

1. $5a^2 - 15$

2. $2y + 6xy$

3. $36xy^2 - 48x^2y$

4. $75b^2c^3 + 60bc^6$

5. $81r + 48rs$

6. $10q - 25q^2$

7. $82e^3 - 122ef$

8. $6z^4 - 18z^3$

9. $l^2 - 9l$

10. $20p^2 - 16p^2q^2$

11. $9c^4d^3 - 6c^2d^4$

12. $6e^3f - 11ef$

13. $34x^4y^3 - 17x^2y^5$

14. $35m^3n + 105m^2n^3$

15. $x^2 + 7x + 12$

16. $x^2 - 13x + 40$

17. $a^2 + 11ab + 18b^2$

18. $y^2 - 7xy - 18x^2$

19. $m^2 - mn - 90n^2$

20. $c^2 - 19cd + 34d^2$

Hint: On these, you'll have to factor twice to completely factor.

21. $2x^2 + 4x - 96$

22. $-x^2 - 12x - 36$

23. $3x^3 - 69x^2 + 180x$

24. $-5x^8 - 40x^7 - 60x^6$

25. $4x^2y + 8xy - 96y^2$

26. $-x^2 + 23xy + 50y^2$

Tip: Now use ac method or difference of squares. Always look for a GCF first!

27. $2x^2 + x - 6$

28. $4g^2 - 81h^2$

29. $3x^2 - 2x - 1$

30. $8n^2 - 72p^2$

31. $16c^4 - 81$

32. $5x^2 - 24x + 27$

33. $3a^2 + 11ab + 10b^2$

34. $25v^5x - 9v^3x$

35. $10x^3 - 25x^2 + 10x$

36. $-6x^2y - 8xy - 2y$

37. $9t^6m^4 - 196t^8m^4$

38. $3e^2 + 5ef - 12f^2$

39. $75x^2 - 147y^2$

40. $-15x^2 - 14x + 8$

Solve these polynomial equations by completely factoring.

41. $6x^2 + 21x = 0$ 42. $9x^2 - 5x = 8x^2 + 3x$ 43. $9x^2 - 25 = 0$ 44. $x^2 + 4x - 60 = 0$

45. $7x^2 + 3 = 3x^2 + 39$

46. $x^2 + 4x + 5 = 23 - 3x$

47. $x^2 + 6x + 3 = 8x + 2$

48. $3x(2x - 7) + 14(2x - 7) = 0$

49. $25x^2 + 30 = 60x - 6$

50. $(x + 6)(x - 3) = 5x + 30$

51. $6x^2 + 75x + 11 = 20 + 4x - 2x^2$

Worksheet: Simplify square roots & imaginary numbers

Simplify each expression. Use perfect square factors to help you. No decimals!

1. $\sqrt{76}$

2. $\sqrt{90}$

3. $\sqrt{48}$

4. $2\sqrt{75}$

5. $-5\sqrt{576}$

6. $\frac{4\sqrt{45}}{3}$

7. $-\frac{\sqrt{72}}{18}$

8. $\sqrt{3} \cdot \sqrt{12}$

9. $\frac{\sqrt{128}}{\sqrt{2}}$

10. $5\sqrt{42} \cdot 2\sqrt{3}$

11. $\frac{4\sqrt{294}}{\sqrt{3}}$

12. $\frac{\sqrt{90}}{\sqrt{40}}$

13. $\frac{6}{\sqrt{5}}$

14. $\sqrt{\frac{1}{7}}$

15. $\frac{\sqrt{13}}{4\sqrt{6}}$

16. $\frac{\sqrt{5}}{\sqrt{12}}$

17. $\frac{-3\sqrt{15}}{\sqrt{3}}$

18. $\frac{\sqrt{375}}{\sqrt{100}}$

19. $\sqrt{\frac{5}{2}}$

20. $\frac{2\sqrt{243}}{3\sqrt{200}}$

Simplify the following complex numbers.

21. $\sqrt{-196}$

22. $\sqrt{-15}$

23. $\sqrt{-52}$

24. $\sqrt{\frac{-1}{3}}$

25. $\sqrt{\frac{-5}{121}}$

26. $2\sqrt{3} \cdot 5\sqrt{-3}$

27. $-11i(8i)$

28. $10\sqrt{-9} \cdot 2\sqrt{-7}$

29. $\frac{1}{\sqrt{-4}}$

30. $\frac{10}{5i}$

31. $\frac{8 \pm \sqrt{-36}}{4}$

32. $\frac{-7 \pm \sqrt{-42}}{14}$

33. $\frac{15 \pm \sqrt{-2}}{5}$

34. $\frac{-10 \pm \sqrt{-27}}{21}$

35. $\frac{28 \pm \sqrt{-320}}{12}$

Worksheet: More on Complex Numbers and Solve Quadratic Equations
by taking square roots & with the quadratic formula

Simplify the following complex numbers.

1. $10(-8-2i) - 4(-9+i)$

2. $(3-5i)(9+11i)$

3. $(2+5\sqrt{7}i)^2$

4. $\frac{5}{1-\sqrt{-9}}$

5. $\frac{6i}{2+4i}$

Solve the following equations by taking square roots. Use fractions and radicals in your answers. No decimals.

6. $x^2 = 144$

7. $x^2 - 8 = 0$

8. $x^2 + 12 = 0$

9. $3x^2 = 30$

10. $x^2 + 18 = 30$

11. $2x^2 + 5 = 37$

12. $5x^2 + 13 = 14$

13. $3x^2 - 12 = -20$

14. $(x-7)^2 = 81$

15. $(x+6)^2 = 3$

16. $3(x-4)^2 - 7 = 68$

17. $\frac{1}{4}(x+1)^2 + 5 = 7$

$$18. 2(x-1)^2 - 11 = -8 \quad 19. \frac{1}{3}(x+4)^2 + 21 = 17 \quad 20. 3\left(\frac{1}{2}x - 4\right)^2 - 17 = 58$$

Solve the following equations with the quadratic formula.

$$21. 2x^2 - 6x - 5 = 0$$

$$22. 30x^2 - 24x + 40 = 10x^2 + 36x - 1$$

$$23. 18x^2 - 96x + 129 = 0$$

$$24. 10x^2 - 20 = x^2 + 30x - 45$$

25. $x^2 + 2x - 1 = -6x - 20$

26. $\frac{-2}{9}x^2 + 4x = 1$

27. A cannon ball is fired from a platform 10 feet above the ground with an initial velocity of 40 ft/sec. The equation that gives the height of the ball t seconds after it is fired is $h = -16t^2 + 40t + 10$. When will the ball hit the ground? Round your answer to 2 decimal places.

Worksheet: Solve Quadratic Equations by
completing the square & quadratic formula

Square each binomial to get a perfect square trinomial.

$(px + q)^2$	$ax^2 + bx + c$	$(px + q)^2$	$ax^2 + bx + c$	$(px + q)^2$	$ax^2 + bx + c$
$(x + 9)^2$		$(x - 15)^2$		$(5x + 2)^2$	
$(x - 11)^2$		$(2x + 7)^2$		$(8x - 3)^2$	
$(x + 6)^2$		$(3x - 1)^2$		$5(x + 4)^2$	

Rewrite each perfect square trinomial as the square of a binomial.

$ax^2 + bx + c$	$(px + q)^2$	$ax^2 + bx + c$	$(px + q)^2$	$ax^2 + bx + c$	$(px + q)^2$
$x^2 + 4x + 4$		$x^2 - 26x + 169$		$4x^2 + 12x + 9$	
$x^2 - 10x + 25$		$x^2 + 6x + 9$		$9x^2 - 6x + 1$	
$x^2 + 14x + 49$		$x^2 - 2x + 1$		$64x^2 + 80x + 25$	

Complete the square by adding a number in the first blank to form a perfect square trinomial. Finish by writing it as a squared binomial.

- $x^2 + 16x + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$
- $x^2 - 20x + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$
- $x^2 - 12x + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$
- $x^2 + 50x + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$
- $x^2 + 3x + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$
- $x^2 - 5x + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$
- $x^2 - 11x + \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$
- $2(x^2 + 6x + \underline{\hspace{1cm}}) = \underline{\hspace{1cm}}$
- $3(x^2 - 14x + \underline{\hspace{1cm}}) = \underline{\hspace{1cm}}$
- $-(x^2 + 24x + \underline{\hspace{1cm}}) = \underline{\hspace{1cm}}$

Solve the equations by completing the square.

- $x^2 - 14x = -45$
- $x^2 + 6x = 2$
- $x^2 - 10x - 2 = 0$

$$14. 4x^2 + 8x = -1$$

$$15. 3x^2 - 10x + 129 = 2x^2 + 12x$$

$$16. 3x^2 + 50x + 140 = 8x - 6$$

$$17. 8x^2 - 4x + 17 = 7x^2 + 4$$

$$18. -x^2 - 12x = 31$$

$$19. \frac{1}{4}x^2 + 2x = -2$$

$$20. 2x^2 - 12x + 13 = 1$$

$$21. 3x^2 + 24x + 52 = 1$$

$$22. 12x^2 + 3x = 11x^2 - 4x - 6$$

Solve with the quadratic formula.

$$23. 2x^2 + 18x = 3x^2 + 8x + 17$$

$$24. 600x^2 - 240x = 24x^2 - 25$$

25. $\frac{1}{4}x^2 + \frac{1}{4}x + \frac{13}{8} = 0$

26. $28x^2 - 19x - 11 = 4x^2 + 19x$

27. Suppose you stand at the top of the bleachers 64 feet high and toss an egg upward at a rate of 20 ft/sec. The equation which models the height of the egg after t seconds has passed is $h = -16t^2 + 20t + 64$. When will the egg splat on the ground? Round your answer to 2 decimal places.

Directions: Do work on your own notebook paper and/or graph paper.

Find the vertex of the parabola. Then build a 3-point t-chart. Plot 5 points on the parabola using symmetry. Sketch the parabola. Remember to shade the inequalities.

1. $y = -x^2 + 9$

2. $y = x^2 - 2x + 1$

3. $y > -x^2 - 2x + 8$

4. $y \geq 3x^2 + 6x - 2$

5. $y < -2x^2 + 20x - 49$

6. $y = 2x^2 - 2x + 3$

Find the vertex of the parabola. Name the a-value. Use the vertex and a-value to sketch the parabola. Remember to shade the inequalities.

7. $y \leq -x^2 + 6x - 9$

8. $y = 2x^2 + 12x + 19$

9. $y = -3x^2 + 6x + 3$

10. $y < \frac{1}{2}x^2 - 5$

11. $y = -\frac{1}{3}x^2 + 4x - 9$

12. $y > \frac{1}{5}x^2 - 4x + 20$

Word problems!

13. A golfer attempts to hit a ball out of a 2-foot-deep sand trap at a rate of 30 ft/sec. What is the maximum height the ball reaches?
14. A football player kicked a 41-yard punt. The path of the ball was modeled by the equation $y = -0.035x^2 + 1.4x + 1$, where x represents the ball's horizontal distance from the football player and y represents the ball's vertical distance above the ground, both x and y measured in yards.
- What is the maximum height of the ball?
 - The player kicked the football toward midfield from the 18-yard line. Over which yard line was the ball when it was at its max height?
15. From 1980 through 1995, the annual sales, S (in thousands of dollars), of a photography studio can be modeled by $S = \frac{-1}{8}t^2 + 3t + 42$, where $t = 0$ represents 1980. During what year were annual sales maximized?
16. You are running a little business selling appliques for water bottles. Your cost, C , to produce x appliques is given by the equation $C = 2.5x^2 - 625x + 39214$. How many appliques should you produce to minimize your cost? What is the minimum cost?

Directions: Do work on your own notebook paper and/or graph paper.

Name the vertex of the parabola. Then build a 3-point t-chart. Plot 5 points on the parabola using symmetry. Sketch the parabola. Remember to shade the inequalities.

1. $y = 2x^2 + 1$ 2. $y = (x - 4)^2 - 1$ 3. $y > -(x + 2)^2 + 8$
 4. $y \geq 3(x + 1)^2 - 2$ 5. $y < -2(x - 7)^2$ 6. $y = \frac{1}{3}(x - 6)^2 - 2$

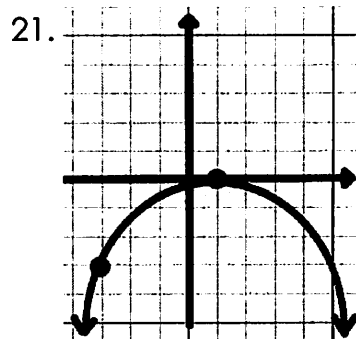
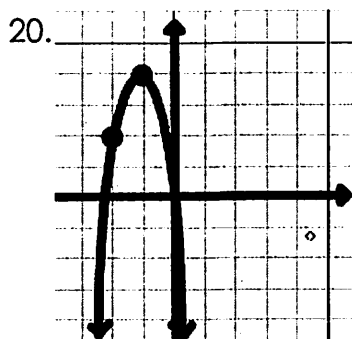
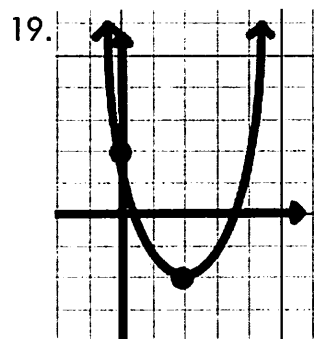
Name the vertex of the parabola. Name the a-value. Use the vertex and a-value to sketch the parabola. Remember to shade the inequalities.

7. $y \leq -(x - 1)^2 + 6$ 8. $y = 2(x + 5)^2 - 4$ 9. $y = -3x^2 + 10$
 10. $y < \frac{1}{4}x^2 - 3$ 11. $y = -\frac{1}{3}(x + 9)^2$ 12. $y > \frac{1}{5}(x - 10)^2 - 1$

Name the x-intercepts of the parabola. Then find the vertex. Use the vertex and roots to sketch the parabola. Remember to shade the inequalities.

13. $y = (x + 5)(x - 7)$ 14. $y = 2(x + 6)(x + 2)$ 15. $y = -(x - 3)(x - 11)$
 16. $y = -3(x + 1)(x - 3)$ 17. $y = \frac{2}{5}(x - 10)(x + 8)$ 18. $y = (2x - 5)(2x + 3)$

Set up the equation for each parabola in vertex form. Put your final answer in standard form.

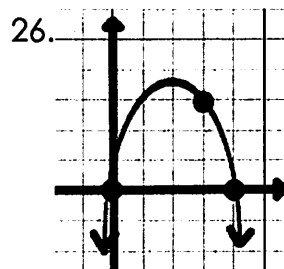
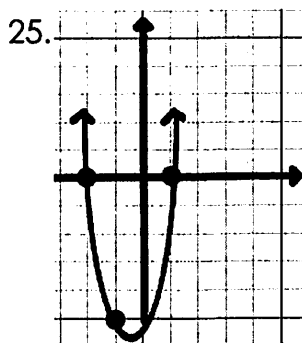
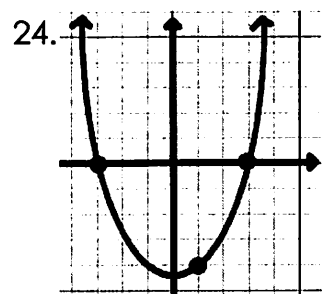


Sketch the parabola first. Then set up the equation for each parabola in vertex form.

22. vertex: $(2, -1)$
point: $(4, 3)$

23. vertex: $(-1, -6)$
point: $(1, -8)$

Set up the equation for each parabola in factored form. Put your final answer in standard form.



Sketch the parabola first. Then set up the equation for each parabola in factored form.

27. x-intercepts: 1, 4
point: $(3, 2)$

28. x-intercepts: -5, 0
point: $(-3, 18)$

Worksheet: Review graphing quadratic functions, Find intercepts

$y = 2x^2 - 16x + 20$	Form of Equation	Up or Down	1
Vertex		x-intercepts	
y-intercept		sketch	

$y = -x^2 + 6x - 4$	Form of Equation	Up or Down	2
Vertex		x-intercepts	
y-intercept		sketch	

$y = 2(x + 1)(x - 7)$	Form of Equation	Up or Down	3
Vertex	x-intercepts		
y-intercept	sketch		

$y = -(x + 4)(x - 2)$	Form of Equation	Up or Down	4
Vertex	x-intercepts		
y-intercept	sketch		

$y = -5(x + 6)^2 + 1$	Form of Equation	Up or Down	5
Vertex	x-intercepts		
y-intercept	sketch		

$y = \frac{1}{2}(x - 8)^2 - 2$	Form of Equation	Up or Down	6
Vertex	x-intercepts		
y-intercept	sketch		

$y = \frac{2}{3}(x + 6)^2 + 1$	Form of Equation	Up or Down	7
Vertex	x-intercepts		
y-intercept		sketch	

8. Find the y-intercepts of the quadratic functions. Do work on NB paper.

a) $y = -\frac{2}{3}x^2 + 6x - 9$ b) $y = 4(x - 5)^2 + 11$ c) $y = \frac{1}{2}(x + 6)(2x - 1)$

9. Find the x-intercepts of the quadratic functions. Do work on NB paper.

a) $y = -x^2 + 9$ b) $y = x^2 - 2x + 1$ c) $y = -x^2 - 2x + 8$

d) $y \geq 3x^2 + 6x - 2$ e) $y = 5(3x + 2)(x - 9)$ f) $y = -2(x + 6)^2$

g) $y = 2x^2 - 6$ h) $y = \frac{1}{3}(x - 12)^2 - 2$ i) $y = 4(x - 5)^2 + 11$

j) $y = -3(x - 2)^2 + 8$ k) $y = -\frac{1}{2}(x + 3)^2 - 1$