

<b>Marking Period: 2</b>	<b>Unit Title: Introduction to Derivatives</b>	<b>Recommended Instruction Days: 10-15</b>
--------------------------	--	--

**Standard-New Jersey Student Learning Standards: F-IF**

**Strand:**  
**F-IF: Interpreting Functions**

**Understand the concept of a function and use function notation**

1. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If  $f$  is a function and  $x$  is an element of its domain, then  $f(x)$  denotes the output of  $f$  corresponding to the input  $x$ . The graph of  $f$  is the graph of the equation  $y = f(x)$ .
2. Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

**Interpret functions that arise in applications in terms of the context**

4. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship.
5. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.

**Analyze functions using different representations**

7. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
  - a. Graph linear and quadratic functions and show intercepts, maxima, and minima
  - b. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.
  - c. Graph polynomial functions, identifying zeros when suitable factorizations are available, and showing end behavior.
  - d. Graph rational functions, identifying zeros and asymptotes when suitable factorizations are available, and showing end behavior.
  - e. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing

LGBT and Disabilities Law: *N.J.S.A. 18A:35-4.35*

Jason Collins - First openly gay NBA player.

The mission is to ensure that every student is able to see themselves in our rich and diverse history.

<b>Social and Emotional Learning: <i>Competencies</i></b>	<b>Social and Emotional Learning: <i>Sub-Competencies</i></b>
<p>Self-Awareness</p> <p>Social Awareness</p> <p>Self-Management</p> <p>Relationship Skills</p> <p>Responsible Decision-Making</p>	<ul style="list-style-type: none"> <li>● Recognizing the importance of self-confidence in handling daily tasks and challenges.</li> <li>● Demonstrate an awareness of the expectations for social interactions in a variety of ways.</li> <li>● Demonstrate an understanding of the need for mutual respect when viewpoints differ.</li> <li>● Recognize the skills needed to establish and achieve personal and educational goals.</li> <li>● Utilize positive communication and social skills to interact effectively with others.</li> <li>● Develop, implement, and model effective problem solving and critical thinking skills.</li> </ul>

**Recommended Activities, Investigations,  
Interdisciplinary Connections, and/or Student  
Experiences to Explore NJSLs-CLKS within Unit**

<b>Essential Questions</b>	<b>Progress Indicators</b>	<b>Activity Description</b>
<ul style="list-style-type: none"> <li>● What is a derivative?</li> <li>● What is the difference between average rate of change and instantaneous rate of change?</li> <li>● How can we find derivatives and how</li> </ul>	<ul style="list-style-type: none"> <li>● Tests</li> <li>● Quizzes</li> <li>● Practice problems for homework</li> <li>● Worksheets</li> <li>● Leveled assessments</li> <li>● Projects</li> </ul>	<ul style="list-style-type: none"> <li>❖ Average vs. instantaneous rate of change</li> <li>❖ Secant lines</li> <li>❖ Estimating derivatives</li> <li>❖ Differentiability</li> <li>❖ Example Tasks Below</li> </ul> <p style="text-align: right;"><b><u>Interdisciplinary Connections:</u></b></p>

<p>do we represent derivatives?</p> <ul style="list-style-type: none"><li>• What is differentiability?</li></ul>		<p><b><u>Comprehensive Health and Physical Education Domain: Fitness and Physical Activity</u></b></p> <p>An individual's maximum heart rate (MHR) is the highest heart rate that can be sustained during prolonged exercise. An accurate formula for MHR is <math>M(t) = 192 - 0.007t^2</math>. A simpler model for MHR is <math>H(t) = 220 - t</math>.</p> <ol style="list-style-type: none"><li>Calculate the equation of the tangent line at <math>t = 20</math> for <math>H(t)</math>.</li><li>Calculate the equation of the tangent line at <math>t = 20</math> for <math>M(t)</math>.</li><li>Discuss briefly why, given your results, <math>M(t)</math> is a more realistic model for MHR than <math>H(t)</math>.</li></ol> <p><b>Answer</b></p> <ol style="list-style-type: none"><li><math>y = 220 - t</math></li><li><math>y = 194.8 - 0.28t</math></li><li><math>H(t)</math> predicts a constant decline of 1 bpm every year regardless of age. But a more realistic model would feature a progressively large decline in MHR as the individual ages. This is what the <math>M(t)</math> model predicts (its graph is a downward opening quadratic function whose tangent line slopes get more negative as <math>t</math> increases).</li></ol> <p><b>Task</b></p> <p>Let <math>d(t) = 16t</math> be the distance function. Find the average speed over time intervals</p> <ol style="list-style-type: none"><li><math>1 \leq t \leq 2</math></li><li><math>2 \leq t \leq 3</math></li></ol> <p><b>Answer</b></p> <ol style="list-style-type: none"><li>16</li><li>16</li></ol> <p><b>Task</b></p>
--	--	--

		<p>Suppose <math>y = 2x + 4</math> is the line tangent to the graph of some function <math>f(x)</math> at <math>x = 2</math>. Find <math>f'(2)</math> and <math>f(2)</math>.</p> <p><b>Answer</b> <math>f'(2) = 2</math> <math>f(2) = 8</math></p>
--	--	--

**Mathematical Practices**

- 1. Make sense of problems and persevere in solving them.**
- 2. Reason abstractly and quantitatively.**
- 3. Construct viable arguments and critique the reasoning of others.**
- 4. Model with mathematics.**
- 5. Use appropriate tools strategically.**
- 6. Attend to precision.**
- 7. Look for and make use of structure.**
- 8. Look for and express regularity in repeated reasoning.**

Assessments (Formative)

Assessments (Summative)

<b>To show evidence of meeting the standard/s, students will successfully engage within:</b>		<b>To show evidence of meeting the standard/s, students will successfully complete:</b>	
<p><b><u>Formative Assessment:</u></b></p> <ul style="list-style-type: none"> <li>● Entry and Exit Slips</li> <li>● Quizzes</li> <li>● Self Assessments</li> <li>● Focus Packets</li> </ul>		<p><b><u>Benchmarks:</u></b></p> <ul style="list-style-type: none"> <li>● Chapter Tests</li> <li>● Projects</li> </ul> <p><b><u>Summative Assessments:</u></b></p> <ul style="list-style-type: none"> <li>● District assessments</li> </ul>	
<b>Differentiated Student Access to Content: Teaching and Learning Resources/Materials</b>			
<b>Core Resources</b>	<b>Alternate Core Resources IEP/504/At-Risk/ESL</b>	<b>ELL Core Resources</b>	<b>Gifted &amp; Talented Core Resources</b>
<p>online albert resource online achievethecore resource online learnzillion resource online khanacademy resource online desmos resource online edulastic resource</p>	<p>Reteaching worksheets Skill building workbook Math manipulatives Leveled practice worksheets</p>	<p>Dictionary for native language Video tutorial in native language Success for English Learners worksheets Leveled Strategies for English Learners Linguistic Support</p>	<p>Enrichment worksheets Art of Problem Solving Leveled assessments</p>
<b>Supplemental Resources</b>			
<ul style="list-style-type: none"> <li>● Technology: Chromebooks, Graphing Calculators, Smartboards,</li> <li>● Other: Zoom and Google Meets, Schoology, Google Classroom</li> </ul>			

**Differentiated Student Access to Content:  
Recommended *Strategies & Techniques***

<b>Core Resources</b>	<b>Alternate Core Resources <i>IEP/504/At-Risk/ESL</i></b>	<b>ELL Core Resources</b>	<b>Gifted &amp; Talented Core Resources</b>
<p>Deliver instruction utilizing varied learning styles including audio, visual, and tactile/kinesthetic, provide individual instruction as needed, modify assessments and/or rubrics, repeat</p>	<p>Utilize a multi-sensory (VAKT) approach during instruction, provide alternate presentations of skills by varying the method (repetition, simple explanations, additional examples, modeling, etc.), modify test content and/or format, allow students to retake test for additional credit, provide additional times and preferential seating as needed, review, restate and repeat directions, provide study guides, and/or break assignments into segments of shorter tasks.</p>	<p>Extend time requirements, preferred seating, positive reinforcement, check often for understanding/review, oral/visual directions/prompts when necessary, supplemental materials including use of an online bilingual dictionary, and modified assessment and/or rubric.</p>	<p>Create an enhanced set of introductory activities, integrate active teaching/learning opportunities, incorporate authentic components, propose interest-based extension activities, and connect student to related</p>