Summer Math

The Summer Before 8th Grade



Summer Math

7th Grade Honors

The Summer Before 8th Grade



Summer Math Sections:	Notes:
Summer Math The Summer Before 8th Grade Practice Packet	Focuses On: - all four operations with integers (including order of operations problems with integers) - all four operations with rational numbers (positive and negative decimals, fractions, and mixed numbers) - solving one- and two-step equations - solving proportions and percent problems - area, perimeter, circumference, surface area, and volume - Evaluating algebraic expressions using the order of operations - Distributive Property - Simplifying Algebraic Expressions - Solving 1-Step Equations - Solving 2-Step Equations - Solving Multi-Step Equations - Scientific Notation - Exponent Rules - Slope & Rate of Change - Graphing Linear Functions from Slope-Intercept Form - Solving Proportions - Similar Figures - The Pythagorean Theorem Includes explanations & examples and practice problems for the summer. Recommended Use: - Practice 25 problems a week for 8 weeks - Show all your work and calculations - Provided answer key to check your work.
Virtual Nerd Video Tutorial Browser See Provided Letter	Recommended Use: View supporting math video tutorials before, during, or after your practice session with your summer math packet. Actively view the videos while recording and solving examples.

Middle School Summer Math The Summer Before 8th Grade

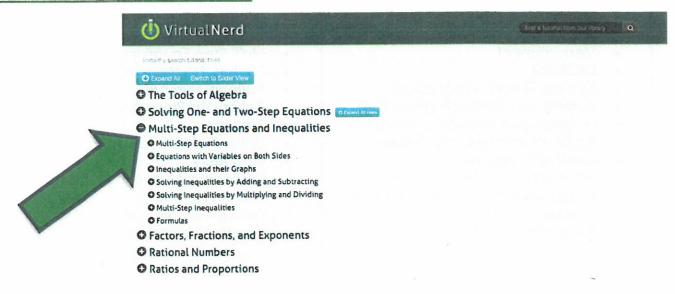


Virtual Nerd is an expansive library of instructional math content. Please use it this summer as a supplemental learning resource. It is a helpful resource that helps bring practice, clarity and skill reinforcement to your at home math routine.

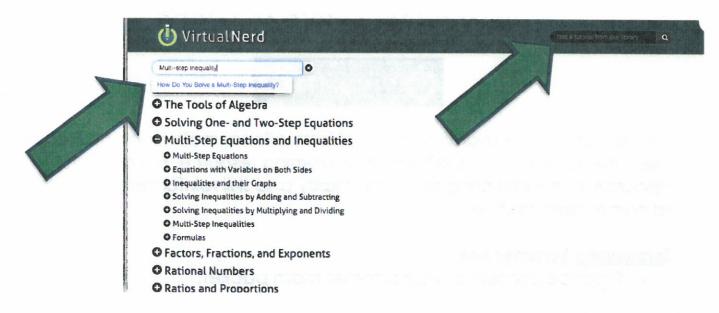
Suggested Summer Use:

- Practice content in your summer math packet.
- Use a mobile device to SCAN your grade level's QR code(s) to access the Virtual Nerd website. If you're using a desktop or laptop computer use the provided website.
- Search for a video related to the math content practiced in your packet that day. For example: if you're working on finding the MULTI-STEP INEQUALITIES in your math packet, either before, during or after your practice session, search MULTI-STEP INEQUALITIES by expanding the topic lists (Click on the + sign until you find your topic and specific tutorial) OR type directly into the search bar by keyword or topic.

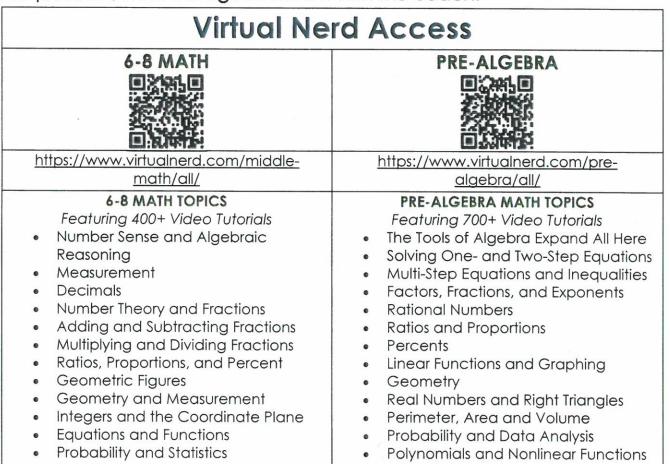
EXPANDING TOPICS OPTION



SEARCH BAR OPTION



View the video with a <u>notebook</u> and <u>pencil</u>. Walk through the examples in the video with the instructional coach. Play the video, pause to copy the problem, work through to solve it with the coach.



Operations with Integers

Adding Integers

 <u>Negative + Negative</u>: Add the absolute values of the two numbers and make the answer negative.

ex:
$$-5 + (-9)$$
 \longrightarrow $5 + 9 = 14$ \longrightarrow answer: (-14)

• <u>Negative + Positive (or Positive + Negative)</u>: Subtract the absolute values of the two numbers (larger minus smaller) and take the sign of the number with the greater absolute value.

ex:
$$-7 + 12 \longrightarrow 12 - 7 = 5 \longrightarrow 12 > 7$$
, so answer is positive \longrightarrow answer: 5

ex:
$$6 + (-9)$$
 \longrightarrow $9 - 6 = 3$ \longrightarrow $9 > 6$, so answer is negative \longrightarrow answer: (-3)

Subtracting Integers

 Keep the first number the same, change the subtraction sign to an addition sign, and change the sign of the second number. Then use the integer addition rules.

ex:
$$-3 - 9 \longrightarrow -3 + (-9) = (-12)$$

ex:
$$15 - (-8) \longrightarrow 15 + 8 = 23$$

ex:
$$-6 - (-4) \longrightarrow -6 + 4 = (-2)$$

Multiplying & Dividing Integers

Ignore the signs and multiply or divide as usual. Then determine the sign of the answer using the following rules:

- Negative · or ÷ Negative = Positive
- Negative · or ÷ Positive (or Positive · or ÷ Negative) = Negative

ex:
$$-3 \cdot (-5)$$
 \longrightarrow $3 \cdot 5 = 15$ \longrightarrow neg · neg = pos \longrightarrow answer: (15)

ex:
$$48 \div (-6)$$
 \longrightarrow $48 \div 6 = 8$ \longrightarrow pos \div neg = neg \longrightarrow answer: -8

Order of Operations

Parentheses
Exponents
Multiplication & Division (left to right)
Addition & Subtraction (left to right)

Find the sum or difference.

Find the product or quotient.

Evaluate the numerical expression. (Be sure to use the order of operations!)

Operations with Rational Numbers

Adding & Subtracting Rational Numbers

Determine whether you should add or subtract using integer rules. Then add or subtract.

• <u>Decimals</u>: Line up the decimal points. Then add or subtract and bring the decimal point down. Use integer rules to determine the sign of the answer.

ex: -9.8 + 6.24
$$\longrightarrow$$
 neg + pos: subtract $\longrightarrow \frac{9.80}{6.24} \longrightarrow$ answer: $\frac{-9.8}{3.56}$

• <u>Fractions/Mixed Numbers</u>: Find a common denominator and then add or subtract. Borrow or convert an improper fraction answer, if necessary. Use integer rules to determine the sign of the answer.

ex:
$$5\frac{3}{4} - \left(-3\frac{7}{8}\right) \longrightarrow 5\frac{3}{4} \quad 3\frac{7}{8} \longrightarrow \text{pos + pos: add} \longrightarrow \frac{5\frac{3}{4} - \frac{6}{8}}{8\frac{13}{8}} \longrightarrow \text{answer: } 9\frac{5}{8}$$

Multiplying & Dividing Rational Numbers

Determine the sign of the answer using integer rules. Then multiply or divide.

• <u>Multiplying Decimals</u>: Ignore the decimal points. Multiply the numbers. Then count the decimal places in the problem to determine the location of the decimal point in the answer.

ex: -9.23 · (-1.1)
$$\longrightarrow$$
 neg · neg = pos \longrightarrow $\xrightarrow{\begin{array}{c} 9.23 \\ \times 11 \\ 923 \\ \hline 10.153 \end{array}}$ answer: (0.153)

• <u>Dividing Decimals</u>: Move the decimal in the divisor to the end of the number. Move the decimal in the dividend the same number of places and then bring it straight up in quotient.

ex:
$$-5.2 \div 0.2 \longrightarrow \text{neg} \div \text{pos} = \text{neg} \longrightarrow 02. \boxed{52}. \longrightarrow \text{answer:} \boxed{-26}$$

<u>Multiplying Fractions</u>: Convert mixed numbers to improper fractions. Then cross-simplify.
 Multiply the numerators and multiply the denominators. Simplify if necessary.

ex:
$$-1\frac{3}{4} \cdot \frac{6}{14} \rightarrow \text{neg} \cdot \text{pos} = \text{neg} \rightarrow \frac{1}{2} \frac{7}{4} \cdot \frac{63}{42} = \frac{3}{4} \rightarrow \text{answer} = \frac{3}{4}$$

 <u>Dividing Fractions</u>: Convert mixed numbers to improper fractions. Then flip the second fraction to its reciprocal and multiply the two fractions. Simplify if necessary.

ex:
$$-\frac{1}{2} \div \left(-\frac{3}{8}\right) \longrightarrow \text{neg} \div \text{neg} = \text{pos} \longrightarrow \frac{1}{2} \cdot \frac{8}{3} = \frac{4}{3} \longrightarrow \text{answer:} \boxed{\frac{1}{3}}$$

Find the sum, difference, product, or quotient.

33. 38.61 + 36.841

34. 1.755 - 1.23 35. 0.71 · 9.2

36. |3.|2 ÷ 0.|

37. 3.651 - (-12.63) 38. -3.9 + (-7.6)

39. 17.6 · 4.3

40. 6 · (-16.7)

41. 26.474 - 14.527 42. -2.1 + 3.78

43. -6. I5 ÷ (-8.2)

44. - 12.8 · (-4.88)

Find the sum, difference, product, or quotient.

48. $3 \frac{1}{2} \div \frac{3}{7}$

49. 3 1/3 - 5 1/9

50. $5 \cdot (-1^2/5)$

51. $-4^{2}/_{3} + (-1^{3}/_{4})$ 52. $-5/_{6} \div (-2^{1}/_{6})$

53. $9 \div (-4 \frac{1}{2})$

54. - 18 + 3 ⁴/₅

55. -5 ²/₃ · (-2 ⁵/₆) 56. -5 ³/₄ - (-3 ⁷/₈)

Solving Equations

Solving One-Step Equations

• Cancel out the number on the same side of the equation as the variable by using the inverse operation. (Addition/Subtraction; Multiplication/Division). Be sure to do the same thing to both sides of the equation!

ex:
$$6x = -18$$
 \longrightarrow $6x = -18 \longrightarrow$ answer: $(x = -3)$

ex:
$$y + 23 = -9$$
 \longrightarrow $y + 23 = -9$ \longrightarrow answer: $y = -32$

ex:
$$\frac{h}{3} = 4$$
 \longrightarrow $3 \cdot \frac{h}{3} = 4 \cdot 3$ \longrightarrow answer: $(h = 12)$

ex:
$$w - 13 = -5$$
 \longrightarrow $w - 13 = -5$ \longrightarrow answer: $w = 8$

Solving Two-Step Equations

 Undo operations using inverse operations one at a time using the order of operations in reverse. (i.e.: undo addition/subtraction before undoing multiplication/division)

ex:
$$7x - 4 = -32$$
 \longrightarrow $7x - \frac{1}{4} = -32$ \longrightarrow $\frac{7x}{7} = \frac{-28}{7}$ \longrightarrow answer: $(x = -4)$

ex:
$$\frac{j}{5} + 13 = 15$$
 \longrightarrow $\frac{j}{5} + 13 = 15$ \longrightarrow $5 \cdot \frac{j}{5} = 2 \cdot 5$ \longrightarrow answer: $(j = 10)$

ex:
$$\frac{b+7}{3} = -2$$
 \longrightarrow $3 \cdot \frac{b+7}{3} = -2 \cdot 3$ \longrightarrow $b+\frac{1}{7} = -6$ \longrightarrow answer: $b=-13$

Solve the one-step equation.

57.
$$19 + j = -34$$

58. m - 26 = 13 59.
$$\frac{x}{5}$$
 = -3

59.
$$\frac{x}{5} = -3$$

60.
$$12f = 216$$

6 l.
$$g - (-3) = -7$$

62.
$$\frac{h}{9} = 13$$

63.
$$b + (-3) = -9$$

$$64. -4w = -280$$

Solve the two-step equation.

65.
$$5m - 3 = 27$$
 66. $7 + \frac{9}{2} = -3$

67.
$$4 + 3r = -8$$

68.
$$\frac{1}{2}p - 4 = 7$$

69.
$$\frac{k+8}{3} = -2$$

70.
$$\frac{f}{5}$$
 - (-13) = 12

71.
$$-15 - \frac{9}{3} = -5$$

72.
$$-8 + 4m = 2$$

73.
$$-18 - \frac{3}{4}v = 3$$

74.
$$\frac{-5+n}{4} = -1$$

75.
$$3.5m + 0.75 = -6.25$$
 76. $2y + 3 = 19$

76.
$$2y + 3 = 19$$

Proportions and Percent

Solving Proportions

 Set cross-products equal to each other and then solve the one-step equation for the given variable.

ex:
$$\frac{5}{b} = \frac{4}{10}$$
 \longrightarrow $5 \cdot 10 = 4b$ \longrightarrow $\frac{50}{4} = \frac{4b}{4}$ \longrightarrow answer: $b = 12.5$

Solving Percent Problems with Proportions

• Set up and solve a proportion as follows: $\frac{4}{100} = \frac{\text{part}}{\text{whole}}$

ex: 25 is what percent of 500?
$$\rightarrow \frac{x}{100} = \frac{25}{500} \rightarrow \text{answer: } x = \boxed{5}$$

ex: What is 15 % of 88?
$$\longrightarrow \frac{15}{100} = \frac{x}{88} \longrightarrow \text{answer: } x = (13.2)$$

ex: 18 is 30% of what number?
$$\longrightarrow \frac{30}{100} = \frac{18}{x} \longrightarrow \text{answer: } x = 60$$

Solving Percent Problems with Equations

 Translate the question to an equation and then solve. (Be sure to convert percents to decimals or fractions.)

ex: 20 is 40% of what number?
$$\longrightarrow$$
 20 = 0.4x \longrightarrow answer: x = 50

ex: 8 is what percent of 32?
$$\longrightarrow$$
 8 = 32x \longrightarrow x = 0.25 \longrightarrow answer: 25%

ex: What is 25 % of 88?
$$\longrightarrow$$
 x = 0.25 · 88 \longrightarrow answer: x = (22)

Real-World Percent Problems

(This is just one way of many to solve real-world percent problems)

- <u>Tax</u>: Find the amount of tax using a proportion or equation. Then add the tax to the original amount to find the total cost.
- <u>Discount</u>: Find the amount of the discount using a proportion or equation. Then subtract the amount of discount from the original price to find the sale price.

Solve the proportion.

77.
$$\frac{h}{6} = \frac{20}{24}$$

78.
$$\frac{5}{7} = \frac{c}{14}$$

79.
$$\frac{6}{8} = \frac{21}{b}$$

80.
$$\frac{30}{j} = \frac{26}{39}$$

81.
$$\frac{5}{k} = \frac{15}{20}$$

82.
$$\frac{32}{112} = \frac{a}{14}$$

83.
$$\frac{16}{7} = \frac{18}{9}$$

$$84. \ \frac{w}{60} = \frac{15}{200}$$

Solve the percent problem.

Geometry

Geometry Basics

- · Perimeter is the distance around a polygon
- · Circumference is the distance around a circle
- Area is the space inside a figure
- · Volume is the capacity of a 3-dimensional figure
- Surface Area is the sum of the areas of all the faces on a 3-dimensional figure

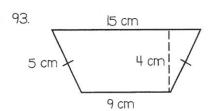
2-Dimensional Geometry Formulas

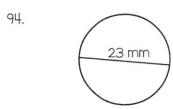
- Perimeter of Any Figure: sum of side lengths
- Circumference = π · diameter
- Area of Parallelogram = base · height
- Area of Triangle = $\frac{1}{2}$ base height
- Area of Trapezoid = $\frac{1}{2}$ · height(base₁ + base₂)
- Area of Circle = π · radius²

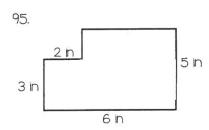
3-Dimensional Geometry Formulas

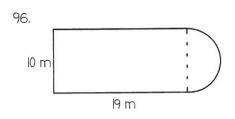
- Volume of Rectangular Prism = length · width · height
- Volume of Cylinder = $\pi \cdot \text{radius}^2 \cdot \text{height}$
- Surface Area of Rectangular Prism = $2 \cdot length \cdot width + 2 \cdot length \cdot height + 2 \cdot height \cdot width$
- Surface Area of Cylinder = $2 \cdot \pi \cdot \text{radius}^2 + 2 \cdot \pi \cdot \text{radius} \cdot \text{height}$

Find the perimeter (or circumference) and area. Use 3.14 for pi.

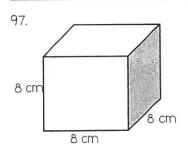


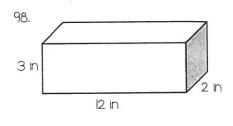


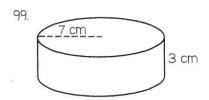


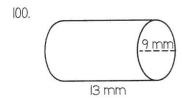


Find the surface area and volume.









Evaluating Algebraic Expressions

- 1. Substitute the given values for the variables in the expression
- 2. Evaluate the expression using the order of operations
 - Parentheses/Brackets (inside to outside)
 - Exponents
 - Multiplication/Division (left to right)
 - Addition/Subtraction (left to right)

ex:
$$9x^2 - 4(y + 3z)$$

for $x = -3$, $y = 2$, $z = 5$
 $9(-3)^2 - 4(2 + 3 \cdot 5)$

$$9(-3)^2 - 4(2 + 15)$$

$$9(-3)^2 - 4 \cdot 17$$

$$81 - 4 \cdot 17$$

$$81 - 68 = 13$$

The Distributive Property

- 1. Multiply the number outside the parentheses by each term in the parentheses.
- 2. Keep the addition/subtraction sign between each term.

ex:
$$5(8x - 3)$$

 $5(8x - 3)$
 $5(8x) - 5(3)$
 $40x - 15$

Simplifying Algebraic Expressions

- 1. Clear any parentheses using the Distributive Property
- 2. Add or subtract like terms (use the sign in front of each term to determine whether to add or subtract)

ex:
$$2(3x - 4) - 12x + 9$$

 $2(3x - 4) - 12x + 9$
 $6x - 8 - 12x + 9$

Evaluate each expression for a = 9, b = -3, c = -2, d = 7. Show your work.

i. a - cd	2. $2b^3 + c^2$	3. <u>a + d - c</u> b	4. $(a - b)^2 + d(a + c)$
5. 4c - (b - a)	6. <u>a</u> - 5a	7. 2bc + d(12 - 5)	8. b + 0.5[8 - (2c + a)]

Simplify each expression using the Distributive Property.

9. 5(2g – 8)	10. 7(y + 3)	113(4w – 3)	12. (6r + 3)2

Simplify each expression, showing all work.

r	13. 8(x + 1) - 12x	14. $6w - 7 + 12w - 3z$	15. $9n - 8 + 3(2n - 11)$	16. 3(7x + 4y) - 2(2x + y)
r	17. (15 + 8d)(-5) - 24d + d	18. 9(b - 1) - c + 3b + c	19. 20f - 4(5f + 4) + 16	20. 8(h - 4) - h - (h + 7)
T				
L				

Solving One-Step Equations

- Cancel out the number on the same side of the equal sign as the variable using inverse operations (addition/subtraction; multiplication/division)
- 2. Be sure to do the same thing to both sides of the equation!

ex:
$$-18 = 6j$$

 $-18 = 6j$
 $-6 = 6j$
 $-3 = j \longrightarrow j = -3$

Solving Two-Step Equations

- . Undo operations one at a time with inverse operations, using the order of operations in reverse (i.e. undo addition/subtraction before multiplication/division)
- 2. Be sure to always do the same thing to both sides of the equation!

ex:
$$\frac{a}{7} - 12 = -9$$

$$\frac{a}{7} - 12 = -9$$

$$\frac{a}{7 + 12 + 12}$$

$$\frac{a}{7 \times 7} = 3 \times 7$$

$$a = 21$$

Solving Multi-Step Equations

- 1. Clear any parentheses using the Distributive Property
- 2. Combine like terms on each side of the equal sign
- 3. Get the variable terms on the same side of the equation by adding/subtracting a variable term to/from both sides of the equation to cancel it out on one side
- 4. The equation is now a two-step equation, so finish solving it as described above

ex:
$$5(2x - 1) = 3x + 4x - 1$$

 $10x - 5 = 3x + 4x - 1$
 $10x - 5 = 7x - 1$
 $-7x - 7x$
 $3x - 5 = -1$
 $+5 + 5$
 $3x = 4$
 $3x = 4$
 $3x = 4$

Solve each equation, showing all work.

21. f - 64 = -23	227 = 2d	b .	24. 13 = m + 21
		$\frac{b}{23} = -6$	
25. $5x - 3 = -28$	(i) + 8	h	28. 22 = 6y + 7
25. 54 - 720	26. $\frac{\omega + 8}{-3} = -9$	27. $-8 + \frac{h}{4} = 13$	20. 22 - 49 1 7
29. $8x - 4 = 3x + 1$	30. $-2(5d - 8) = 20$	31. 7r + 21 = 49r	329g - 3 = -3(3g + 2)
	30. 2(05. 3) 20		, , , , , , , , , , , , , , , , , , , ,
			283
		*	
33. $5(3x - 2) = 5(4x + 1)$	34. $3d - 4 + d = 8d - (-12)$	35. $f - 6 = -2f + 3(f - 2)$	36. $-2(y-1) = 4y - (y+2)$
33. 0(3). 2/ 0(1). 1/			

Scientific Notation

Standard Form to Scientific Notation: move the decimal after the first non-zero digit and eliminate any trailing zeros. Multiply by 10 to the power equal to the number of places you moved the decimal point. If the original number was greater than 1, the exponent is positive. If the number was less than 1, the exponent is negative.

Scientific Notation to Standard Form: move the decimal point the number of places indicated by the exponent. If the exponent is positive, move the decimal right. If negative, move left.

ex: 0.0000571

0,00005,71

Original number < 1, so negative exponent

$$= 5.71 \times 10^{-5}$$

ex: 3.5 x 103

Positive exponent, so move decimal right

Negative Exponents & Simplifying Monomials

Zero Exponent: Any number raised to the zero power equals 1

ex: $y^0 = 1$

Negative Exponent: Move the base to the opposite side of the fraction line and make the exponent positive

ex: $x^{-4} = \frac{1}{x^4}$

Monomial x Monomial: Multiply the coefficients and add the exponents of like bases

ex: $(4x^3)(2x^5) = 8x^8$

Monomial ÷ Monomial: Divide the coefficients and subtract the exponents of like bases

ex: $\frac{a}{a^6} = a^{-5} = \frac{1}{a^5}$

<u>Power of a Monomial</u>: Raise each base (including the coefficient) to that power. If a base already has an exponent, multiply the two exponents

ex: $(-2fg^5)^3 = -8f^3g^{15}$

<u>Power of a Quotient</u>: Raise each base (including the coefficient) to that power. If a base already has an exponent, multiply the two exponents

ex: $\left(\frac{5d^3}{c}\right)^2 = \frac{25d^6}{c^2}$

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37. 67,000,000,000	38. 0.0009213	39. 0.0000000004	40. 3,201,000,000,000,000

Convert each number to Standard Form.

41. 5.92 x 10 ⁻⁵	42. I.I x 10 ⁷	43. 6.733 x 10 ⁻⁸	44. 3.27 x 10 ²
		ii	

Simplify each expression. Write your answers using only positive exponents.

45. w ⁻⁹	46. $\frac{m^5}{m^2}$	47. f ⁵ · f ³	48. $\left(\frac{h^2}{g}\right)^3$
49. (a ⁵) ²	50. $\frac{1}{b^{-3}}$	51. z ⁰	52. 4r ⁶ · 3r · 2r ²
53. $\frac{qp^{-2}}{3q^{-3}}$	54. <u>8d³</u> 2cd ⁻²	55. (g ⁴ h) ² · (2g ³ h ⁻¹) ²	56. (6a)º
57. (-3n ² k ⁴) ²		59. <u>6 · 107</u> 2 · 103	60. (1.5 · 10 ⁻⁶) · (4 · 10 ⁹)

Slope & Rate of Change

<u>Finding the Slope Given Two Points</u>: Use the coordinates from the points in the slope formula:

Slope (m) =
$$\frac{y_2 - y_1}{x_2 - x_1}$$

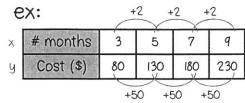
<u>Finding the Rate of Change From a Table</u>: Determine the amount the dependent variable (y) is changing and the amount the independent variable (x) is changing.

Rate of Change =
$$\frac{\text{change in } y}{\text{change in } x}$$

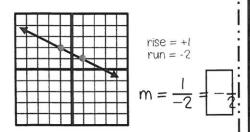
<u>Finding the Slope From a Graph</u>: Choose 2 points on the graph. Find the vertical change (rise) and horizontal change (run) between the 2 points and write it as a fraction $\frac{\text{rise}}{\text{run}}$. (Up is positive, down is negative, right is positive, and left is negative).

ex:
$$(4, -2)$$
, $(-3, 8)$

$$m = \frac{8 - (-2)}{-3 - 4} = \frac{10}{-7} = -\frac{10}{7}$$



$$m = \frac{50}{2} = 25 \text{ dollars/month}$$



Graphing Linear Equations

Slope-Intercept Form: y = mx + bslope y-intercept

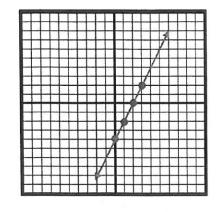
How To Graph:

- 1. Make a point on the y-axis at the y-intercept.
- Use the slope to determine where to make the next point. The numerator tells you the rise (how far up/down) and the denominator tells you the run (how far right/left) to make the next point.
- 3. Repeat to make more points and then connect the points with a line.

ex: y = 2x - 4

y-intercept: -4

slope: $2 = \frac{2}{1} \leftarrow rise$



Find the slope of the line that passes through the points. Show your work.

61. (-5, 3), (2, 1)

62. (8, 4), (11, 6)

63. (9, 3), (9, -1)

64. (-4, -2), (-6, 4)

Find the rate of change. Show your work.

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65.	н
	н
	-1
	-1

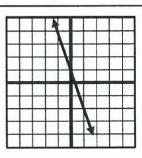
Number of Hours	3	6	9	12
Distance (in miles)	135	270	405	540

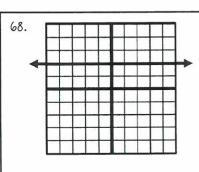
66.

Number of Weeks	1	3	5	7
Pounds	173	169	165	161

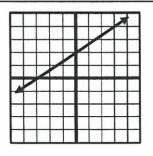
Find the slope of the line.

67.



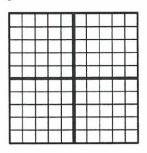


69.

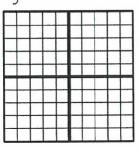


Graph the line.

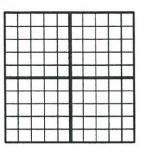
70.
$$y = -x - 3$$



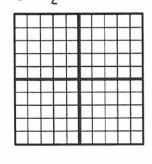
71.
$$y = \frac{1}{3}x + 2$$



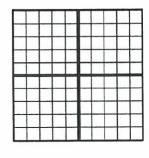
72.
$$y = -3x - 1$$



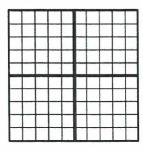
73.
$$y = -\frac{3}{2}x - 2$$



74.
$$y = 2x + 1$$



75.
$$y = \frac{1}{4}x$$



Solving Proportions

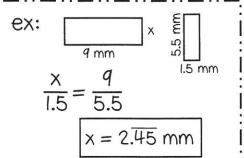
- 1. Set the two cross-products equal to each other
- 2. Solve the equation for the variable

ex:
$$\frac{m}{4} = \frac{3}{5}$$

 $\frac{5m}{5} = \frac{12}{5}$
 $m = 2.4$

Similar Figures

- To find a missing side length, set up a proportion, matching up corresponding sides.
- 2. Solve the proportion using the steps above.

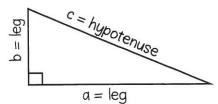


The Pythagorean Theorem

*** The Pythagorean Theorem applies to right triangles only **

The sides next to the right angle (a ε b) are legs

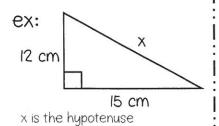
The side across from the right angle (c) is the hypotenuse



Pythagorean Theorem: $a^2 + b^2 = c^2$

To find the hypotenuse: add the squares of the legs and then find the square root of the sum

To find a leg: subtract the square of the given leg from the square of the hypotenuse and then find the square root of the difference



 $12^2 + 15^2 = x^2$ $144 + 225 = x^2$

$$369 = x^2$$

$$x = \sqrt{369} \approx 19.2 \text{ cm}$$

ex:
$$a = ?$$
, $b = 3$, $c = 6$
a is a leg
$$a^{2} + 3^{2} = 6^{2}$$

$$a^{2} + 9 = 36$$

$$a^{2} = 36 - 9 = 27$$

$$a = \sqrt{27} \approx 5.2$$

Solve each proportion, showing all work.

76.	6	4
	7 =	\overline{m}

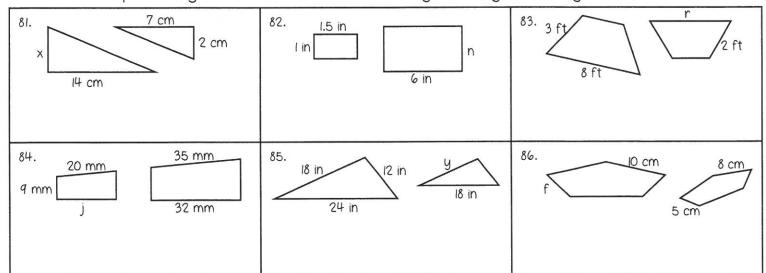
$$\frac{12}{5} = \frac{k}{3}$$

$$\frac{78}{7} = \frac{8}{2}$$

$$\frac{79.}{n} = \frac{9}{36}$$

30.
$$\frac{4}{21} = \frac{3}{c}$$

Assume each pair of figures is similar. Find the missing side length, showing all work.



Find the missing side length in each right triangle to the nearest tenth. Show your work!

This the missing side length in each right thangle to the hear est tenth. The goal work:					
o7. a = 6, b = 8, c = ?	88. a=?, b=9cm, c=13cm	89. a = 7, b = ?, c = 14	90. a = 14 in, b = 14 in, c = ?		
91. 3 5 x	92. X 10 mm	93. 7 in x	94. 20 18		
95. <u>15</u>	96. 104 in 52 in x	97. 35 ft 10 ft	98. x 24 cm 20 cm		

etermine whether or not you can form a right triangle from the given side lengths. Explain.

	 0 .0	
99. 18, 22, 26	100. 5, 12, 13	
	400	

Summer Math Math Answer Key The Summer Before 8th Grade

SEACREST

COUNTRY DAY SCHOOL

Answer Key

l. -3

5. 17

9.80

13. 5

17. 110

21. -7

25. 34

29. -24

33. 75.451

37. |6.28|

41. 11.947

45. 30 ³/₄

49. -17/9

53. -2

57. j = -53

61. g = -38

65. m = 6

69. k = -14

73. v = -28

77. h = 5

81. $k = 6^{2/3}$

85. |2.75

89. 20%

93. P = 34 cm; $A = 48 \text{ cm}^2$

97. $SA = 384 \text{ cm}^2$; $V = 512 \text{ cm}^3$

2. 237

6. 339

10. -81

14. 97

18. -15

22. 98

26. -27

30. -55

34. 0.525

38. -11.5

42. 1.68

46. 1 1/20

50. -7

54. -14 1/5

58. m = 39

62. h = 117

66. y = -20

70. f = -5

74. n = 1

78. c = 10

82. a = 4

86. 8

90. 27

94. C = 72.22 mm; $A = 415.265 \text{ mm}^2$

98. $SA = 132 \text{ in}^2$; $V = 72 \text{ in}^3$

3. -97

7. 6

11. 36

15. - 176

19. - 177

23. 108

27. - 168

31. -41

35. 6.532

39. 75.68

43. 0.75

47. 4 1/20

51. -6 ⁵/₁₂

55. 16 1/8

59. X = -15

63. b = -6

67. r = -4

71. g = -30

75. m = -2

79. b = 28

83. $g = 7^{7/8}$

•

87. |2.5%

91. \$46.40

95. P = 22 in; $A = 26 \text{ in}^2$

99. $SA = 439.6 \text{ cm}^2$; $V = 461.58 \text{ cm}^3$

4. 196

8. -41

12. 26

16. - 120

20. 14

24. 34

28. 77

32. - 16

36. |3|.2

40. -100.2

44. 62.464

48. 2 9/20

52. ⁵/₁₃

56. -17/8

60. f = 18

64. W = 70

68. p = 22

72. $m = 2 \frac{1}{2}$

76. y = 8

80. j = 45

84. $W = 4 \frac{1}{2}$

88. 9

92. \$14.98

96. P = 63.7 m; $A = 229.25 \text{ m}^2$

100. $SA = 494.55 \text{ mm}^2$; $V = 826.605 \text{ mm}^3$

Evaluate each expression for a = 9, b = -3, c = -2, d = 7. Show your work.

1. a - cd	2. $2b^3 + c^2$	3. $\frac{a + d - c}{b}$	4. $(a - b)^2 + d(a + c)$
23	-50	-6	193
5. 4c - (b - a) 4	6. $\frac{a}{b}$ - 5a -48	7. 2bc + d(12 - 5)	8. b + 0.5[8 - (2c + a)]
4	-48	61	-1.5

Simplify each expression using the Distributive Property.

4. 5(2g - 8)	10. $7(y + 3)$	113(4w – 3)	12. (6r + 3)2
10g - 40	74 + 21	-12w + 9	12r + 6
	3		

Simplify each expression, showing all work.

13. 8(x + 1) - 12x	14. 6w - 7 + 12w - 3z	15. $9n - 8 + 3(2n - 11)$	16. $3(7x + 4y) - 2(2x + y)$
-4x + 8	18w - 3z - 7	15n - 41	17x + 10y
	N		
			-
17. (15 + 8d)(-5) - 24d + d	18. $9(b-1)-c+3b+c$	19. 20f - 4(5f + 4) + 16	20.8(h - 4) - h - (h + 7)
-63d - 75	12b - 9	0	6h - 39
1			
T	1		

Solve each equation, showing all work.

Solve each equation, showing all work.					
21. f - 64 = -23	227 = 2d	23. $\frac{b}{-12} = -6$	24. 13 = m + 21		
f = 41	$d = -\frac{7}{2} = -3.5$	b = 72	m = -8		
25. 5x - 3 = -28	26. $\frac{\omega + 8}{-3} = -9$	27. $-8 + \frac{h}{4} = 13$	28. 22 = 6y + 7		
x = -5	w = 19	h = 84	$y = \frac{5}{2} = 2.5$		
$29. \ 8x - 4 = 3x + 1$	30. $-2(5d - 8) = 20$	31. 7r + 21 = 49r	32. $-9g - 3 = -3(3g + 2)$		
× = 1	$x = -\frac{2}{5} = -0.4$	$r = \frac{1}{2} = 0.5$	no solution		
33. $5(3x - 2) = 5(4x + 1)$	34. $3d - 4 + d = 8d - (-12)$	35. $f - 6 = -2f + 3(f - 2)$	36. $-2(y-1) = 4y - (y+2)$		
x = -3	d = -4	all real numbers	$y = \frac{4}{5} = 0.8$		

Convert each number to Scientific Notation.

38. 0.0009213	39. 0.00000000004	40. 3,201,000,000,000,000
9.213 x 10 ⁻⁴	4 × 10-11	3.201 x 10 ¹⁵
	9.1	N

Convert each number to Standard Form.

41. 5.92 x 10 ⁻⁵	42. I.I x 10 ⁷	43. 6.733 x 10 ⁻⁸	44. 3.27 x 10 ²
0.0000592	11,000,000	0.00000006733	327

Simplify each expression. Write your answers using only positive exponents.

45. ω^{-q} $\frac{1}{\omega^{q}}$	46. $\frac{m^5}{m^2}$	47. f ⁵ ·f ³	$\frac{h^2}{g^3}$ $\frac{h^6}{g^3}$
49. (a ⁵) ²	50. <u>I</u> b ⁻³	51. Z ⁰	52. 4r ⁶ · 3r · 2r ²
alo	b ³	[24r ^q
53. $\frac{q_p-2}{3q-3}$	$\frac{54. 8d^3}{2cd^{-2}}$	55. (g ⁴ h) ² · (2g ³ h ⁻¹) ²	56. (6a)º
53. $\frac{qp^{-2}}{3q^{-3}}$ $\frac{3q^{3}}{p^{2}}$	$\frac{4d^5}{c}$	4g ¹⁴	
57. (-3n ² k ⁴) ²	$\int_{0.5}^{58.} \left(\frac{\omega^5 x^{-2} y}{\omega^2 x y^4} \right)^3$	59. <u>6 · 10</u> 7 2 · 10 ³	60. (1.5 · 10 ⁻⁶) · (4 · 10 ⁹)
9n ⁴ k ⁸	$\frac{\omega^q}{x^q y^q}$	3 · 104	6 · 10 ³

61. (-5, 3), (2, 1)

 $m = -\frac{2}{7}$

62. (8, 4), (11, 6)

 $m = \frac{2}{3}$

63. (9, 3), (9, -1)

m = undefined

64. (-4, -2), (-6, 4)

m = -3

Find the rate of change. Show your work.

65.	Number of Hours	3	6	9	12
	Distance (in miles)	135	270	405	540

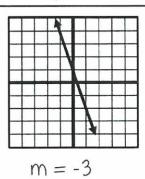
45 miles per hour

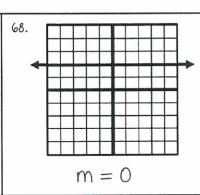
6.	Number of Weeks	ı	3	5	7
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-2 pounds per week

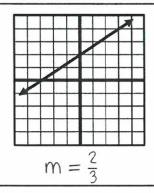
Find the slope of the line.

67.



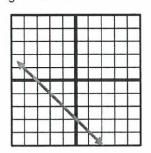


69.

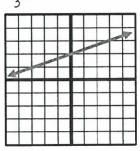


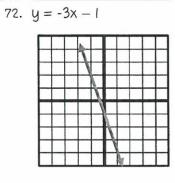
Graph the line.

70. y = -x - 3

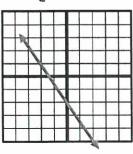


71. $y = \frac{1}{3}x + 2$

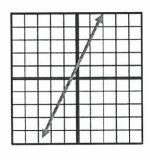


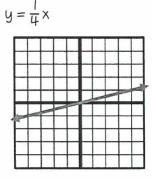


73. $y = -\frac{3}{2}x - 2$



74. y = 2x + 1

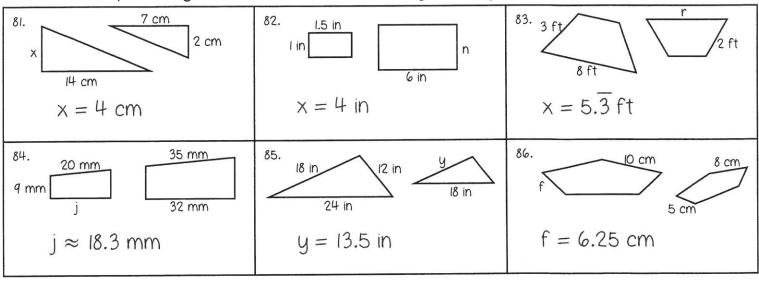




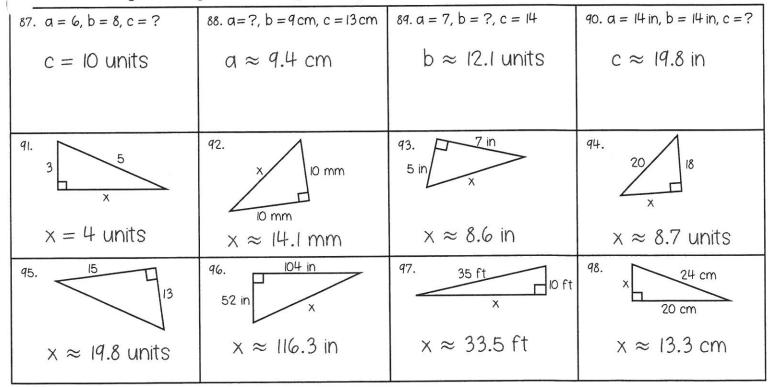
Solve each proportion, showing all work.

$\frac{6}{7} = \frac{4}{m}$	77. $\frac{12}{5} = \frac{k}{3}$	$\frac{h}{7} = \frac{8}{2}$	$\frac{79.}{n} = \frac{9}{36}$	$\frac{80.}{21} = \frac{3}{c}$
m = 4.6	k = 7.2	h = 28	h = 88	h = 15.75

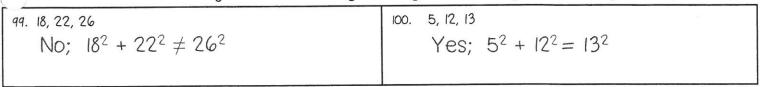
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Find the missing side length in each right triangle to the nearest tenth. Show your work!



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Evaluate each expression for a = 9, b = -3, c = -2, d = 7. Show your work.

1. a - cd	2. $2b^3 + c^2$	3. $\frac{a+d-c}{b}$	4. $(a - b)^2 + d(a + c)$
23	-50	-6	193
5. 4c - (b - a)	6. a/b - 5a	7. 2bc + d(12 - 5)	8. b + 0.5[8 - $(2c + a)$]
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Simplify each expression using the Distributive Property.

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17. (15 + 8d)(-5) - 24d + d	18. $9(b-1)-c+3b+c$	19. 20f - 4(5f + 4) + 16	20. 8(h - 4) - h - (h + 7)
-63d - 75	12b - 9	0	6h - 39

Solve each equation, showing all work.

	Solve each equation, showing all work.						
	21. f - 64 = -23	227 = 2d	23. $\frac{b}{-12} = -6$	24. 13 = m + 21			
	f = 41	$d = -\frac{7}{2} = -3.5$	b = 72	m = -8			
	25. 5x - 3 = -28	w + 8	h	28. 22 = 6y + 7			
		26. $\frac{\omega + 8}{-3} = -9$	$278 + \frac{h}{4} = 13$	5			
	x = -5	w = 19	h = 84	$y = \frac{5}{2} = 2.5$			
		5					
	29. 8x - 4 = 3x + 1	30. $-2(5d - 8) = 20$	31. 7r + 21 = 49r	32. $-9g - 3 = -3(3g + 2)$			
	x = 1	$x = -\frac{2}{5} = -0.4$	r = 1/2 = 0.5	no solution			
			i i				
\mid	33. $5(3x - 2) = 5(4x + 1)$	34. $3d - 4 + d = 8d - (-12)$	35. $f - 6 = -2f + 3(f - 2)$	36. $-2(y-1) = 4y - (y+2)$			
	x = -3	d = -4	all real numbers	$y = \frac{4}{5} = 0.8$			
				~ ~			

Convert each number to Scientific Notation.

37. 67,000,000,000	38. 0.0009213	39. 0.00000000004	40. 3,201,000,000,000,000
6.7 × 10 ¹⁰	9.213 × 10 ⁻⁴	4 × 10-11	3.201 × 10 ¹⁵

Convert each number to Standard Form.

41. 5.92 x 10 ⁻⁵	42. 1.1 × 10 ⁷	43. 6.733 x 10 ⁻⁸	44. 3.27 x 10 ²
0.0000592	11,000,000	0.00000006733	327

Simplify each expression. Write your answers using only positive exponents.

45. ω^{-q} $\frac{1}{\omega^{q}}$	46. $\frac{m^5}{m^2}$	47. f ⁵ ·f ³	$\frac{h^{8}}{g^{3}} \left(\frac{h^{2}}{g}\right)^{3}$ $\frac{h^{6}}{g^{3}}$
49. (a ⁵) ²	50. <u>l</u> b-3	51. Z ⁰	52. 4r ⁶ · 3r · 2r ²
a _{io}	b ³	[24r ⁹
53. $\frac{q_p-2}{3q-3}$	54. $\frac{8d^3}{2cd^{-2}}$	55. (g ⁴ h) ² · (2g ³ h ⁻¹) ²	56. (6a) ⁰
$\frac{3q^3}{p^2}$	$\frac{4d^5}{c}$	4g ¹⁴	
57. (-3n ² k ⁴) ²	$\int_{0.5}^{58.} \left(\frac{\omega^5 x^{-2} y}{\omega^2 x y^4} \right)^3$	59. <u>6 · 10</u> ⁷ 2 · 10 ³	60. (1.5 · 10 ⁻⁶) · (4 · 10 ⁹)
9n ⁴ k ⁸	$\frac{\omega^q}{x^q y^q}$	3 · 104	6 · 10 ³

Find the slope of the line that passes through the points. Show your work.

61. (-5, 3), (2, 1)

 $m = -\frac{2}{7}$

62. (8, 4), (11, 6)

 $m = \frac{2}{3}$

63. (9, 3), (9, -1)

m = undefined

64. (-4, -2), (-6, 4)

m = -3

Find the rate of change. Show your work.

65.

Number of Hours	3	6	9	12
Distance (in miles)	135	270	405	540

45 miles per hour

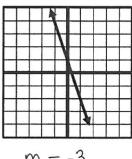
66.

Number of Weeks	1	3	5	7
Pounds	173	169	165	161

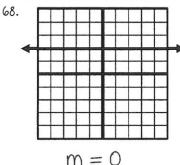
-2 pounds per week

Find the slope of the line.

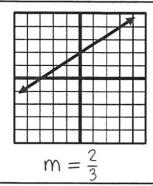
67.



m = -3

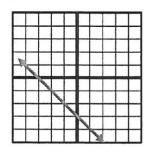


m = 0

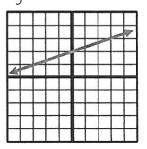


Graph the line.

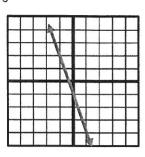
70. y = -x - 3



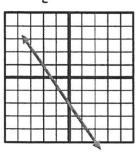
71. $y = \frac{1}{3}x + 2$



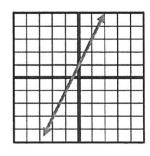
72. y = -3x - 1



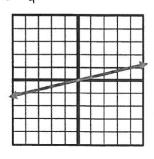
73. $y = -\frac{3}{2}x - 2$



74. y = 2x + 1



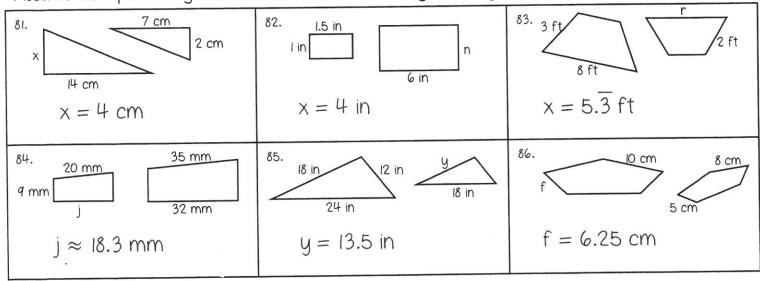
75. $y = \frac{1}{4}x$



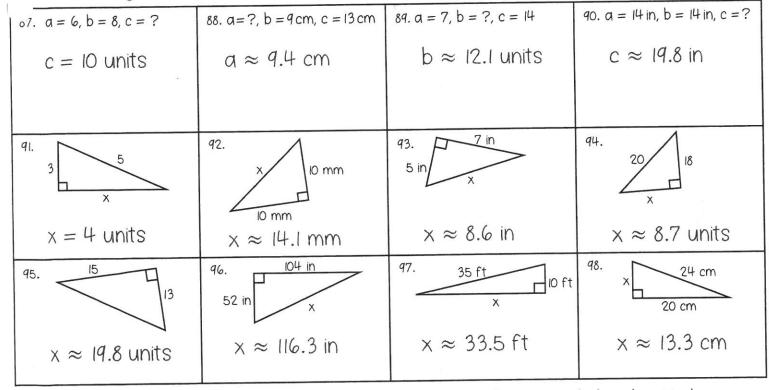
Solve each proportion, showing all work.

$\frac{76.}{7} = \frac{4}{m}$ $m = 4.\overline{6}$	$\frac{77.}{5} = \frac{k}{3}$ $k = 7.2$	$\frac{h}{7} = \frac{8}{2}$ $h = 28$	$\frac{79.}{n} = \frac{9}{36}$ $h = 88$	80. $\frac{4}{21} = \frac{3}{c}$ h = 15.75

Assume each pair of figures is similar. Find the missing side length to the nearest tenth.



Find the missing side length in each right triangle to the nearest tenth. Show your work!



stermine whether or not you can form a right triangle from the given side lengths. Explain.

99. 18, 22, 26No; $18^2 + 22^2 \neq 26^2$ | 100. 5, 12, 13 Yes; $5^2 + 12^2 = 13^2$