

Discrete Mathematics

2018-2019

Tom Tamburello ttamburello@lrhsd.org x3336

Stephanie Marone smarone@lrhsd.org x8579

Unit 2: Set Theory and Logic

Transfer goal: Students will be able to independently use their learning to construct valid conclusions, effectively communicate those conclusions and critique the reasoning of others.

Stage 1 – Desired Results

Established Goals

NJ Student Learning Standards for Mathematics

<http://www.state.nj.us/education/cccs/2016/math/hs>

Number and Quantity N-RNB3: Use properties of rational and irrational numbers.

Algebra A-APRA1: Perform arithmetic operations on polynomials.

NCTM Principles and Standards of School Mathematics

www.cssu.org/cms/lib5/VT01000775/Centricity/Domain/32/CSSUMathCurric

A2: Represent and analyze mathematical situations and structures using algebraic symbols.

21st Century Themes

www.21stcentruyskills.org

- Global Awareness
- Financial, Economic, Business and Entrepreneurial Literacy
- Civic Literacy
- Health Literacy
- Environmental Literacy

	<p style="text-align: center;"><u>21st Century Skills</u></p> <p><i>Learning and Innovation Skills:</i> <input checked="" type="checkbox"/> Creativity and Innovation <input checked="" type="checkbox"/> Critical Thinking and Problem Solving <input checked="" type="checkbox"/> Communication and Collaboration</p> <p><i>Information, Media and Technology Skills:</i> <input checked="" type="checkbox"/> Information Literacy <input type="checkbox"/> Media Literacy <input type="checkbox"/> ICT (Information, Communications and Technology) Literacy</p> <p><i>Life and Career Skills:</i> <input checked="" type="checkbox"/> Flexibility and Adaptability <input checked="" type="checkbox"/> Initiative and Self-Direction <input checked="" type="checkbox"/> Social and Cross-Cultural Skills <input checked="" type="checkbox"/> Productivity and Accountability <input checked="" type="checkbox"/> Leadership and Responsibility</p>
<p><u>Enduring Understandings:</u> <i>Students will understand that . . .</i></p> <p><i>EU 1</i> organizing elements into sets helps to order, arrange and classify the world.</p> <p><i>EU 2</i> the study of logic helps one to communicate effectively, make convincing arguments and develop patterns of reasoning for decision making.</p>	<p><u>Essential Questions:</u></p> <p><i>EU1</i></p> <ul style="list-style-type: none"> • How can set theory be used to make sense of the world around us? <p><i>EU 2</i></p> <ul style="list-style-type: none"> • How can a consumer determine if a company's conclusions are valid or misleading? • How is logic used in other fields? Why do we need logic?
<p><u>Knowledge:</u> <i>Students will know . . .</i></p> <p><i>EU 1</i></p> <ul style="list-style-type: none"> • the various methods and notations used to represent sets of objects. • the methods used to classify sets based on their size and content. • Venn diagrams can be used to model set operations, subsets, and to solve application problems. 	<p><u>Skills:</u> <i>Students will be able to . . .</i></p> <p><i>EU 1</i></p> <ul style="list-style-type: none"> • list sets in descriptive, roster, and set-builder notation form. • demonstrate the ability to use symbolic notation associated with set theory. • perform set operations including the complement, intersection, union, difference, and Cartesian product. • apply DeMorgan's Law. • use one-to-one correspondence to determine a set's cardinality.

EU 2

- simple and compound statements can be logically formed by using symbols and operators.
- truth tables are used to determine whether statements and arguments are valid, invalid or logically equivalent.
- the truth of conditional and biconditional statements is essential to understanding logic and real-life documents.

EU 2

- convert statements into symbolic form.
- construct truth tables for compound statements.
- use conditional and bi-conditional statements in truth tables.
- prove that statements are tautologies or self-contradictions.
- solve matrix problems by using logic.
- use truth tables to determine if statements are logically equivalent.
- classify arguments as valid or invalid.
- use logical arguments and Euler Diagrams to solve problems.
- design electrical circuits by using logical operators.
- explain the difference between series and parallel circuits.

Stage 2 – Assessment Evidence

Recommended Performance Task: EU 1

The Secretary of State is randomly selecting two countries of the world from the website: <https://www.randomlists.com/random-country>. As a future ambassador to those two countries, data must be collected about the similarities and differences between the two countries and the United States. A Venn Diagram will be created to analyze the similarities and differences with respect to geography, weather, religion, customs, and two other variables of your choice. As an ambassador from the United States visiting these countries, you need to be prepared to interact with all citizens. To prove to the Secretary of State that you are ready to travel to the countries you must create an accurate Venn Diagram representing all three countries (United States and the two random countries) and present your findings to the class.

Your Venn Diagram:

Includes the names of the three countries and labeled circles A, B and C.

Correctly compares and contrasts a total of six variables (see above) with respect to those countries

Is neatly organized and colorfully constructed

Your Presentation:

Summarizes your data and Venn Diagram by utilizing set theory vocabulary

Explains what this region represents:

$$A' \cup (B' \cup C)$$

Includes at least 3 important concepts for a visitor to be aware of when traveling to the other two countries

Is 3-5 minutes in length
Is clearly and professionally delivered

Other Evidence: *Tests, Quizzes, Prompts, Self-assessment, Observations, Dialogues, etc.*

Tests, quizzes and activities to include

An Essay about Georg Cantor, the originator of set theory

Posters of Venn diagrams with data collected from in-class surveys

Class data collection and organization involving set operations

SAT problems involving unions and intersections

A Ticket to Leave about DeMorgan's Law

Round Robin cooperative learning activity with one member of the group filling in one column of the truth table, and then passing it to the next person to do the next column, and then continue that process

Paired-Verbal Fluency Summarizer on the relationship between set theory operations and logic operators

Stage 3 – Learning Plan

Suggested Learning Activities to Include Differentiated Instruction and Interdisciplinary Connections: *Consider the WHERETO elements*

Activity 1: NCTM's Life's a Lottery (T)

- Students will apply Venn Diagrams to data regarding lottery winners
- Students will use Logic and Venn Diagrams to analyze advertising effectiveness
- http://www.nctm.org/Publications/Mathematics-Teacher/2006/Vol100/Issue4/Media-Clips_-Life_s-a-Lottery;-Heartburn/

Activity 2: Logic Matrix Problems (T)

- Students will be differentiated based on varying levels of difficulty and solve matrix logic problems
- Students will utilize logic theory and laws to solve puzzles
- <http://www.logic-puzzles.org/init.php>

Key Vocabulary Includes:

set	one-to-one correspondence	exclusive or	logically equivalent
elements	empty set/null set	inclusive or	converse
members	aleph-null	statement	inverse
well defined	universal set	simple statements	contrapositive
description	subset	compound statements	symbolic argument
braces	proper subset	negation	premise
roster from	Venn Diagram	quantifiers	conclusion
natural numbers	disjoint	conjunction	valid argument
counting numbers	complement	disjunction	invalid argument (fallacy)
ellipsis	intersection	neither-nor	law of contraposition (modus tollens)
set-builder notation	union	conditional	distinctive syllogism
finite set	Cartesian product	antecedent	sylogistic argument (syllogism)
infinite set	DeMorgan's laws	biconditional	Euler diagram
equal sets	cardinal number	truth table	series circuit
countable sets	Aristotelian logic	self-contradiction	parallel circuit
cardinal number	symbolic logic	tautology	equivalent circuits
equivalent sets	connectives	implication	

Approximate Timeline: 20 days

Use set theory vocabulary (A)
Categorize sets using set theory vocabulary (M)
Create and use subsets (M)
Use Venn Diagrams to model and perform operations on sets (M)
Verify the equality of sets (M)
Use and apply DeMorgan's Laws (T)
Solve problems by using set theory (T)
Activity 1: Life's a Lottery (T)
Calculate the cardinality of sets (M)
Set Theory Ambassador Performance Task (T)
Use symbolic form to write statements (A)
Explain truth tables for negation, conjunction, disjunction, conditionals and bi-conditionals (A)
Construct truth tables for compound statements (T)
Prove that statements are tautologies or self-contradictions (T)
Activity 2: Solve logic matrix problems (T)
Use truth tables to determine logical equivalence (T)
Explain laws of logic-detachment, contraposition, syllogism (A)
Explain fallacies of logic-converse, inverse, false chain (A)
Use laws of logic and Euler Diagrams to solve problems (M)
Use logic to design electric circuits (M)