lines, and line segments. (G.9-12. CO.4)
- I can explain the definition of reflection in terms of angles, circles, perpendicular lines, parallel lines, and line segments. (G.9-12. CO.4)
- I can explain the definition of translation in terms of angles, circles, perpendicular lines, parallel lines, and line segments. (G.9-12. CO.4)
- I can, given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using graph paper or other technology. (G.9-12. CO.5)
- I can specify a sequence of transformations that will carry a given figure onto another. (G.9-12. CO.5)

Keywords: point, line, distance, segment, perpendicular, parallel, circle, angle, definition, transformation, plane, function, input, output, draw, graph

- I can provide descriptions of rigid motions and explain how each preserves distance and angle. (G.9-12. CO.6)

Given two triangles with two pairs of equal sides and an included equal angle, a **composition of basic rigid motions** (*translation, rotation, and reflection*)



**maps the image of one triangle onto the other.**  
Therefore, the triangles are congruent.

- I can predict the effect of a given rigid motion on a given figure. (G.9-12. CO.6)
- I can define congruence as equality in shape and size and use congruence in terms of rigid motions to decide if two figures are congruent. (G.9-12. CO.7)

- I can recognize triangle congruence (ASA, SAS, SSS) in terms of rigid motions that preserve distance (S) and angle (A). (G.9-12. CO.8)

- I can show how preserving correlating distances (S) and angles (A) between two triangles results in congruence. (G.9-12. CO.8)

Keywords: point, line, distance, segment, perpendicular, parallel, angle, definition, transformation, plane, function, input, output, draw, graph, congruent, ASA, SAS, SSS, triangle, rigid, motion

I can prove theorems about lines and angles using deductive reasoning (such as the law of syllogism). (G.9-12. CO.9)

I can prove a theorem stating vertical angles are congruent. (G.9-12. CO.9)

I can prove a theorem stating when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent. (G.9-12. CO.9)

I can prove a theorem stating points on a perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints. (G.9-12. CO.9)

I can prove theorems about triangles using deductive reasoning (such as the law of syllogism). (G.9-12. CO.10)

I can prove a theorem about triangles such as measures of interior angles of a triangle sum to  $180^\circ$ . (G.9-12. CO.10)

I can prove theorems about parallelograms using deductive reasoning (such as the law of syllogism). (G.9-12. CO.11)

I can prove a theorem about parallelograms such as the diagonals of a parallelogram bisect each other. (G.9-12. CO.11)

**PARALLELOGRAM**

➤ *The diagonals of a parallelogram bisect each other*

**Given:** ABCD is a parallelogram where AC and BD is a diagonal bisect each other at Point O

**To Prove:**  $AO = OC$  or  $BO = OD$

**Proof:** In  $\triangle AOB$  and  $\triangle COD$

$AB = CD$

$AB \parallel CD$

$\angle CDO = \angle OBA$

And  $\angle DCO = \angle OAB$  ----- Alternate interior angles

So,  $\triangle AOB \cong \triangle COD$ , then

$AO = OC$  or  $BO = OD$  Proved

**Keywords:** point, line, distance, segment, perpendicular, parallel, angle, definition, transformation, plane, function, theorem, axiom, postulate, deductive, reasoning, law, syllogism, draw, graph, congruent, triangle, parallelogram, rectangle

I can define identify and correctly use tools such as a compass and straightedge, string, reflective devices, paper folding, and dynamic geometric software to create formal geometric constructions. (G.9-12. CO.12)

I can accurately create geometric constructions such as copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line. (G.9-12. CO.12)

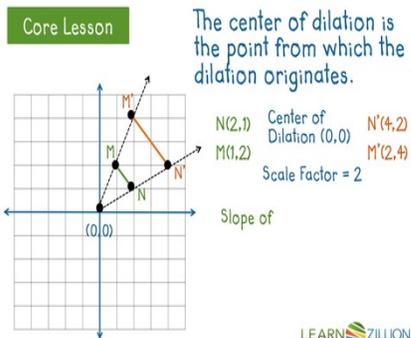
I can define polygons inscribed in a circle. (G.9-12. CO.12)

I can construct an equilateral triangle, a square, and a regular hexagon inscribe in a circle. (G.9-12. CO.13)

**Keywords:** point, line, distance, segment, perpendicular, parallel, angle, definition, transformation, plane, function, theorem, axiom, postulate, deductive, reasoning, law, syllogism, draw, graph, congruent, triangle, parallelogram, rectangle, construction, polygon, inscribe, equilateral, square, hexagon

I can explain the properties of dilations given by a center and a scale factor. (G.9-12. SRT.1)

I can perform dilations given by a center and a scale factor on figures in a plane. (G.9-12. SRT.1)



I can verify that a dilation takes a line not passing through the center of the dilation to a parallel line, and leaves a line passing through the center unchanged. (G.9-12. SRT.1)

I can verify that the dilation of a line segment is longer or shorter in the ratio given by the scale factor. (G.9-12. SRT.1)

I can explain similarity in terms of similarity transformations where angle measure is preserved and side length changes proportionally. (G.9-12. SRT.2)

I can determine if two figures are similar, including triangles. (G.9-12. SRT.2)

I can explain why, if two angle measures are known, the third angle is also known using the properties of similarity transformations. (G.9-12. SRT.3)

**Keywords:** point, line, distance, dilation, triangle, segment, angle, length, scale, factor, ratio, transformation, corresponding, AA, criterion

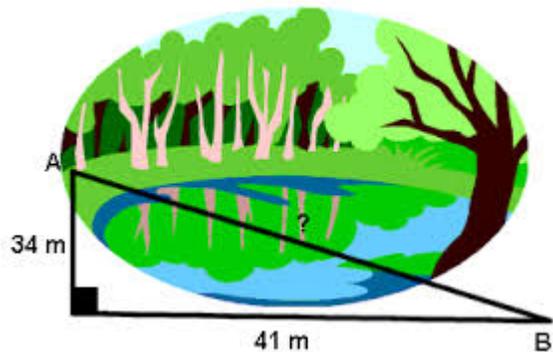
- I can prove theorems about triangles, such as a line parallel to one side of a triangle divides the other two proportionally, and conversely. (G.9-12. SRT.4)
- I can prove theorems about triangles, such as using triangles similarly to prove the Pythagorean Theorem. (G.9-12. SRT.4)
- I can apply the concepts of congruence and similarity criteria to solve problems involving triangles. (G.9-12. SRT.5)
- I can apply the concepts of congruence and similarity criteria to prove relationships in geometric figures. (G.9-12. SRT.5)

Keywords: point, line, distance, dilation, triangle, segment, angle, length, scale, factor, proof, theorem, axiom, postulate, similar, corresponding, proportion, figure, Pythagorean, parallel, side, split, congruent

- I can explain by angle-angle similarity of two right triangles that side ratios are properties of the angles in the triangle. (G.9-12. SRT.6)
- I can use similarity to define trigonometric ratios (tangent, sine, and cosine) for acute angles in right triangles. (G.9-12. SRT.6)
- I can determine cosine and sine ratios for acute angles in right triangles given the lengths of two sides. (G.9-12. SRT.6)
- I can explain the relationship between sine and cosine of complementary angles and construct a diagram to illustrate the relationship. (G.9-12. SRT.7)

I can express the Pythagorean Theorem as  $a^2 + b^2 = c^2$  and use it to find the unknown length of a right triangle side. (G.9-12. SRT.8)

I can use trigonometric ratios and the Pythagorean Theorem to solve real-world problems. (G.9-12. SRT.8)



I can define altitude as an auxiliary line extending from a vertex perpendicular to the opposite side. (G.9-12. SRT.9)

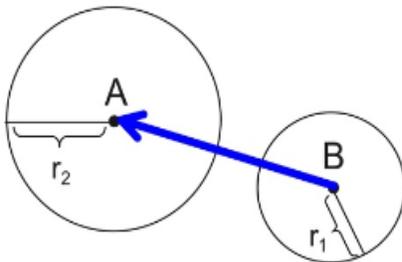
- I can derive the formula  $A = \frac{1}{2} ab \sin(c)$  for the area of a triangle. (G.9-12. SRT.9)

Keywords: point, line, distance, dilation, triangle, segment, angle, length, scale, factor, proof, theorem, axiom, postulate, similar, corresponding, proportion, figure, Pythagorean, parallel, congruent, application, sine, cosine, tangent

- I can prove the Law of Sines. (G.9-12. SRT.10)
- I can use the Law of Sines to formulate solutions in real-world scenarios. (G.9-12. SRT.10)
- I can prove the Law of Cosines. (G.9-12. SRT.10)
- I can use the Law of Cosines to formulate solutions in real-world scenarios. (G.9-12. SRT.10)
- I can distinguish between the problems that call for the Law of Sines and those that call for the Law of Cosines. (G.9-12. SRT.10)
- I can apply the Law of Sines to find the unknown measurements in right and non-right triangles. (G.9-12. SRT.11)
- I can apply the Law of Cosines to find the unknown measurements in right and non-right triangles. (G.9-12. SRT.11)

Keywords: point, line, distance, dilation, triangle, segment, angle, length, scale, factor, proof, theorem, axiom, postulate, similar, corresponding, proportion, figure, Pythagorean, congruent, application, sine, cosine, tangent

- I can prove similarities among all circles by demonstrating that the preimage of a dilation central to the circle is equal to the image in terms of the measure of the central angle. (G.9-12. C.1)



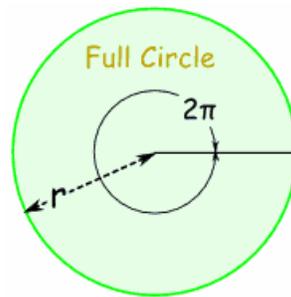
- I can define central angle, inscribed angle, circumscribed angle, diameter, radius, and chord. (G.9-12. C.2)

- I can explain the relationship between central, inscribed, and circumscribed angles. (G.9-12. C.2)
- I can explain that inscribed angles on a diameter are right angles. (G.9-12. C.3)
- I can explain that the radius of a circle is perpendicular to the tangent where the radius intersects the circle. (G.9-12. C.3)
- I can distinguish between inscribed and circumscribed circles of a triangle. (G.9-12. C.3)
- I can prove properties of angles for a quadrilateral inscribed in a circle, such as opposite angles in an inscribed quadrilateral are supplementary. (G.9-12. C.3)
- I can construct a tangent line from a point outside a given circle to the circle. (G.9-12. C.4)

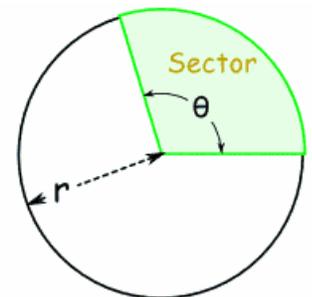
Keywords: circle, arc, chord, tangent, angle, central, point, radius, inscribed, circumscribed, proof, construction, line, point, dilation, intersect, perpendicular

- I can explain similarity in terms of similarity transformations where angle measure is preserved and side length changes proportionally. (G.9-12. C.5)

- I can use similarity to derive the fact that the length of the arc intercepted by an angle is proportional to the radius. (G.9-12. C.5)



$$A = \pi \times r^2$$



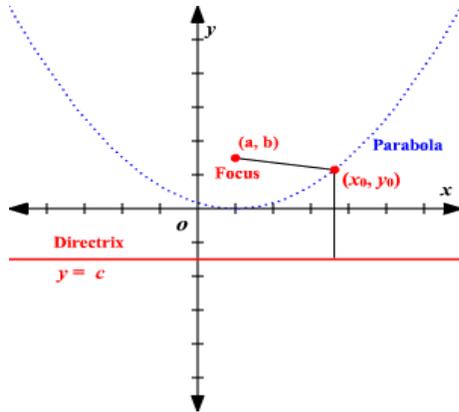
$$A = \left(\frac{\theta}{2\pi}\right) \times \pi \times r^2 = \left(\frac{\theta}{2}\right) \times r^2$$

- I can define the radian measure of the angle as a constant of proportionality. (G.9-12. C.5)

- I can derive the formula for the area of a sector. (G.9-12. C.5)

Keywords: circle, arc, chord, tangent, angle, central, point, radius, inscribed, circumscribed, proof, construction, line, point, dilation, intersect, perpendicular, sector, proportionality

- I can derive the equation of a circle of radius  $(r, r)$  by applying the Pythagorean Theorem to the right angle formed by extending the radius as the hypotenuse from the circle's center to a point on the circle  $(x, y)$ . (G.9-12. GPE.1)
- I can determine the center of a circle given the equation of the circle. (G.9-12. GPE.1)
- I can complete the square to find the center and the radius of a circle given by equation. (G.9-12. GPE.1)



- I can define parabola, focus, and directrix. (G.9-12. GPE.1)
- I can derive the equation of a parabola given a focus and directrix. (G.9-12. GPE.2)
- I can determine the distance from the focus of a parabola to a point on the parabola  $(x, y)$  using the Pythagorean Theorem. (G.9-12. GPE.2)

- I can distinguish between a parabola, ellipsis, and hyperbola. (G.9-12. GPE.3)
- I can determine the sum of the distances from each focus of an ellipse to a point on the ellipse  $(x, y)$  using the Pythagorean Theorem. (G.9-12. GPE.3)

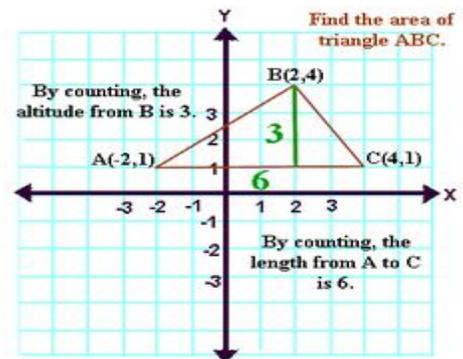
Keywords: circle, arc, chord, tangent, angle, central, point, radius, inscribed, Pythagorean, theorem, circumscribed, proof, square, parabola, focus, directrix, coordinate, Cartesian

- I can identify the appropriate algebraic method to prove or disprove simple geometric theorems given a set of coordinates. (G.9-12. GPE.4)
- I can use slope to determine if lines in a polygon are parallel. (G.9-12. GPE.5)
- I can use the Pythagorean Theorem to determine if the point  $(a, b)$  lies on a circle centered at the origin and containing the point  $(x, y)$ . (G.9-12. GPE.5)
- I can graph a line on the coordinate plane. (G.9-12. GPE.5)

- I can translate a line parallel to another line on the coordinate plane by preserving its angle. (G.9-12. GPE.5)
- I can determine if two lines are parallel by examining their slope. (G.9-12. GPE.5)
- I can find the equation of a line parallel or perpendicular to a given line that passes through a given point. (G.9-12. GPE.5)
- I can rotate a line perpendicular to another line on the coordinate plane. (G.9-12. GPE.35)
- I can determine if two lines are perpendicular by examining their slopes. (G.9-12. GPE.5)
- I can prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems. (G.9-12. GPE.5)

Keywords: circle, arc, chord, tangent, angle, central, point, radius, inscribed, Pythagorean, theorem, proof, square, parabola, focus, directrix, coordinate, Cartesian

- I can use the formula  $x = (r_2x_1 + r_1x_2) / (r_1 + r_2)$  to determine the point or points on a directed line segment  $(x_1, y_1)$   $(x_2, y_2)$  that partitions the segment in a given ration,  $r_1$  to  $r_2$ . (G.9-12. GPE.6)
- I can use coordinates to compute perimeters of polygons and areas of triangles and rectangles. (G.9-12. GPE.7)



Keywords: circle, arc, chord, tangent, angle, central, point, radius, inscribed, Pythagorean, theorem, proof, square, segment, ratio, polygon, triangle, rectangle, coordinate, Cartesian

- I can determine the formulas for the circumference of a circle, arc of a circle, volume of a cylinder, pyramid and cone. (G.9-12. GMD.1)

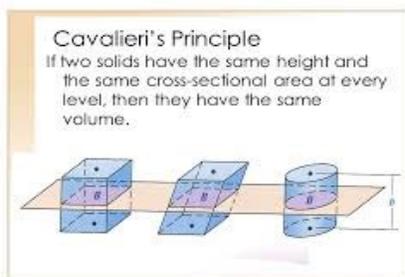
I can describe the relationship between the circumference and area of a circle. (G.9-12. GMD.1)

I can inscribe a polygon to determine its area. (G.9-12. GMD.1)

I can calculate the base area for a prism, cylinder, cone, and pyramid. (G.9-12. GMD.1)

I can determine the volume for a prism, cylinder, cone, and pyramid. (G.9-12. GMD.1)

I can explain the conceptual relationships among the volume formulas of prisms, cylinders, cones, and pyramids. (G.9-12. GMD.1)



I can use dissection arguments, Cavalieri's principle, informal limit arguments. (G.9-12. GMD.1)

I can explain Cavalieri's principle informally using everyday objects such as a stack of pennies to illustrate the principle. (G.9-12. GMD.2)

I can define the volume formulas for cylinders, pyramids, cones, and spheres. (G.9-12. GMD.3)

I can calculate the volume of cylinders, pyramids, cones and spheres to solve real-world problems. (G.9-12. GMD.3)

Keywords: circle, arc, chord, tangent, angle, central, point, radius, inscribed, Pythagorean, theorem, formula, Cavalieri's principle, indivisibles, method, cylinder, pyramid, cone, sphere, volume, circumference, dissection, limit

I can identify the shapes of two-dimensional cross-sections of three-dimensional objects. (G.9-12. GMD.4)

I can identify three-dimensional objects generated by rotations of two-dimensional objects. (G.9-12. GMD.5)

Keywords: circle, arc, chord, tangent, angle, central, point, radius, inscribed, Pythagorean, theorem, formula, Cavalieri's principle, indivisibles, method, cylinder, pyramid, cone, sphere, volume, circumference, dissection, limit

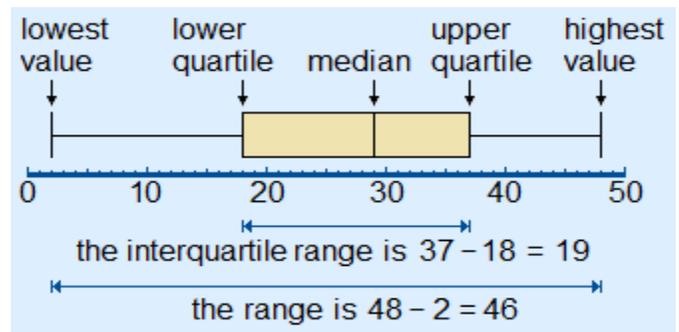
# I can Use Statistics and Probability to Understand Math

I can represent data on the real number line using dot plots, histograms, and box plots, understanding which approach best represents the data set. (SP.9-12.ID.1)

I can determine the appropriate range and scale when representing the data on the real number line. (SP.9-12.ID.2)

I can determine the five number summary when creating a box plot. (SP.9-12.ID.2)

I can define median, mean, interquartile range, and standard deviation. (SP.9-12.ID.2)



I can compare the center of the data distribution (median, mean) of multiple data sets. (SP.9-12.ID.2)

I can compare the spread (interquartile range, standard deviation) of multiple data sets. (SP.9-12.ID.2)

I can compare the shape, center, and spread of several data sets displayed on the same scale. (SP.9-12.ID.3)

I can compare the shape, center, and spread of several data sets within the context of a problem or real-world scenario. (SP.9-12.ID.3)

I can identify extreme data points in multiple data sets. (SP.9-12.ID.3)

I can account for possible effects of extreme data points and decide to omit them, if necessary. (SP.9-12.ID.3)

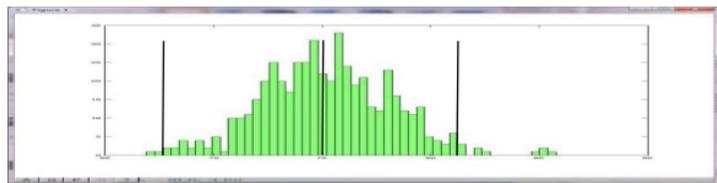
**Keywords:** data, set, statistics, distribution, spread, standard deviation, real, box plot, histogram, dot plot, range, interquartile, scale, mean, median, outlier, compare

I can use the mean and standard deviation of a data set to fit it to a normal distribution curve. (SP.9-12.ID.4)



### Three-Sigma Rule

- Three-sigma rule
  - ~68% of the values lie within 1 std deviation of the mean
  - ~95% of the values lie within 2 std deviations
  - 99.73% of the values lie within 3 std deviations



I can use the three-sigma rule to calculate the percent of a normal population that lies within three deviations of the mean. (SP.9-12.ID.4)

I can recognize that there are data sets (asymmetrical, for example) for which such a procedure is not accurate. (SP.9-12.ID.4)

I can use calculators, spreadsheets, and tables to estimate areas under the normal curve. (SP.9-12.ID.4)

Keywords: data, set, statistics, distribution, spread, standard deviation, real, box plot, histogram, dot plot, range, interquartile, scale, mean, median, outlier, compare, three-sigma rule, empirical, technology, normal population

I can represent data on a scatter plot given the data is on quantitative variables only. (SP.9-12.ID.5)

I can describe how quantitative variables are related on a scatter plot. (SP.9-12.ID.5)

I can decide which type of function (linear, quadratic, exponential) is appropriate to represent a data set. (SP.9-12.ID.5)

I can solve problems by using a function appropriately fitted to the data set. (SP.9-12.ID.5)

I can analyze the scale and shape of a scatter plot to estimate the function with the best fit for the data set. (SP.9-12.ID.6)

I can calculate and plot residuals for the data set and function with a possible fit. (SP.9-12.ID.6)

I can informally assess the fit of a function by analyzing residuals. (SP.9-12.ID.6)

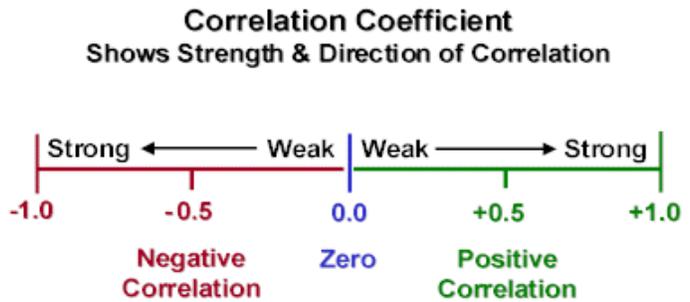
- I can fit a linear function for a scatter plot that suggests a linear association. (SP.9-12.ID.6)

**Keywords:** data, set, statistics, distribution, spread, standard deviation, real, box plot, histogram, dot plot, range, interquartile, scale, mean, median, outlier, residual, function, linear, quadratic, exponential

- I can analyze and interpret the meaning of slope (rate of change) of a linear model in context of the data. (SP.9-12.ID.5)

- I can analyze and interpret the meaning of the intercept (constant term) of a linear model in the context of the data. (SP.9-12.ID.5)

- I can define correlation coefficient and understand that it can only apply to a linear fit. (SP.9-12.ID.5)



- I can use technology to compute and interpret the correlation coefficient of a linear fit. (SP.9-12.ID.5)

- I can understand that correlation does not imply causation. (SP.9-12.ID.6)

- I can determine if two variables seem reasonably linked through correlation. (SP.9-12.ID.6)

- I can determine if two variables seem reasonably linked through causation. (SP.9-12.ID.6)

**Keywords:** data, set, statistics, distribution, spread, standard deviation, real, box plot, histogram, dot plot, range, interquartile, scale, mean, median, outlier, residual, function, linear, slope, correlation, coefficient, causation, intercept

- I can explain the concepts of inference, population parameter, and random sample. (SP.9-12.IC.1)

- I can understand how random samples are used to make inferences about population parameters. (SP.9-12. IC.1)

I can understand why random samples are used to make inferences about population parameters. (SP.9-12. IC.1)

I can decide if a probability model is consistent with results from a given data-generating process. (SP.9-12. IC.2)

I can compare two probability models to determine which is more consistent with results from a given data-generating process. (SP.9-12. IC.2)

Keywords: statistics, inference, population, parameter, random, sample, data, data-generating, simulation, probability, conclusion, model, experiment

I can describe the distinguishing features of sample surveys, experiments, and observational studies. (SP.9-12.IC.3)

I can explain the purposes of sample surveys, experiments, and observational studies, and decide where each data-gathering system is most appropriate. (SP.9-12. IC.3)

I can explain how randomization relates to sample surveys, experiments, and observational studies. (SP.9-12. IC.3)

$$\mu = \frac{\sum X}{N}$$

I can define population mean and population proportion. (SP.9-12. IC.3)

I can use data from a sample survey to estimate a population mean or proportion. (SP.9-12. IC.4)

I can conduct a simulation to gather a random sample mean or proportion and determine which results match the population mean or proportion and which results are extreme. (SP.9-12. IC.4)

I can develop a margin of error by comparing the random sample mean or proportion to the population mean or proportion. (SP.9-12. IC.4)

Keywords: statistics, inference, population, parameter, random, sample, data, data-generating, simulation, probability, conclusion, model, experiment, survey, observation, randomization, mean, proportion

- I can compare two treatment groups by determining the sample mean and standard deviation of each. (SP.9-12.IC.5)
- I can create simulations for two treatment groups to decide if differences between parameters such as mean and standard deviation are significant. (SP.9-12. IC.5)
- I can represent the finding of a simulation for two treatment groups in a histogram. (SP.9-12. IC.5)
- I can evaluate reports for accuracy and breadth of data. (SP.9-12. IC.6)
- I can determine if reports present quantitative or categorical data. (SP.9-12. IC.6)
- I can analyze reports for biased or skewed conclusions. (SP.9-12. IC.6)
- I can distinguish facts from opinions presented in reports. (SP.9-12. IC.6)

Keywords: statistics, inference, population, parameter, random, sample, data, data-generating, simulation, probability, conclusion, model, experiment, survey, observation, randomization, mean, proportion, accuracy, bias, quantitative, categorical, fact, opinion

- I can define event, sample space, union, intersection, and complements as related to probability. (SP.9-12. CP.1)
- I can describe events as subsets of a sample space (the set of outcomes) using characteristics or categories of the outcome. (SP.9-12. CP.1)

I can describe events as unions, intersections, or complements of other events (“or”, “and”, “not”). (SP.9-12. CP.1)

I can show why two events  $A$  and  $B$  are independent if the probability of  $A$  and  $B$  occurring together is the product of their probabilities with the equation  $P(A \text{ and } B) = P(A) \times P(B)$ . (SP.9-12. CP.2)

Combining probabilities: Summary

Marginal	Union	Joint	Conditional
$P(A)$ The probability of A occurring	$P(A \cup B)$ The probability of A or B occurring	$P(A \cap B)$ The probability of A and B occurring	$P(A B)$ The probability of A occurring given that B has occurred

Keywords: probability, events, subset, sample space, characteristic, outcome, union, intersection, complement, independent, characterization

- I can explain the conditional probability of  $A$  given  $B$  as  $P(A \text{ and } B)/P(B)$ , and illustrate this relationship using examples. (SP.9-12.CP.3)
- I can understand conditional probability and explain independence of  $A$  and  $B$  as saying that the conditional probability of  $A$  given  $B$  is the same as the probability of  $A$ , and the conditional probability of  $B$  given  $A$  is the same as the probability of  $B$ . (SP.9-12.CP.3)
- I can distinguish between events that are independent, and those that are not. (SP.9-12.IC.5)

### -Two-way Frequency tables

	Male	Female
Agree	12	31
Disagree	26	15
Total	38	46

I can construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. (SP.9-12. CP.4)

I can use a two-way frequency table to decide if events are independent and to approximate conditional probabilities. (SP.9-12. CP.4)

- I can collect data from a random sample to determine if events are independent. (SP.9-12. CP.4)
- I can explain the concepts of conditional probability and independence in everyday language and everyday situations. (SP.9-12. CP.5)

Keywords: probability, events, subset, sample space, characteristic, outcome, union, intersection, complement, independent, characterization, conditional, two-way, frequency

- I can define a random variable for a quantity of interest by assigning a numerical value to each event in a sample space. (SP.9-12. MD.1)
- I can calculate the expected value of a random variable. (SP.9-12. MD.2)

I can recognize a random variable as the mean of a probability distribution. (SP.9-12. MD.3)

I can create a probability distribution table for a random variable to define it for a sample space and calculate its theoretical values. (SP.9-12. MD.4)

I can create a probability distribution table for a random variable to define it for a sample space in which probabilities are assigned empirically and calculate its theoretical values. (SP.9-12. MD.4)

Keywords: probability, events, interest, distribution, random, variable, expected value, theoretical, empirical

I can weigh the possible outcomes of a decision by assigning probabilities to payoff values and finding expected values. (SP.9-12. MD.5)

I can create a probability distribution table for a game of chance by listing each possible outcome and assigning a probability to each based on the data. (SP.9-12. MD.5)

I can determine the expected payoff for a game of chance by executing the formula  $E(x) = \sum(x_i P_i)$ . (SP.9-12. MD.5)

Number of Orders per Week $x_i$	Probability $P_i$
41	.03
42	.10
43	.15
44	.17
45	.25
46	.15
47	.10
48	.05

I can determine expected values for multiple strategies and compare them to make an informed decision. (SP.9-12. MD.5)

I can use probabilities to make fair decisions. (SP.9-12. MD.6)

I can analyze decisions and strategies using probability concepts. (SP.9-12. MD.7)

Keywords: probability, events, interest, distribution, random, variable, expected value, real-world, application, payoff, risk, chance, strategy, concepts