

**Multiple Choice Questions**

1.  $\lim_{x \rightarrow \infty} \frac{3 + 2x^2 - x^4}{3x^4 - 5} =$

(A) -2

(B)  $-\frac{1}{3}$ (C)  $\frac{1}{5}$ 

(D) 1

(E) 3

2. What is  $\lim_{x \rightarrow -\infty} \frac{x^3 + x - 8}{2x^3 + 3x - 1} =$

(A)  $-\frac{1}{2}$ 

(B) 0

(C)  $\frac{1}{2}$ 

(D) 2

(E) 4

3. Which of the following lines is an asymptote of the graph of  $f(x) = \frac{x^2 + 5x + 6}{x^2 - x - 12}$ ?

I.  $x = -3$ II.  $x = 4$ III.  $y = 1$ 

(A) II only

(B) III only

(C) I and III only

(D) II and III only

(E) I, II and III

4. If the horizontal line  $y = 1$  is an asymptote for the graph of the function  $f$ , which of the following statements must be true?

(A)  $f(0) = 1$

(B)  $f(x) = 1$  for all  $x$

(C)  $f(1)$  is undefined

(D)  $\lim_{x \rightarrow 1} f(x) = \infty$

(E)  $\lim_{x \rightarrow \infty} f(x) = 1$

5. If  $x = 1$  is the vertical asymptote and  $y = -3$  is the horizontal asymptote for the graph of the function  $f$ , which of the following could be the equation of the curve?

(A)  $f(x) = \frac{-3x^2}{x-1}$

(B)  $f(x) = \frac{-3(x-1)}{x+3}$

(C)  $f(x) = \frac{-3(x^2-1)}{x-1}$

(D)  $f(x) = \frac{-3(x^2-1)}{(x-1)^2}$

(E)  $f(x) = \frac{-3x}{(x-1)^2}$

### Free Response Questions

6. Let  $f(x) = \frac{3x-1}{x^3-8}$ .

- (a) Find the vertical asymptote(s) of  $f$ . Show the work that leads to your answer.
- (b) Find the horizontal asymptote(s) of  $f$ . Show the work that leads to your answer.

7. Let  $f(x) = \frac{\sin x}{x^2 + 2x}$ .

- (a) Find the vertical asymptote(s) of  $f$ . Show the work that leads to your answer.
- (b) Find the horizontal asymptote(s) of  $f$ . Show the work that leads to your answer.

8. If  $\lim_{x \rightarrow 0} \frac{\sqrt{2+ax} - \sqrt{2}}{x} = \sqrt{2}$  what is the value of  $a$ ?