# All Things Mathematics



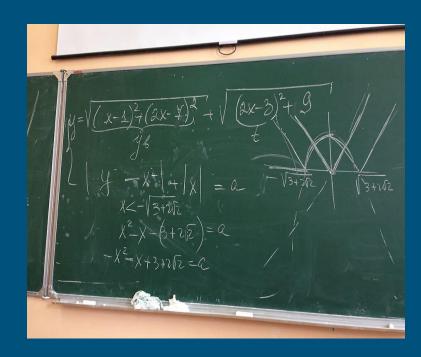
Effingham County Schools
August 2024

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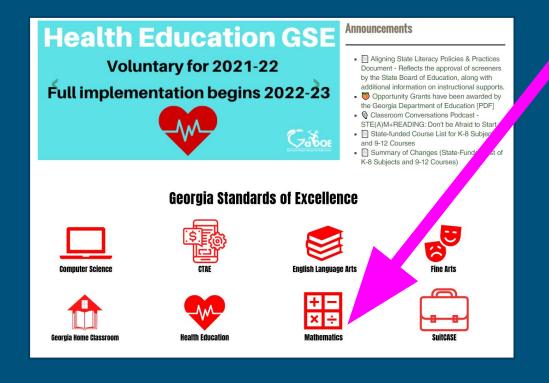
### Two Types of Standards

Georgia's K-12 Mathematics Standards are content standards, which tell us what teachers are charged with teaching.

The Standards of Mathematics Practices are what you want to see students doing in the mathematics classroom.



## GaDOE Mathematics Resources www.georgiastandards.org



## Standards Structure, K-12

#### Georgia's K-12 Mathematics Standards 7<sup>TH</sup> Grade

NUMERICAL REASONING - integers, percentages, fractions, decimal numbers

#### Big Idea

- includes summary of concepts for grade level

Learning objectives/ expectations - "breaks down" the standard in an instructional progression

any form (integers, percentages, fractions, and deci- Expectations			Standard							
7.NR.1.1	Show that a number and its opposite have a am of 0 (are additive inverses). Describe situations in which opposite quantities combine to make 0.	In the equation additive inverses	3 + -3 = 0, 3 and -3 are	Example  Your bank account balan \$25.00 into your account	<ul> <li>grade level/course key competency; represents what students should</li> </ul>					
7.NR.1.2	Show and explain p + q as the number located a distance  q  from p, in the positive or negative direction, depending on whether q is positive or negative. Interpret sums of rational numbers by describing applicable situations.	integers and oth presented within	be able to add and subtract er rational numbers r relevant, mathematical strategic thinking and a	6 + (-4) is 4 units to the l number line or 4 units do number line.		ultimately master				
7.NR.1.3	Represent addition and subtraction with rational numbers on a horizontal or a vertical number line diagram to solve authentic problems.	Strategies and Methods  Students should represent a variety of types of rational numbers on a number line diagram presented by horizontally and vertically.  Evidence of Student Learning  - instructional supports								
7.NR.1.4	Show and explain subtraction of rational numbers as adding the additive inverse, p – q = p + (–q). Show that the distance between two rational numbers on the number line is the absolute value of their difference and apply this principle in contextual situations.	<ul> <li>Examples</li> <li>Find the distance between a submarine submerged at a depth of 27 <sup>3</sup>/<sub>4</sub> feet below sea level and an airplane flying at an altitude of 1262 <sup>1</sup>/<sub>2</sub> feet above sea level.</li> <li>- <sup>1</sup>/<sub>2</sub> - (-2) is the same expression as - <sup>1</sup>/<sub>2</sub> + - (-2), which is 2 units to the right of - <sup>1</sup>/<sub>2</sub> on a horizontal number line or 2 units up from - <sup>1</sup>/<sub>2</sub> on a vertical number line.</li> </ul>								
7.NR.1.5	Apply properties of operations, including part-whole reasoning, as strategies to add and subtract rational numbers.	Fundamentals  Students should be allowed to explore the signs of integers and what they really mean to discover integer	Strategies and Methods  Students should be able to use the Commutative and Associative properties to combine more than two rational numbers flexibly.		Example  • (-8) + 5 + (-2) may be solved as (-8) + ( -2) + 5 to first make -10 by using the Commutative Property.					

#### GA DOE Mathematics Resources

https://www.georgiastandards.org/Georgia-Standards/Pages/Math.aspx

#### NEW! Mathematics Curriculum & Instruction Resources Now Available

- K-5
- 6-8
- 9-12

#### K-12 Instructional Support Resources

- Initial Implementation Year Transition Resource (all grade levels)
- Explanation of Changes and Improvements Georgia's K-12 Mathematics Standards
- K-12 Mathematics Glossary
- K-12 Mathematics Course Descriptions
- K-12 Mathematics Learning Progressions
- K-12 Mathematical Practices
- K-12 Mathematical Modeling Framework
- K-12 Framework for Statistical Reasoning
- Fostering Positive Mathematical Mindsets
- K-12 Mathematics Curriculum Maps
- K-12 Comprehensive Course Overviews
- Mathematics Support Guide for English Learners
- Guides for Effective Mathematics Instruction (K-12)
- Georgia Mathematics Strategies Toolkit to Address Learner Variability for Grades K-5
- Georgia Mathematics Strategies Toolkit to Address Learner Variability for Grades 6-8
- Georgia Mathematics Strategies Toolkit to Address Learner Variability for High School
- K-12 Mathematics Manipulatives and Materials List
- K-12 Mathematics Parent Letters

### GA DOE Mathematics Learning Progressions

				K-12 MA7	THEMATIC	S LEARNI	NG PROGE	RESSION	- GEORG	IA			
	ELEMENTARY SCHOOL (K-5)						MIDDLE SCHOOL (6-8)			HIGH SCHOOL (9-12)			
Key Concepts	к	1	2	3	4	5	6	7	8	Algebra: Concepts & Connections	Geometry: Concepts & Connections	Advanced Algebra: Concepts & Connections	Courses beyond Advanced Algebra
						NUMERICAL	REASONIN	IG					
Numbers	Whole numbers to 100	Whole numbers to 120     Partition shapes into halves and quarters/fourths (fourths) with no shading	Whole numbers to 1000     Partition shapes into halves, thirds and quarters (fourths) with no shading	Whole numbers to 10,000 Unit fractions with denominators of 2, 3, 4, 6, and 8 Represent fractions  Cajuivalence of simple fractions introduce shading to identify and compare fractional parts	Whole numbers to 100,000 Non-unit fractions with denominators of 2, 3, 4, 5, 6, 8, 10, 12, and 100 Fractions with like denominators Decimal fractions (tenths and hundredths)	Multi-digit whole numbers     Fractions with unlike denominators     Fractions greater than 1 Decimal fractions to thousandths	Rational numbers as a concept of the control o	All rational numbers     Simple probability	All rational numbers     Scientific notation     Numerical expressions with integer exponents     Approximate rational and irrational numbers (radicals) on a number line	All rational numbers     Operations with radicals	All numbers in The Real Number System	All numbers in The Real Number System     Complex numbers	Application of a numbers in the real number system     The Complex Number System (Precalculus and beyond)
Counting	Counting forward to 100     Counting backward from 20     Counting objects to 20	Counting forward and backward within 120     Skip counting by 2s, 5s, and 10s     Counting objects to 120	Counting forward and backward within 1000 Skip counting by 2s, 5s, 10s, 25s, and 100s Counting objects to 1000	Counting unit fractions	Counting non- unit fractions	Counting decimal numbers	Students should apply the foundational knowledge of counting to make sense of other mathematical ideas related to numbers in The Real Number System.			Students should apply the foundational knowledge of counting to make sense of other mathematical ideas related to numbers in The Real and Complex Number Systems.			
Place Value	Compose and decompose numbers within 20     Identify and write numerals to 20	Compose and decompose 2- digit numbers	Hundreds, tens and ones in 3- digit numbers	Round numbers to 1000 to nearest 10 or 100     Read & write multi-digit whole numbers to thousands	Magnitude of place value     Multi-digit whole numbers to 100,000     Round multi- digit whole numbers     Fractions with denominators of 10 or 100	Magnitude of place value extended to decimal numbers     Powers of 10 to 10 <sup>3</sup> Read & write decimal numbers to thousandths place     Round decimal numbers to hundredths place	Students should apply the foundational knowledge of place value to make sense of other mathematical ideas related to numbers in The Real Number System.			Systems.			
Comparisons	Comparing objects up to 10     Comparing numbers of objects in a set from 1-10	Comparing numbers to 100	Comparing numbers to 1,000	Comparing numbers to 10,000     Unit fractions	Multi-digit numbers     Fractions less than 1     Decimal fractions to hundredths place	Decimal fractions to thousandths place     Fractions greater than 1	Integers     Unit rates     Ratios     Numerical data distributions     Measures of variation     Absolute value     Display and analyze	Rational numbers     Probabilities     Random sampling	Rational and irrational numbers (radicals)     Compare proportional relationships presented in different ways	Rate of change (slope)     Intercept     Distributions of two or more data sets.		Recognize the purpose of and differences among different types of studies.     Population distributions, sample data distributions	Application of all numbers in the real number system     The Complex Number System (Precalculus and beyond)

https://www.ga doe.org/Curric ulum-Instructio n-and-Assess ment/Curriculu m-and-Instructi on/Documents/ Mathematics/G eorgia-K-12-M athematics-Sta ndards-Learnin g-Progressions .pdf

Should a should be should

## GaDOE Inspire

Log into Infinite Campus

Click SLDS

Click Ga Connects Preview

Click Inspire





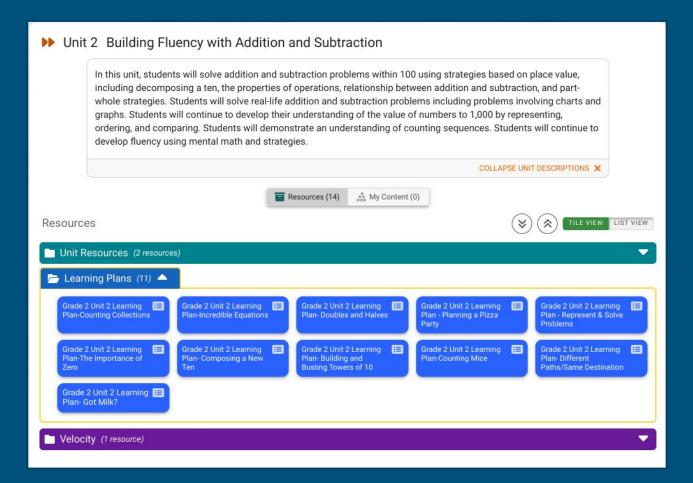
### GaDOE Inspire

- Courses
  - Standards
  - DOE Curriculum Maps and Pacing
  - Unit Overview
  - Interdisciplinary Connections
  - Instructional Learning Plans
  - Velocity (Interdisciplinary Activity)
- Resource Repository
  - Gifted Education
  - Cognitive Disabilities
  - Classroom Management
  - MTSS

- My Content Collections
  - To access Assessment Item Banks
  - Subscribe to a New Content Collection
  - o Enter Code
- Standards



Teacher
Guidance and
Student
Reproducibles



#### Unit 2 Building Fluency with Addition and Subtraction

In this unit, students will solve addition and subtraction problems within 100 using strategies based on place value, including decomposing a ten, the properties of operations, relationship between addition and subtraction, and part-whole strategies. Students will solve real-life addition and subtraction problems including problems involving charts and graphs. Students will continue to develop their understanding of the value of numbers to 1,000 by representing, ordering, and comparing. Students will demonstrate an understanding of counting sequences. Students will continue to develop fluency using mental math and strategies.

COLLAPSE UNIT DESCRIPTIONS X

You have not created or copied any resources for this unit.

## Effingham County School District (ECSD) Mathematics Resources

ECSD Pacing and Curriculum Maps for Mathematics

Google Drive Search Bar: Curriculum Guides and Pacing Dashboard

- Ga DOE Unit
- Standards within the units
- Days in unit
- Assessments to be given within each unit
- Expectations (Learning Targets) and Success Criteria
- Local and GaDOE resources



#### Standards of Mathematical Practice

dake sense of problems and persevere in solving Attend to precision 2. Reason abstractly and quantitatively

3. Construct viable arguments and critique the reasoning of others

Reasoning and explaining

4. Model with mathematics

5. Use appropriate tools strategically

Modeling and using tools

7. Look for and make use of structure.

8. Look for and express regularity in repeated reasoning.

Seeing structure and generalizing

## SMP 1. Make Sense of Problems and Persevere in Solving Them

When presented a mathematics problem, students should ask:

What does the problem mean?

How can I represent and solve the problem?

What is the most efficient way to solve the problem?

Does my thinking and strategy for solving this problem make sense? Does my answer make sense?

Is there another way to solve this problem?

Students should be given opportunities to struggle.

Mistakes should be embraced as part of the learning process.

#### SMP 6. Attend to Precision

#### Students should be

- using clear and precise language in their discussions and in their reasoning about mathematics.
- determining when it is appropriate to use estimation and when it is appropriate to give exact answers.
- determining appropriate units, draw pictures that represent problems and label parts of graphs correctly.
- articulating place value correctly and read numbers accurately.



A school is holding a carnival. The students determined ticket prices as shown in the picture.

Which ticket option is the best deal?

Which ticket option is the worst deal?

How would you suggest they change their prices?

## Would You Rather...

or



Win \$500 a week for life



Win \$1,000,000

## Work as a server at Restaurant A **OR**

Work as a server at Restaurant B?

The state of the s

#### **Restaurant A**

\$18 per hour No tipping allowed

(meals range from \$8 to \$25 each)

#### **Restaurant B**

\$10.50 per hour Tipping encouraged

(meals range from \$8 to \$25 each)

wouldvourathermath.com

#### What is a Number Talk

Classroom conversations and discussions around purposefully crafted computation problems

Designed to elicit specific strategies that focus on number relationships and number theory

A pivotal vehicle for developing **fluency:** flexibility, appropriate strategy, efficiency and accuracy

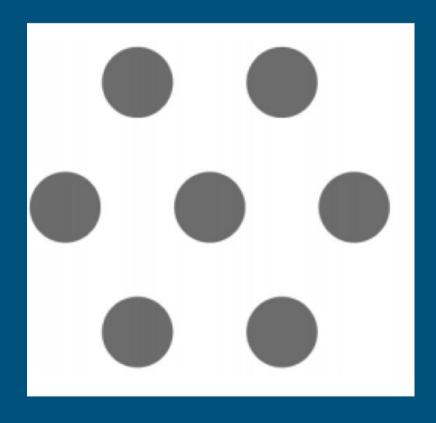
Problems are expected to be solved mentally while students share and defend solutions

Limited to 5-10 minutes of instructional time, 2-3 times a week

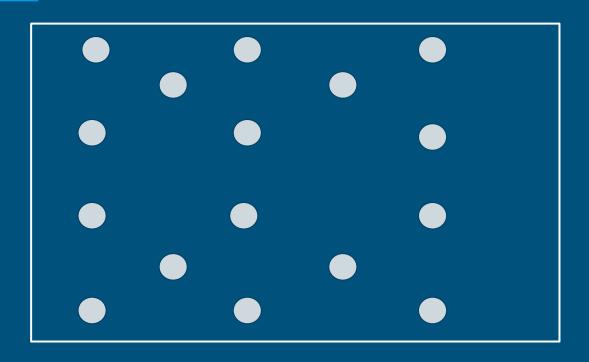
#### Number Talks

- Teacher presents a problem
- Teacher allows students time to think; students signal when they have an answer
- Teacher records students' answers for class to see
- Teacher asks individual students to share strategies used to derive their answers
- As students share strategies, teacher records on board for class to see
- Repeat with at least one more problem; ideally, this additional problem would allow students to use the same strategies

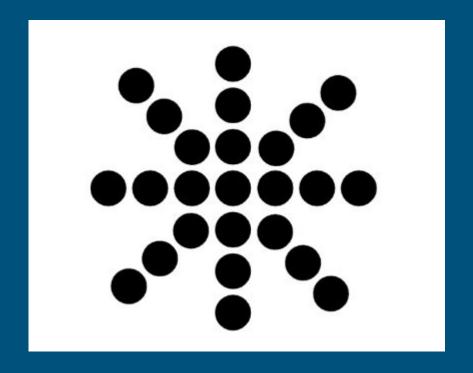
### How many dots in total?



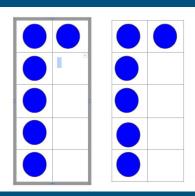
## How many dots in total?



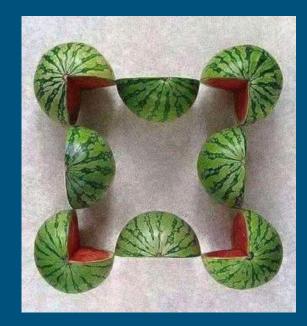
## How many dots in total?













2+6+8+3+4

5+7+8+3+5

19 + 17

24 + 49

85 + 98

Find the difference.

100 - 53

Find the difference.

120 - 44

Find the answer.

## 25 X 6

Find the answer.

351 ÷ 9

Find the quotient.

 $6 \div \frac{1}{3}$ 

Find the product.

<sup>3</sup>/<sub>4</sub> × 2

### Troubleshooting...

- Progress from easy problems to more difficult problems
- Assign problems that use similar strategies
- If students are having difficulty, allow them to talk with a partner and then share answers/strategies
- If students are not sharing a strategy that you intended, share the strategy with them disguised as "a student from another class" used this strategy
- Facilitate number talks in whole group and small groups (to allow participation of those who are hesitant to share)

#### Six Elements of an Effective Mathematics Lesson

The elements are Susan Halligan's synthesis of research in effective teaching practices by Hunter, Brophy, and others **applied specifically to mathematics instruction**. It includes the best practice findings of Marzano, Stiggins, Wormeli and others

Provides a template to increase attention to all necessary components of mathematics concept and skill acquisition

Builds a common language for collaboration

Framework, not a prescription

#### THE Six Elements

Instruction

Homework

Processing

Drill

**Application** 

Review/Preview



#### Instruction

## Processing

## Application

Teacher-Focused
Direct Instruction
Whole Group
Small Groups
I do-We do-You do (Gradual
Release Model)
Differentiated Instruction
Modeling
Teach in pieces
Teach - Practice - Teach Practice - Mixed Practice
Chunking of content
Check for understanding

Student-focused Independent or group assignment Use of manipulatives Time to make discoveries Students draw pictures to represent thinking Students explain their thinking to **Pairs** Small groups Whole class Be very intentional in assigning problems Results in understanding of standard algorithms

Student-Focused
Independent or group
assignment
Mathematical Modeling
Connections to real world
More than one way to solve
More than one correct answer

# What do you notice?

# **Traditional Problem:**

If you have 1,000 pretzels and the class eats 100 pretzels each day, how many days can the class eat pretzels.

# Modeling with Mathematics:

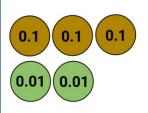
If a class has a bag of pretzels and they want it to last the whole week, how can we figure out how many pretzels to give each kid each day?

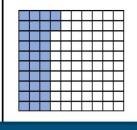
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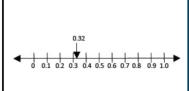
# Match the type of mathematics problem

Mario's family is planning a vacation. They would like to visit three places in Georgia. Plan an itinerary and a budget for the trip.

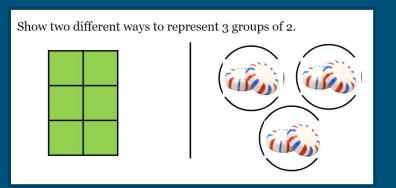
C. Represent 0.32 with place value disks and decimal grids. Locate 0.32 on a number line.







3 x 2 The second recess in school is at 1 o'clock in the afternoon, which is 2 hours after the first recess. When is the first recess?



Sheryl was organising buses for a school trip. She had 171 children, 22 teachers & 13 parents. A bus could take 20 passengers. How many buses would she need and how many spare seats would be left for extra luggage?

- Computation Problem
- Multiple Representations
- Word/Application Problem
- Mathematical Modeling Problem

#### Drill

Purpose is to increase speed of recalling facts

Basic facts that students need to immediately recall in order to be better mathematicians

Drill should be a maximum of 5 minutes daily

Can be choral, written or via technology and done individually or with groups of students

# Math Facts Checks (Grades 1-5)

#### Effingham County School District Math Facts Progress Check 2024-2025

Students in Grades 1-5 will take the Math Facts Progress Check three times a year. Testing windows are as follows:

Math Fact Check #1: October 21-25
Math Fact Check #2: February 3-7

Math Fact Check #3: May 2-16

Grade Level	Math Computation Information	# of Questions	Time Allotted	Goal
1	Addition and Subtraction: Single digit addends; sums and minuends to 10	60	4 minutes	By the last Math Facts Check, students will have met their goal if they have answered 90% or more of the questions correctly.  For Grades 1-2, 54 of 60 is 90%.  For Grades 3-5, 81 of 90 is 90%.
2	Addition and Subtraction: Single digit addends; sums and minuends to 18	60	4 minutes	
3	Multiplication: Single digit factors 0-9	90	4 minutes	
4	Multiplication: Single digit factors 0-9	90	3 minutes	
5	Division: Single digit factors 0-9; dividends through 81	90	3 minutes	

# Grade Level Goals for Each School

Grades 1-3: 70% of students meet the 90% goal!

Grades 4-5: 80% of students meet the 90% goal!

# Talk to a Neighbor



Consider the grade/course you teach, what mathematics topics could be included in Drill in addition to Math Facts?

#### Homework

Purpose is to keep learning warm so assignment should be **over firm learning only** 

Should be a very short assignment given at the last moment possible, otherwise assignment is "classwork to be completed at home"

Provide support for those at home - online chat/teacher videos/answer keys/before-after school help

Have a plan for those who did not complete the homework assignment

Consider positive grading

#### Review/Preview

Purpose is to maintain old learning in order to build foundations for new learning.

Emphasis on essentials (End of Grade/End of Course)

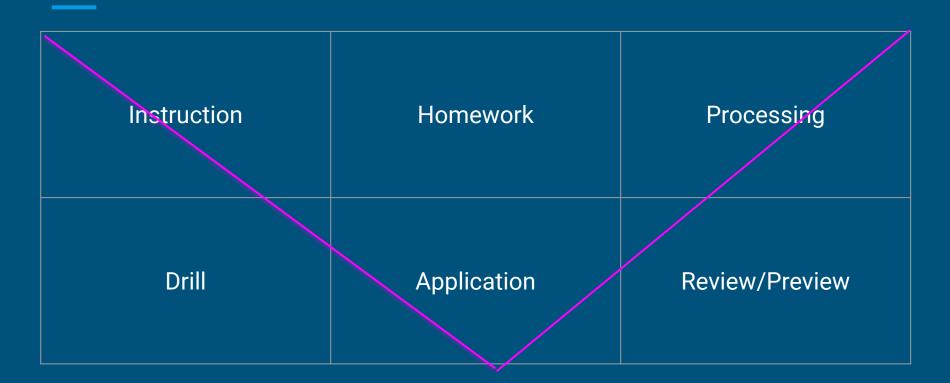
Student-focused

Spiral Reviews

Increase accuracy (not speed!!)

Daily (max 10 minutes)

#### Six Elements of an Effective Mathematics Lesson



#### Closure (Not one of the Six Elements, but important!)

Purpose is to reflect on day's learning

Review learning target and success criteria

Assess students progress towards meeting learning target

Will help with dismissal and transition to next class

Should be five minutes or less in length

#### Success Criteria?

Can you...

Locate and interpret Georgia's K-12 Mathematics Standards?

Access ECSD Mathematics resources?

Apply the Standards of Mathematical Practice?

Facilitate a Number Talk?

Plan and teach a lesson that includes the Six Elements?



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