

Lesson 10-2

Monday, February 3, 2020 8:44 PM

Name _____

MB 593



Lesson 10-2

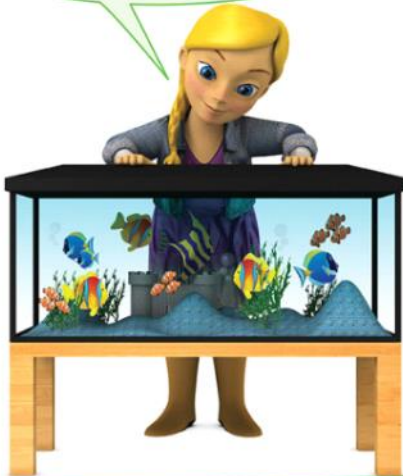
Develop a Volume Formula

Solve & Share

Kevin needs a new aquarium for his fish. The pet store has a fish tank in the shape of a rectangular prism that measures 5 feet long by 2 feet wide by 4 feet high. Kevin needs a fish tank that has a volume of at least 35 cubic feet. Will this fish tank be big enough? *Solve this problem any way you choose.*

Make Sense and Persevere

Read the problem carefully to make sure that you understand what you are trying to find. *Show your work!*



I can ...

find the volume of rectangular prisms using a formula.

Content Standards 5.MD.C.4, 5.MD.C.5a, 5.MD.C.5b
Mathematical Practices MP.1, MP.2, MP.3, MP.4, MP.6

Volume: Area of the base
x height of the prism

$$V = l \times w \times h$$

$$V = 5 \text{ ft} \times 2 \text{ ft} \times 4 \text{ ft}$$

$$V = 10 \text{ ft}^2 \times 4 \text{ ft}$$

$$V = 40 \text{ ft}^3$$

$$\text{Yes } 40 \text{ ft}^3 > 35 \text{ ft}^3$$

Look Back! © MP.3 Critique Reasoning Malcolm says the volume of the aquarium would change if its dimensions were 2 feet long, 4 feet wide, and 5 feet high. Do you agree? Explain.

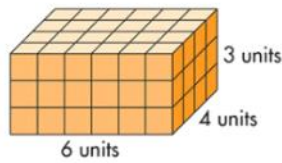
No. The commutative or associative properties say that the same factors can be multiplied in any order.

Essential Question

How Can You Use a Formula to Find the Volume of a Rectangular Prism?

Remember that volume is the number of cubic units (units^3) needed to pack a solid figure without gaps or overlaps.

Find the volume of the rectangular prism if each cubic unit represents 1 cubic foot.



You can find the volume of a rectangular prism by counting cubes or using a **formula**.

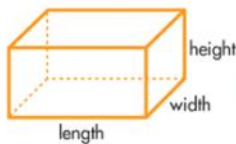


A formula is a rule that uses symbols to relate two or more quantities.

B If the dimensions of a rectangular prism are given as length ℓ , width w , and height h , then use this formula to find the volume V :

Volume = length \times width \times height

$V = (\ell \times w) \times h$ or $V = \ell \times (w \times h)$



The factors in the formula can be regrouped using the **Associative Property**.



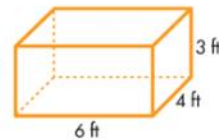
C Use the formula to find the volume of the rectangular prism.

$V = \ell \times w \times h$

$V = (6 \times 4) \times 3$

$V = 24 \times 3$

$V = 72$



The volume of the rectangular prism is 72 cubic feet or 72 ft^3 .

Convince Me! © MP.2 Reasoning Give the dimensions of a different rectangular prism that also has a volume of 72 ft^3 . Explain how you decided.

Handwritten work showing the factorization of 72:

$$72 \text{ ft}^3 = 12 \text{ ft}^2 \times 6 \text{ ft}$$

$$12 \text{ ft}^2 = 6 \text{ ft} \times 2 \text{ ft}$$

Handwritten dimensions:

length = 6 ft
width = 2 ft
height = 6 ft

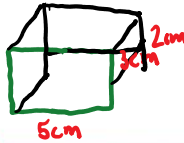
☆ Guided Practice

Do You Understand?

1. In the example on page 594, could you first multiply the width by the height? Explain.

Yes, b/c of the associative property

2. **MP.4 Model with Math** A wooden block measures 5 centimeters long, 3 centimeters wide, and 2 centimeters tall. Draw a rectangular prism to show the block and label it. What is the volume of the block?



$$V = l \times w \times h$$

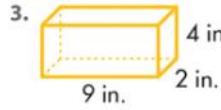
$$V = 5\text{ cm} \times 3\text{ cm} \times 2\text{ cm}$$

$$V = 15\text{ cm}^2 \times 2\text{ cm}$$

$$V = 30\text{ cm}^3$$

Do You Know How?

In 3 and 4, find the volume of each rectangular prism.

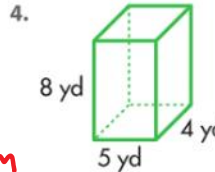


$$V = l \times w \times h$$

$$V = 9\text{ in} \times 2\text{ in} \times 4\text{ in}$$

$$V = 18\text{ in}^2 \times 4\text{ in}$$

$$V = 72\text{ in}^3$$



$$V = l \times w \times h$$

$$V = 5\text{ yd} \times 4\text{ yd} \times 8\text{ yd}$$

$$V = 20\text{ yd}^2 \times 8\text{ yd}$$

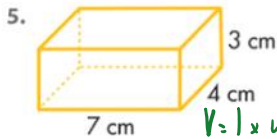
$$V = 160\text{ yd}^3$$

$$\begin{array}{r} 3 \\ 18 \\ \times 4 \\ \hline 72 \end{array}$$

☆ Independent Practice

In 5–10, find the volume of each rectangular prism.

Complete 5–7

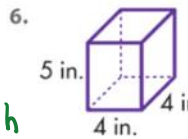


$$V = l \times w \times h$$

$$V = 7\text{ cm} \times 4\text{ cm} \times 3\text{ cm}$$

$$V = 28\text{ cm}^2 \times 3\text{ cm}$$

$$V = 84\text{ cm}^3$$

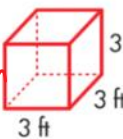


$$V = l \times w \times h$$

$$V = 4\text{ in} \times 4\text{ in} \times 5\text{ in}$$

$$V = 16\text{ in}^2 \times 5\text{ in}$$

$$V = 80\text{ in}^3$$

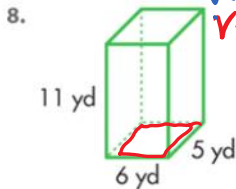


$$V = l \times w \times h$$

$$V = 3\text{ ft} \times 3\text{ ft} \times 3\text{ ft}$$

$$V = 9\text{ ft}^2 \times 3\text{ ft}$$

$$V = 27\text{ ft}^3$$

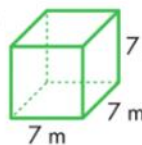


$$V = l \times w \times h$$

$$V = 6\text{ yd} \times 5\text{ yd} \times 11\text{ yd}$$

$$V = 30\text{ yds}^2 \times 11\text{ yds}$$

$$V = 330\text{ yds}^3$$

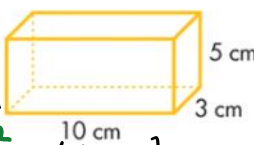


$$V = l \times w \times h$$

$$V = 7\text{ m} \times 7\text{ m} \times 7\text{ m}$$

$$V = 49\text{ m}^2 \times 7\text{ m}$$

$$V = 343\text{ m}^3$$



$$V = l \times w \times h$$

$$V = 10\text{ cm} \times 3\text{ cm} \times 5\text{ cm}$$

$$V = 30\text{ cm}^2 \times 5\text{ cm}$$

$$V = 150\text{ cm}^3$$

*For another example, see Set B on page 625.

Complete questions: 9, 10, 11, 12, 14, & 17

Math Practices and Problem Solving

In 11 and 12, use the picture of the dictionary.

11. The dictionary is 3 inches thick. What is the volume of the dictionary?

$$189 \text{ in}^3$$

$$V = l \times w \times h$$

$$V = 7 \text{ in} \times 9 \text{ in} \times 3 \text{ in}$$

$$V = 63 \text{ in}^2 \times 3 \text{ in}$$

$$V = 189 \text{ in}^3$$

12. **MP.2 Reasoning** A school orders 10 dictionaries. They cost \$25 each. The school also pays \$15 for shipping. How much does the school pay to get the new dictionaries? Show your work.

$$10 \text{ books} \times \$25 = \$250$$

$$\$250 + \$15 = \$265$$



7 in.

What operations do you need to use to solve this problem?

13. **MP.1 Make Sense and Persevere** The Outer Bay exhibit at the Monterey Bay Aquarium has a viewing window that is 56.5 feet long, 17 feet tall, and 13 inches thick. Estimate its volume in cubic feet. Remember 12 inches = 1 foot.

14. **Higher Order Thinking** What is the height of a rectangular prism that has a volume of 280 cubic meters, a length of 8 meters, and a width of 7 meters? Show how you found your answer.

$$V = l \times w \times h$$

$$240 \text{ m}^3 = 8 \text{ m} \times 7 \text{ m} \times h$$

$$280 \text{ m}^3 = 56 \text{ m}^2 \times h$$

$$\begin{array}{r} \times 5 \\ 56 \overline{) 280} \\ \underline{-280} \\ 0 \end{array}$$

The height is 5 m

15. **Algebra** Nat used the expression $3 \times s$ to find the cost of 3 shirts. What is the value of the expression if $s = \$16$?

16. The height of a tree is 8.194 meters. What is the height rounded to the nearest tenth of a meter?

Common Core Assessment

17. Choose all the expressions that can be used to find the volume of this wooden box.

- $(6 \times 4) \times 3$
- $(6 \times 4) + 3$
- 6×4
- $6 \times (4 \times 3)$ - Associative Property
- $(4 \times 3) \times 6$ - Associative Property

$$V = l \times w \times h$$

$$V = 6 \times 4 \times 3$$

