

Adding And Subtracting Integers

Neg. + Neg. = MORE Negative

More Negative

More Positive

$$(-2) + (-5) = -7$$

$$-8 + 2 = -6$$

$$-4 + 7 = 3$$

Subtracting a Neg. → Change to Adding Pos.

$$-2 - (-5) = -2 + (+5) = +3$$

Evaluate the following:

1. $-1.3 + 1.0 =$ _____

8. $-7 + (-6) =$ _____

2. $-8 + 4 =$ _____

9. $-3 + (-12) =$ _____

3. $-1.1 + 2.2 =$ _____

10. $8 + (-16) =$ _____

4. $-2.7 + 4.5 =$ _____

11. $-16 - (-28) =$ _____

5. $-17 + 17 =$ _____

12. $-4 - 7 =$ _____

6. $-33 + 26 =$ _____

13. $-4.6 - (-3) =$ _____

7. $1.6 + (-1.5) =$ _____

14. $5 - 13 =$ _____

Multiplying and Dividing Rational Numbers

Multiplication:

- **Same Sign**- The product of two integers with the same sign is positive.
- **Different Signs**- The product of two integers with different signs is negative.

Division:

- **Same Sign**- The quotient of two integers with the same sign is positive.
- **Different Signs**- The quotient of two integers with different signs is negative.

<https://learnzillion.com/lessons/1776-compare-the-outcomes-of-fraction-multiplication-with-the-outcomes-of-decimal-multiplication>

Exercise 1

Find the product.

a. $3(-4) =$

b. $-7 \bullet 4 =$

c. $-5 \bullet -6 =$

Exercise 2

Find the quotient

a. $-36 \div (-6) =$

b. $-10 \div 5 =$

c. $\frac{-45}{5} =$

Mixed Practice

Evaluate the following:

1. $\frac{32}{-8} =$

2. $-12 \bullet (-5) =$

3. $-48 \div -6 =$

4. $-\frac{7}{10} \div \frac{2}{5} =$

5. $\frac{-18}{-2} =$

6. $\frac{-1}{4} \bullet \left(-\frac{4}{5}\right) =$

7. $-0.05 \bullet (-0.5) =$

8. $-10\frac{2}{7} \div \left(-4\frac{4}{11}\right) =$

9. $-2\frac{4}{5} \div (-7) =$

10. $-2(-3)(-9) =$

11. $\frac{-10}{-\frac{1}{4}} =$

12. $-0.4 \bullet -0.02 =$

Order of Operations

| | |
|---------------------------------|---|
| Parenthesis | $10 - (50 \div (-2 \bullet 25) + 7) \times 4$ |
| Exponents | $10 - (50 \div (-50) + 7) \times 4$ |
| (M)ultiplication or (D)ivision) | $10 - (-1+ 7) \times 4$ $10 - (6) \times 4$ $10 - 24$ |
| (A)ddition or (S)ubtraction) | -14 |

Simplify each of the following.

$1) (34 - 2^2) \div (11 - 6)$

$6) 2 \times (10 - 5) + 9^2$

$2) (9 - 3)^2 + (18 \div 3)$

$7) (72 - 6^2) \div (8 - 4)$

$3) (40 - 4) \div 3 + 2^2$

$8) (6 \times 3 + 5^2) - 7$

$4) (10 + 3)^2 + (12 \div 6)$

$9) (11 \times 9 + 3^2) + 6$

$5) 6 \times (12 + 5) + 2^2$

$10) (36 - 6) \div 6 - 2^2$

Combining Like Terms

Example 1 : <https://www.khanacademy.org/math/algebra-basics/core-algebra-expressions/core-algebra-manipulating-expressions/v/combining-like-terms-1>

Example 2: <http://www.mathsisfun.com/algebra/like-terms.htm>

Example: $3(5x + 11) + 8(7x + 3)$

$$15x + 33 + 56x + 24$$

$$15x + 56x + 33 + 24$$

$$71x + 57$$

Simplify the following expressions.

$$1. \quad 4m + 9m - 7 =$$

$$2. \quad -2x + 16 - 40x - 20 =$$

$$3. \quad 2z + 6 + 15 - 3z =$$

$$4. \quad -10x - 30x + 4 + 18 =$$

$$5. \quad 16x + 15 + 3x - 3 + 22x$$

$$6. \quad 20x + 15 - 25x =$$

$$7. \quad -20x + 15 + 16x - 35 =$$

$$8. \quad 12r + 5s - 7t + 11r + 9s - 4r =$$

$$9. \quad 8y - 18y - 7 =$$

$$10. \quad \frac{1}{4}x + 3 + \frac{1}{8}x - 6 =$$

$$11. \quad \frac{1}{5} + 3x - 10x + \frac{7}{10} =$$

$$12. \quad \frac{1}{7}b + 4 - 2 + \frac{5}{7}b =$$

Distributive Property

Useful links

- <https://learnzillion.com/lessons/3721-use-area-models-to-represent-the-distributive-property>
- <https://learnzillion.com/lessons/810>

Example: **3(2x – 5)**

Since in the order of operations, multiplication comes before addition and subtraction, we must get rid of the multiplication **before** you can combine like terms.

We do this by using the **distributive property**

Step 1: $3(2x - 5)$

Step 2: $3(2x) - 3(5)$

Step 3: $6x - 15$

Final answer: $6x - 15$

Simplify the following expressions

1. $2(x + 4)$

2. $3(5 - y)$

3. $-2(5 + 14p)$

4. $9(3x + 10)$

5. $8(-7t - 5)$

6. $-3(4f - 12)$

7. $-3(6v + 8) + 11$

8. $4(-1y - 10) + 80$

9. $-6(3c - 3) - 6$

10. $k + 3(5k - 0)$

11. $-(5 + 4w)$

12. $7 + q(6 - 2)$

13. $1 - (7n + 9)$

14. $2 - 3(y + 13)$

15. $\frac{1}{2}(9 + 4m)$

One Step Equations

Solve by doing the inverse operation. Addition and Subtraction are opposites.

Goal: ISOLATE THE VARIABLE

Solve each equation.

$$1) \ 26 = 8 + v$$

$$2) \ 3 + p = 8$$

$$3) \ 15 + b = 23$$

$$4) \ -15 + n = -9$$

$$5) \ m + 4 = -12$$

$$6) \ x - 7 = 13$$

$$7) \ m - 9 = -13$$

$$8) \ p - 6 = -5$$

$$9) \ v - 15 = -27$$

$$10) \ n + 16 = 9$$

Solving Multi- Step Equations

Go to the following site to watch a video to refresh your memory:

<https://www.khanacademy.org/math/algebra-basics/core-algebra-linear-equations-inequalities/core-algebra-solving-basic-equations/v/two-step-equations>

Solve the following equations for the given variable.

$$1. \ 2v + 7 = 3$$

$$2. \ 4b + 3 = -9$$

$$3. \ 17 = 5k - 2$$

$$4. \ -6t - 7 = 17$$

$$5. \ 8n + 16.2 = 1.6$$

$$6. \ -5g + 2.3 = -18.8$$

$$7. \ -18 - 6k = 6(1 + 3k)$$

$$8. \ 5n + 34 = -2(1 - 7n)$$

$$9. \ 2(4x - 3) - 8 = 4 + 2x$$

$$10. \ -3(4x + 3) + 4(6x + 1) = 43$$

Identifying terms in an equation

Example: $2x^2 + 5x - 4$

Terms: $2x^2$, $5x$, -4

Coefficients: 2, 5

Constant: -4

Variable: x

Define the following vocabulary words:

Term: _____

Constant: _____

Coefficient: _____

Variable: _____

1. Which of the following terms describes the 6 in the expression $8x^3 + 6x^2 - 3x + 4$

- A. Constant B. Coefficient C. Term D. Variable

2. Which of the following terms describes the 9 in the expression $-4x + 8y + 6z + 9$

- A. Constant B. Coefficient C. Term D. Variable

3. Circle each **term** in the equation. $5x^2 - 3 + 2x + 1$

4. Circle each **coefficient** in the equation. $4x + 1 - 2x + 7$

5. Circle each **constant** in the equation. $3x^2 + 10 + 7x - 6$

6. Circle each **variable** in the equation. $10x + 7 - 3x - 2$

Unit Rates

Example: 240 miles in 4 hours

$$240 \text{ miles} \div 4 \text{ hours} = 60 \text{ miles per hour}$$

OR

$$\frac{240 \text{ miles}}{4 \text{ hours}} = \frac{x \text{ miles}}{1 \text{ hour}}$$

Cross Multiply

To Solve

Basic skills: Unit Rates

Independent Practice 1

1. 5000 words in 10 pages
_____ words per page

2. 256 students in 8 buses
_____ in each bus

3. 35 Oranges in 7 bags
_____ oranges in each bag

4. 20 candies for 10 dollars
_____ dollars per candy

5. type 600 words in 20 minutes
_____ words per minute

6. 600 km in 10 hours
_____ km per hour

Fraction Review

Simplify fractions: $\frac{20}{60} = \frac{2}{6} = \frac{1}{3}$

1) $\frac{40}{56} = \underline{\quad}$

11) $\frac{7}{14} = \underline{\quad}$

21) $\frac{16}{18} = \underline{\quad}$

2) $\frac{2}{8} = \underline{\quad}$

12) $\frac{14}{70} = \underline{\quad}$

22) $\frac{16}{40} = \underline{\quad}$

3) $\frac{42}{56} = \underline{\quad}$

13) $\frac{6}{9} = \underline{\quad}$

23) $\frac{10}{90} = \underline{\quad}$



Multiply.

(1) $\frac{1}{3} \times 3\frac{1}{2} =$

(2) $\frac{2}{3} \times 3\frac{11}{13} =$

(3) $\frac{14}{15} \times 2\frac{1}{2} =$

(4) $\frac{5}{8} \times 1\frac{1}{5} =$

(5) $\frac{1}{2} \times 1\frac{1}{9} =$

(6) $2\frac{1}{4} \times \frac{1}{6} =$



Divide.

(1) $\frac{1}{3} \div \frac{8}{13} =$

(2) $\frac{1}{2} \div \frac{7}{9} =$

(3) $\frac{1}{3} \div \frac{7}{10} =$

(4) $\frac{1}{2} \div \frac{5}{6} =$

(5) $\frac{1}{2} \div \frac{11}{14} =$

(6) $\frac{1}{12} \div \frac{1}{2} =$