

Solving Multi-Step Equations

1. Clear parentheses using the distributive property.
2. Combine like terms within each side of the equal sign.
3. Add/subtract terms to both sides of the equation to get the terms with variables on one side and constant terms on the other side.
4. Isolate the variable by multiplying/dividing both sides of the equation by the number with the variable.

Ex: $3(2x - 5) - 3 = 2x + 8 + 6x$

$$6x - 15 - 3 = 2x + 8 + 6x$$
$$6x - 18 = 8x + 8$$
$$\cancel{6x} - 26 = 8x$$
$$-26 = \cancel{2x} + 8$$
$$-26 = 2x + 8$$
$$-26 - 8 = 2x + 8 - 8$$
$$-34 = 2x$$
$$-17 = x \rightarrow \boxed{x = -17}$$

Solving Absolute Value Equations

1. Isolate the absolute value.
2. Break the absolute value equation into two separate equations. For the first equation, set the expression inside the absolute value notation equal to the opposite side of the equation. For the second equation, make the number on the opposite side negative.
3. Solve each equation.

Ex: $-3|3x+2| - 2 = -8$

$$-3|3x+2| - 2 = -8$$
$$\cancel{-3|3x+2|} - 2 = -8$$
$$\cancel{-3|3x+2|} = -6$$
$$|3x+2| = 2$$
$$3x + 2 = 2 \quad 3x + 2 = -2$$
$$3x = 0 \quad 3x = -4$$
$$x = 0 \quad x = -\frac{4}{3}$$
$$\boxed{x = \{0, -\frac{4}{3}\}}$$

Solving Word Problems Algebraically

1. Define a variable.
2. Write an equation.
3. Solve the equation.
4. Label your answer with the appropriate units.

Ex: Bobby is 4 years younger than twice Jimmy's age. If Bobby is 26 years old, how old is Jimmy?

Let j = Jimmy's age

$$2j - 4 = 26$$

$$j = 15$$

→ Jimmy is 15 years old

Solve each equation.

1. $-3x - 9 = -27$	2. $25 + 2(n + 2) = 30$	3. $-9b - 6 = -3b + 48$
4. $5 - (m - 4) = 2m + 3(m - 1)$	5. $-24 - 10k = -8(k + 4) - 2k$	6. $f - (-19) = 11f + 23 - 20f$
7. $\frac{3}{4}d - \frac{1}{2} = \frac{3}{8} + \frac{1}{2}d$	8. $-0.5g + 13 = 3g$	9. $-5(h + 12) - (4h - 2) = h - 8$
10. $ 3x + 4 = 16$	11. $3 x - 5 = 27$	12. $-8 2x - 6 + 4 = -60$

Solve each word problem algebraically.

13. The sum of two consecutive integers is one less than three times the smaller integer. Find the two integers.	14. The length of a rectangular picture is 5 inches more than three times the width. Find the dimensions of the picture if its perimeter is 74 inches.
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Solving & Graphing Inequalities

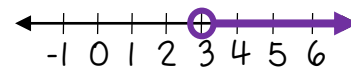
1. Solve the inequality as if it is an equation.
2. If you multiply or divide both sides of the inequality by a negative number, flip the inequality sign.
3. Write your answer with the variable on the left of the inequality sign.
4. Graph the solution on a number line. Make an open circle on the number if the number is not included in the solution ($<$ or $>$) and make a closed circle if the number is included (\leq or \geq). Shade to the left for less than ($<$ or \leq) and shade to the right for greater than ($>$ or \geq).

Ex: $-24 > 3x - 6 - 9x$

$$\begin{array}{r} -24 > -6x - 6 \\ +6 \quad \quad +6 \end{array}$$

$$\begin{array}{r} -18 > -6x \\ -6 \quad -6 \end{array}$$

$$3 < x \rightarrow \boxed{x > 3}$$



Compound Inequalities

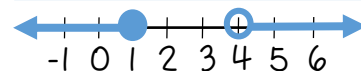
"Or" Inequalities

1. Solve each inequality separately and graph the solution to each on one number line.

Ex: $x + 2 > 6$ or $-2x \geq -2$

$$\begin{array}{r} x + 2 > 6 \\ -2 \quad -2 \end{array} \quad \text{or} \quad \begin{array}{r} -2x \geq -2 \\ -2 \quad -2 \end{array}$$

$$\boxed{x > 4} \quad \text{or} \quad \boxed{x \leq 1}$$



"And" Inequalities:

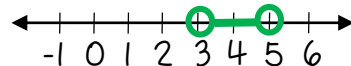
1. Isolate the variable, making sure to do the same thing to all 3 parts of the inequality.
2. Graph the solution to each part of the compound inequality and see where those graphs overlap. The overlapping part is the solution.

Ex: $3 < 2x - 3 < 7$

$$\begin{array}{r} 3 < 2x - 3 < 7 \\ +3 \quad \quad +3 \end{array}$$

$$\begin{array}{r} 6 < 2x < 10 \\ 2 \quad 2 \end{array}$$

$$\boxed{3 < x < 5}$$



Absolute Value Inequalities

1. Isolate the absolute value.
2. Change the absolute value inequality into a compound inequality. For $>$ or \geq , turn it into an "or" inequality. For $<$ or \leq , turn it into an "and" inequality. For the first inequality, keep everything the same, except eliminate the absolute value symbols. For the second inequality, make the number on the opposite side negative and flip the inequality sign.
3. Solve and graph the compound inequality.

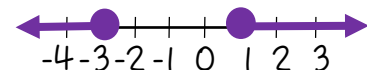
Ex: $|x + 1| - 3 \geq -1$

$$\begin{array}{r} |x + 1| - 3 \geq -1 \\ +3 \quad \quad +3 \end{array}$$

$$|x + 1| \geq 2$$

$$\begin{array}{r} x + 1 \geq 2 \quad \text{or} \quad x + 1 \leq -2 \\ -1 \quad -1 \quad \quad -1 \quad -1 \end{array}$$

$$\boxed{x \geq 1} \quad \text{or} \quad \boxed{x \leq -3}$$



Solve each inequality. Graph the solution on a number line.

15. $-6x + 3 > -39$

16. $25 - 3(n - 2) \geq -8n + 6$

17. $8g - 6(g + 1) < 4(2g - 9)$

18. $7k + 1 \leq 8$ or $-7 < k - 10$

19. $-4 < 3b + 2 \leq 20$

20. $9 < -3m < 24$

21. $y + (-6) \geq -13$ or $-3y + 8 > -7$

22. $|2x + 5| < 13$

23. $7|w - 6| \geq 21$

24. $-2|3m| + 3 < -51$

Finding Slope from 2 Points

Slope Formula: $m = \frac{y_2 - y_1}{x_2 - x_1}$

Ex: Find the slope of the line that passes through the points $(-9, -3)$ and $(7, -7)$

Special Cases:

$\frac{0}{\#} \rightarrow$ slope = 0

$\frac{\#}{0} \rightarrow$ slope is undefined

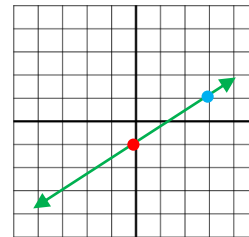
$$m = \frac{-7 - (-3)}{7 - (-9)} = \frac{-4}{16} = \boxed{-\frac{1}{4}}$$

Slope-Intercept Form

$$y = mx + b$$

$m =$ slope & $b =$ y-intercept

Ex: Graph $y = \frac{2}{3}x - 1$



y-intercept is -1
slope = $\frac{2}{3}$, (so from the y-intercept go up 2 & right 3)

Graphing from Slope-Intercept Form:

1. Make a point at the y-intercept.
2. Use the slope ($\frac{\text{rise}}{\text{run}}$) to make more points.
3. Connect the points to form a line.

Standard Form

$$Ax + By = C$$

$A, B,$ & C are integers & A is not negative

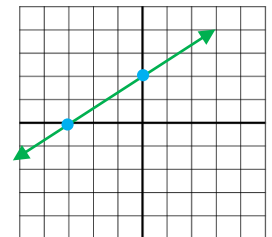
Ex: Graph $2x - 3y = -6$

Graphing Using Intercepts:

1. Find the x-intercept by substituting 0 for y .
2. Find the y-intercept by substituting 0 for x .
3. Make a point at each intercept and then connect the points to form a line.

x-intercept: $2x - 3(0) = -6$
 $2x = -6 \rightarrow x = -3$
 $(-3, 0)$

y-intercept: $2(0) - 3y = -6$
 $-3y = -6 \rightarrow y = 2$
 $(0, 2)$



Point-Slope Form

$$y - y_1 = m(x - x_1)$$

$m =$ slope & (x_1, y_1) is a point on the graph

Ex: Write the equation of the line passing through the points $(-1, 2)$ and $(3, 4)$ in point-slope form. Then convert it to slope-intercept and standard form.

$$m = \frac{4 - 2}{3 - (-1)} = \frac{2}{4} = \frac{1}{2}$$

Point-Slope Form: $y - 2 = \frac{1}{2}(x + 1)$

Converting Point-Slope Form to Slope-Intercept Form:

1. Distribute m .
2. Move y_1 to the other side of the equation.

Convert to Slope-Intercept Form:

$$\rightarrow y - 2 = \frac{1}{2}x + \frac{1}{2} \rightarrow y = \frac{1}{2}x + \frac{5}{2}$$

Converting Slope-Intercept Form to Standard Form:

1. Bring the x term to the left.
2. If there are fractions in the equation, multiply everything through by the least common denominator.
3. If A is negative, multiply everything through by -1 .

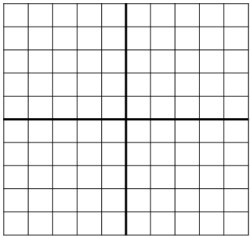
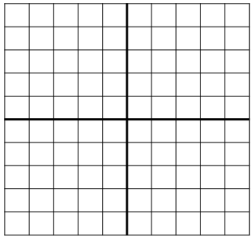
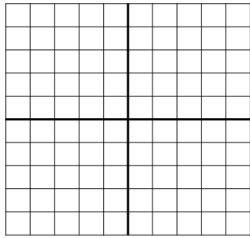
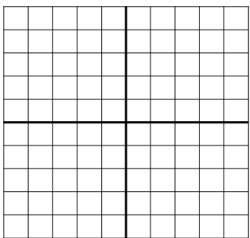
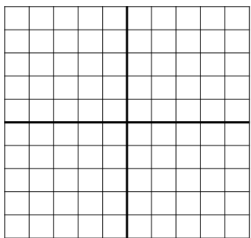
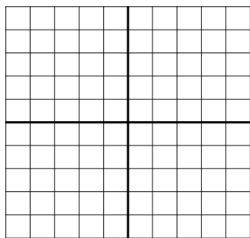
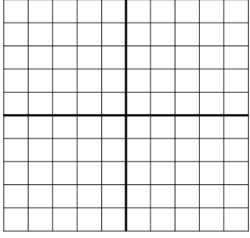
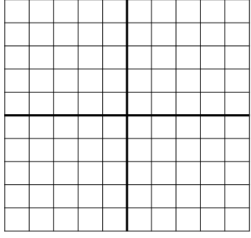
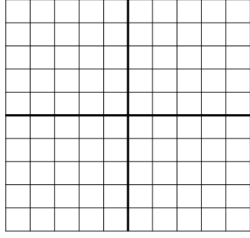
Convert to Standard Form:

$$\rightarrow -2\left(-\frac{1}{2}x + y = \frac{5}{2}\right) \rightarrow x - 2y = -5$$

Find the slope of the line that passes through the pair of points.

25. $(9, -3)$ and $(9, -8)$	26. $(-8, 5)$ and $(3, -6)$	27. $(7, -1)$ and $(15, 9)$
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Graph each line.

<p>28. $y = -\frac{3}{2}x + 2$</p> 	<p>29. $y = x - 3$</p> 	<p>30. $y = \frac{1}{3}x + 5$</p> 
<p>31. $2x - y = -2$</p> 	<p>32. $x + y = 4$</p> 	<p>33. $3x + 4y = -12$</p> 
<p>34. $y + 3 = \frac{1}{2}(x + 2)$</p> 	<p>35. $y - 1 = \frac{2}{3}(x - 3)$</p> 	<p>36. $y - 2 = 0$</p> 

Write the equation of the line in point-slope, slope-intercept, and standard form.

37. Line passing through point $(3, 5)$ with a slope of 1	38. Line passing through points $(-4, 2)$ and $(0, 3)$	39. Line passing through points $(1, 3)$ and $(2, 5)$
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Parallel & Perpendicular Lines

Parallel Lines have the *same slope* but different y-intercepts.

Perpendicular Lines have *opposite reciprocal slopes*.

Writing Equations of Parallel Lines:

1. Find the slope of the original line by first converting it to slope-intercept form if it is in Standard Form. The slope of the line parallel will have that same slope.
2. Use the given point along with the slope you just found to write the equation of the line in point-slope form.
3. Convert the point-slope form equation to slope-intercept form.

Ex: Write the equation of the line that is parallel to the line $y = 3x - 5$ and passes through the point $(-2, 4)$.

$$y = 3x - 5$$

$m = 3$, so slope of parallel line is **3**, too

$$\rightarrow y - 4 = 3(x + 2)$$

$$\rightarrow y - 4 = 3x + 6$$

$$\rightarrow \boxed{y = 3x + 10}$$

Ex: Write the equation of the line that is perpendicular to the line $x - 3y = -6$ and passes through the point $(-1, 1)$.

$$x - 3y = -6 \rightarrow -3y = -x - 6$$

$$\rightarrow y = \frac{1}{3}x + 2$$

$m = \frac{1}{3}$, so slope of perpendicular line is **-3**

$$\rightarrow y - 1 = -3(x + 1)$$

$$\rightarrow y - 1 = -3x - 3$$

$$\rightarrow \boxed{y = -3x - 2}$$

Writing Equations of Perpendicular Lines:

1. Find the slope of the original line. The slope of the line perpendicular will have the opposite (negative) reciprocal slope.
2. Use the given point along with the slope you just found to write the equation of the line in point-slope form.
3. Convert the point-slope form equation to slope-intercept form.

Linear Inequalities

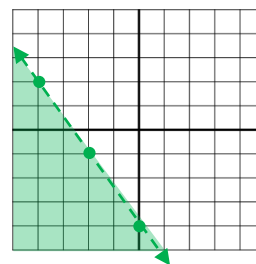
1. Convert the linear inequality in slope-intercept form. Be sure the y is on the left and remember to flip the inequality sign if you multiply or divide by a negative.
2. Graph the line as if it is an equation, except use a dotted line if the inequality sign is $<$ or $>$. If the sign is \leq or \geq , use a regular solid line.
3. Shade above the line for a "greater than" inequality ($>$ or \geq). Shade below the line for a "less than" inequality ($<$ or \leq). (For vertical lines, shade to the right for greater than and to the left for less than).

Ex: $-3x - 2y > 8$

$$\begin{array}{r} -3x - 2y > 8 \\ +3x \qquad +3x \end{array}$$

$$\frac{-2y}{-2} > \frac{3x + 8}{-2}$$

$$y < -\frac{3}{2}x - 4$$



Determine whether the lines are parallel, perpendicular, or neither. Justify your answer.

40. $y = 2x - 8$
 $y = \frac{1}{2}x + 6$

41. $y = x$
 $x + y = -2$

42. $3x + 2y = 18$
 $y + 4 = -\frac{3}{2}(x - 4)$

Write the equation of the line parallel to the given line that passes through the given point in slope-intercept form.

43. $y = -4x - 2$; $(0, -1)$

44. $2x - y = -4$; $(2, 5)$

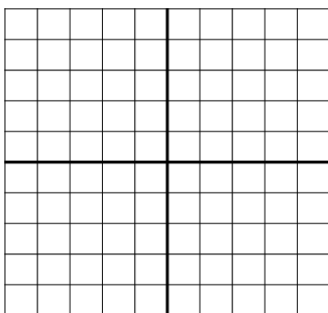
Write the equation of the line perpendicular to the given line that passes through the given point in slope-intercept form.

45. $y = \frac{2}{3}x - 9$; $(-6, -2)$

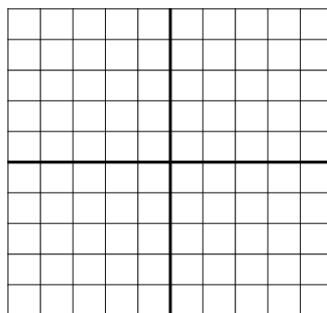
46. $4x + y = -6$; $(4, 5)$

Graph the solution to each linear inequality.

47. $y \leq -4x - 3$



48. $2x - y < 1$



49. $x + 3y > 3$

