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Things to Know for the Common Core Algebra 1 Regents Exam

ABSOLUTE VALUE	<p>Equations: Separate into 2 equations - one w/the original equation (without absolute value), the other with every term inside the absolute value negated. CHECK all solutions in the original equation. REJECT those that don't work.</p> <p>Ex) Solve for x $2x - 3 + x = 3$</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;"> $2x - 3 + x = 3$ $3x = 6$ $x = 2$ </div> <div style="text-align: center;"> $-2x + 3 + x = 3$ $-x = 0$ $x = 0$ </div> <div style="text-align: center;"> <u>CHECK: $x = 2$</u> $2(2) - 3 + 2 = 3$ $1 + 2 = 3$ $1 + 2 = 3$ ✓ </div> </div> <div style="display: flex; justify-content: space-around; align-items: flex-start; margin-top: 10px;"> <div style="text-align: center;"> $2(0) - 3 + 0 = 3$ $-3 + 0 = 3$ $3 + 0 = 3$ </div> <div style="text-align: center; border: 1px solid black; padding: 5px;"> Answer: {2, 0} </div> </div>
AREA	<p>Square: $A = s^2$ Rectangle: $A = LW$ Triangle: $A = \frac{1}{2}bh$</p> <p>Circle: $A = \pi r^2$ Trapezoid: $A = \frac{1}{2}h(b_1 + b_2)$</p>
CALCULATOR	<p>Key Strokes on Calculator:</p> <p>Absolute Value: MATH → NUM abs(</p> <p>Factorial: MATH → → → PRB !</p> <p>Fractions: to convert a decimal into a fraction MATH → FRAC →</p> <p>Graphing: many graphs can be seen using ZOOM 6: ZOOMSTD If not, adjust window using WINDOW</p>
EXPONENTIAL GROWTH & DECAY	<p>If something is growing at a rate of $r\%$: $C(1 + r)^t$</p> <p>If something is decaying at a rate of $r\%$: $C(1 - r)^t$</p> <p>where... C = current value r = % written as decimal (move 2 places LEFT) t = time</p> <p>Compound Interest: $A = P(1 + \frac{r}{n})^{nt}$</p> <p>where... A = Future Value P = Principal (original value) n = # of compoundings r = % written as decimal (move 2 places LEFT) t = time</p>

FACTORING

Greatest Common Factor: whatever all the terms have in common goes in front of parentheses. What is left after dividing goes inside.

$$Ex) 4a^3 + 6a^2 - 2a = 2a^2(2a + 3a^2 - 1)$$

Difference of Two Squares: There must be two terms separated by subtraction and both must be perfect squares (coefficients perfect & exponents even) $Ex) 25x^6 - 49 = (5x^3 + 7)(5x^3 - 7)$

Trinomial: Looks like... $x^2 + \square x + \triangle$ find two numbers that Multiply to \triangle and Add to \square . $Ex) x^2 - 2x - 24 = (x - 6)(x + 4)$

Perfect Square Trinomials: A trinomial where the number in \triangle is a perfect square and the number in \square is TWICE the square root of that number $ex) x^2 + 10x + 25 = (x + 5)^2$ $ex) x^2 - 16x + 64 = (x - 8)^2$

Factor COMPLETELY: First factor by greatest common factor then factor again by DOTS or Trinomial. Answer looks like: $_ (_) (_)$

FRACTIONS

Undefined: Forget about the numerator. Set the denominator equal to zero and solve for x. $Ex) \frac{3x-1}{x+5}$ is undefined when $x + 5 = 0$ meaning $x = -5$.

Adding/Subtracting: Find a common denominator and then multiply original fractions by what each is "missing". Add/Subtract numerators. Leave denominators alone. $Ex) \frac{x-2}{3} + \frac{x+1}{4} = \frac{4x-8}{12} + \frac{3x+3}{12} = \frac{7x-5}{12}$

Multiplying: Factor first, then cancel diagonally or up/down. Multiply straight across to get final answer.

$$Ex) \frac{x^2-4}{3x+6} \cdot \frac{4}{2x-4} = \frac{(x+2)(x-2)}{3(x+2)} \cdot \frac{4}{2(x-2)} = \frac{4}{3}$$

Dividing: Same as multiplying except FLIP the second fraction first.

Simplifying: Any terms that have "+" or "-" between them must be factored first. Then cancel. $Ex) \frac{x^2-9x+20}{4x-20} = \frac{(x-4)(x-5)}{4(x-5)} = \frac{x-4}{4}$

FUNCTIONS

To determine if something is a function...

Graphs: must pass the "Vertical Line Test" (no vertical line can ever intersect the graph more than once)

Points: All x-values must be DIFFERENT to be a function.

To evaluate a function...

If $f(x)$ is given and we want to find "f(some number)", just substitute the number in place of x on the right side of the equation. $Ex) If f(x) = 2x^2 - 3x + 1$, then $f(5) = 2(5)^2 - 3(5) + 1 = 36$

FUNCTIONS

(continued)

Piecewise Functions: functions that are defined differently for different values of x .

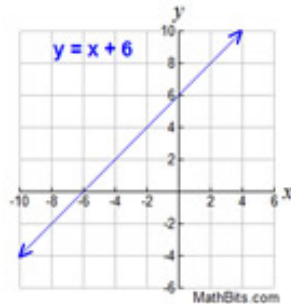
ex) If $f(x) = \begin{cases} 2x + 3, & x < 1 \\ -x + 7, & x \geq 1 \end{cases}$ find $f(2)$.

Since "2" is in the domain $x \geq 1$, we would use the function $-x + 7$

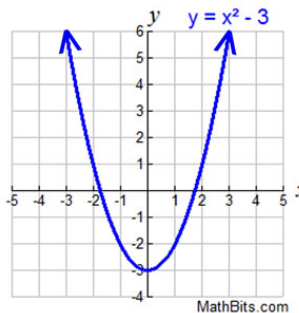
So $f(2) = -(2) + 7 = \boxed{5}$

To graph a piecewise function, graph the given equation ONLY for the values of x given. Make sure the graph satisfies the Vertical Line Test.

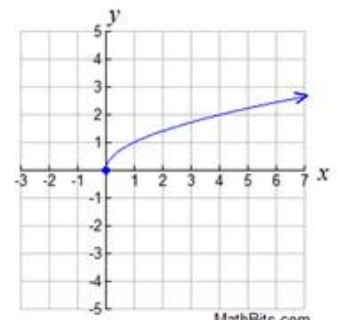
Domain of a Function: All possible x -values for the given function. Look at the graph and see how far left and right the graph goes.



Domain: All Real Numbers
or $(-\infty, \infty)$

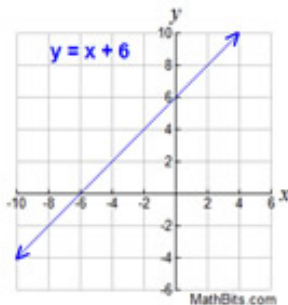


Domain: All Real Numbers
or $(-\infty, \infty)$

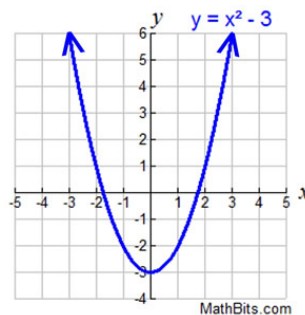


Domain: $x \geq 0$
or $[0, \infty)$

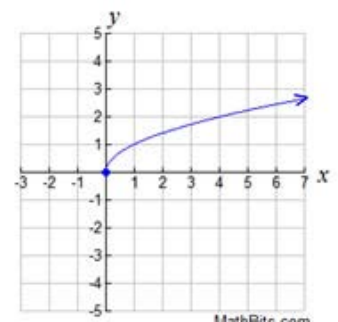
Range of a Function: All possible y -values for the given function. Look at the graph and see how far down and up the graph goes.



Range: All Real Numbers
or $(-\infty, \infty)$



Range: $y \geq -3$
or $[-3, \infty)$



Range: $y \geq 0$
or $[0, \infty)$

GRAPHS

Graphs to Recognize...

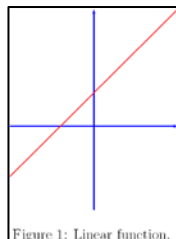


Figure 1: Linear function.
LINEAR
(line)

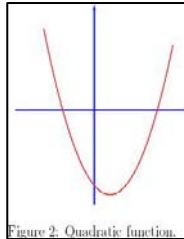
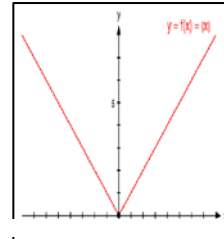
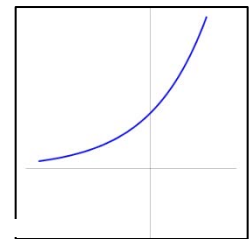


Figure 2: Quadratic function.
QUADRATIC
(u - shaped)



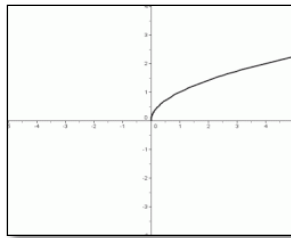
ABS. VALUE
(v - shaped)



EXPONENTIAL
(hockey stick)

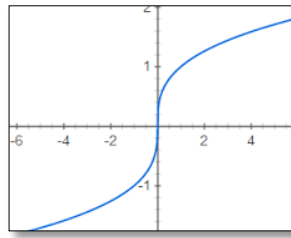
GRAPHS

(continued)



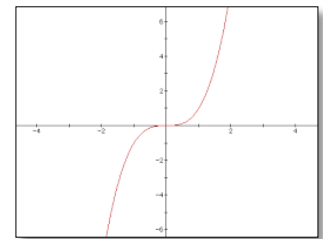
SQUARE ROOT

$$y = \sqrt{x}$$



CUBE ROOT

$$y = \sqrt[3]{x}$$



CUBIC

$$y = x^3$$

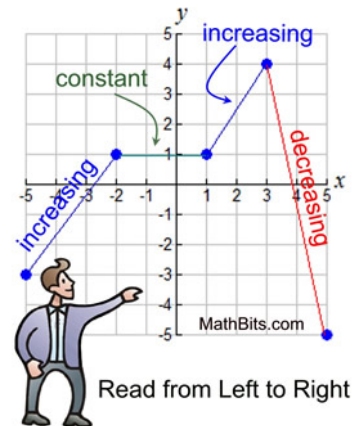
Increasing and Decreasing Intervals:

The function (graph) at the right is increasing from the point $(-5,-3)$ to the point $(-2,1)$, which is described as increasing when $-5 < x < -2$.

Using interval notation, it is described as increasing on the interval $(-5,-2)$.

It also increases from the point $(1,1)$ to the point $(3,4)$, described as increasing when $1 < x < 3$.

Using interval notation, it is described as increasing on the interval $(1,3)$.



The graph shown above is decreasing from the point $(3,4)$ to the point $(5,-5)$, described as decreasing when $3 < x < 5$.

Using interval notation, it is described as decreasing on the interval $(3,5)$.

Intervals of increasing, decreasing or constant

ALWAYS pertain to x -values.

Do NOT read numbers off the y -axis.

Stay on the x -axis for these intervals!

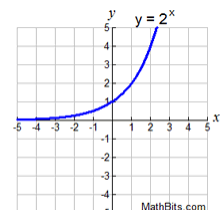
Positive and Negative:

Some functions are positive over their entire domain.

(All y -values above the x -axis.)

positive: $-\infty < x < +\infty$

or "all Reals", or $(-\infty, +\infty)$

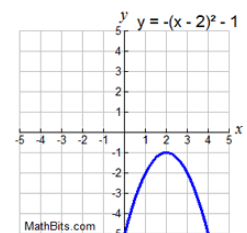


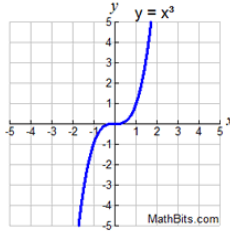
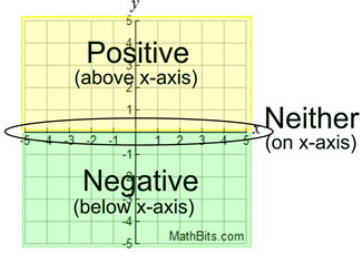
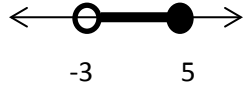
Some functions are negative over their entire domain.

(All y -values below the x -axis.)

negative: $-\infty < x < +\infty$

or "all Reals", or $(-\infty, +\infty)$



<p>GRAPHS (continued)</p>	<p>Some functions have both positive and negative regions. (y-values above and below x-axis)</p> <p>positive: $x > 0$ or $(0, +\infty)$ negative: $x < 0$ or $(-\infty, 0)$ (do not include zero)</p>  
<p>INEQUALITIES</p>	<p>Number lines:</p> <ul style="list-style-type: none"> > shade RIGHT w/open circle < shade LEFT w/open circle \geq shade RIGHT w/closed circle \leq shade LEFT w/closed circle <div style="border: 1px solid black; padding: 5px; width: fit-content;"> <p>REMEMBER: If divide by a negative number, the symbol switches.</p> </div> <p>Both x and y: These get graphed on xy-plane as lines (dotted or solid) and then a region gets shaded. (If vertical line, follow above rules)</p> <ul style="list-style-type: none"> > dotted line/shade UP < dotted line/shade DOWN \geq solid line/shade UP \leq solid line/shade DOWN
<p>INTERVAL NOTATION</p>	<p>Parentheses: means UNEQUAL (use open circles) Brackets: means EQUAL (use closed circles)</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin-left: auto;"> <p>SHADE in between the 2 numbers on a # Line</p> </div> <p>Ex) Inequality notation: $-3 < x \leq 5$ interval notation: $(-3, 5]$</p> 
<p>LINES</p>	<p>Equation of a Line: $y = mx + b$ where m = slope and b = y-intercept</p> <p>If Vertical line: $x = a$ number (slope is undefined) \updownarrow</p> <p>If Horizontal line: $y = a$ number (slope is zero) \leftrightarrow</p> <p>Slope of a Line: (using 2 points on the line)</p> <p>Parallel lines have <u>equal</u> slopes.</p> <p>Perpendicular Lines have <u>negative reciprocal</u> slopes.</p> <p>A positive slope looks like... \swarrow A negative slope looks like... \searrow</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin-left: auto;"> $m = \frac{y_2 - y_1}{x_2 - x_1}$ </div> <p>To write the equation of a line:</p> <p><u>Step 1:</u> Find slope (m).</p> <p><u>Step 2:</u> Find y- intercept (b) by plugging a point in for (x, y) and slope in for "m" into "$y = mx + b$" to solve for "b".</p> <p>Ex) Write the equation of a line perpendicular to $y = 2x + 7$ that passes through the point $(-6, 4)$.</p> <p><u>Step 1:</u> since the slope of $y = 2x + 7$ is "2", the slope of a perp. line would be $m = -\frac{1}{2}$.</p> <p><u>Step 2:</u></p> <div style="display: flex; align-items: center; gap: 20px;"> <div style="border: 1px solid black; padding: 5px;"> $m = -\frac{1}{2}$ $x = -6$ $y = 4$ </div> <div style="font-size: 2em;">→</div> <div style="display: flex; flex-direction: column; gap: 5px;"> $y = mx + b$ $4 = (-\frac{1}{2})(-6) + b$ $4 = 3 + b$ $1 = b$ </div> <div style="font-size: 2em;">→</div> <div style="border: 1px solid black; padding: 5px;"> $y = -\frac{1}{2}x + 1$ </div> </div>

NUMBERS

& their Properties

Types of Numbers :

1. Integers: a whole number that can be positive, negative, or zero.
2. Rational: any number that can be written as a fraction
(when written as a decimal it either ENDS or REPEATS)
3. Irrational: a number that cannot be written as a fractions
(the decimal NEVER ends and NEVER repeats)

Properties of Numbers:

1. Commutative: when the numbers/variables change order
Ex) $3 + 4 = 4 + 3$ or $a \cdot b = b \cdot a$
2. Associative: when the parentheses change what is inside them
Ex) $3 + (4 + 5) = (3 + 4) + 5$ or $a \cdot (b \cdot c) = (a \cdot b) \cdot c$
3. Distributive: the number outside () multiplies each term inside
Ex) $3(4 + 5) = 3(4) + 3(5)$
4. Identity: for Addition, can add "0" and not change the number
for Multiplication, can mult by "1" and not change number
Ex) $3 + 0 = 3$ or $3 \cdot 1 = 3$
5. Inverse: for Addition, can add two numbers to get an answer of 0.
for Multiplication, can multiply to get an answer of 1.
Ex) $3 + (-3) = 0$ or $3 \cdot \frac{1}{3} = 1$
6. Zero Property: anything multiplied by 0 is 0 Ex) $3 \cdot 0 = 0$

PARABOLAS

Equation of a Parabola: $y = ax^2 + bx + c$

If "a" is positive, graph looks like...
The Vertex is a MINIMUM point



If "a" is negative, then
The Vertex is a MAXIMUM point



Axis of Symmetry: (the vertical line that passes through vertex)

* This value of x should be in the middle of the table*

$$x = \frac{-b}{2a}$$

Vertex: First find the axis of symmetry using the formula above, then plug that x-value into the parabola's equation to find "y". Vertex = (x, y)

Ex) Find the coordinates of the vertex of the parabola: $y = x^2 - 6x + 4$

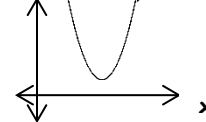
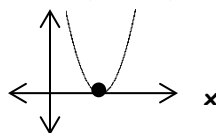
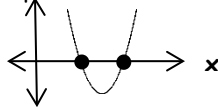
$$\text{Axis of Symmetry: } a = 1, b = -6, c = 4 \rightarrow x = \frac{-(-6)}{2(1)} = 3$$

$$\text{Vertex: } y = (3)^2 - 6(3) + 4 \rightarrow y = -5 \quad \text{VERTEX: } (3, -5)$$

(*For vertex form of a Parabola - see "Quadratic Equations" on page 7*)

Roots: The values of x where the graph intersects the x-axis (y = 0)

A parabola can have either: 2 roots, 1 root, or no roots. See diagrams below.



To find the roots algebraically, set equation equal to zero and FACTOR. Set each factor equal to zero and solve for x.

<p>PERCENTS</p>	<p>Percent Problems: set up this proportion and cross-multiply to solve</p> $\frac{\text{part}}{\text{whole}} = \frac{\%}{100} \quad \text{or} \quad \frac{\text{is}}{\text{of}} = \frac{\%}{100}$ <p>In sales tax problems, whole = original and % is 100 + sales tax</p> <p>Percent Error:</p> $\frac{ \text{Measured} - \text{Actual} }{\text{Actual}} \cdot 100$ <p>If it says relative error, don't multiply by 100</p> <p>Percent Increase/Decrease: $\frac{ \text{Original} - \text{New} }{\text{Original}} \cdot 100$</p>													
<p>PERIMETER</p>	<p>Square: $P = 4s$ Rectangle: $P = 2L + 2W$ Circle: $C = \pi d$ or $2\pi r$</p> <p>All other shapes: add all the sides</p>													
<p>POLYNOMIALS</p>	<p>Exponent Rules: The coefficients always perform the operation in the problem, the exponents never do.</p> <table border="1" data-bbox="487 672 760 814"> <tr><td>Multiplying Problems:</td></tr> <tr><td>Coefficients Multiply</td></tr> <tr><td>Exponents ADD</td></tr> <tr><td>Ex) $6x^6 \cdot 2x^2 = 12x^8$</td></tr> </table> <table border="1" data-bbox="815 672 1052 814"> <tr><td>Dividing Problems:</td></tr> <tr><td>Coefficients Divide</td></tr> <tr><td>Exponents SUBTRACT</td></tr> <tr><td>Ex) $6x^6 \div 2x^2 = 3x^4$</td></tr> </table> <table border="1" data-bbox="1101 672 1416 856"> <tr><td>Adding/Subtracting Problems:</td></tr> <tr><td>Coefficients Add/Subtract</td></tr> <tr><td>Exponents STAY THE SAME</td></tr> <tr><td>Ex) $6x^6 + 2x^6 = 8x^6$</td></tr> <tr><td>Ex) $6x^6 + 2x^2 = 6x^6 + 2x^2$</td></tr> </table> <p>Zero and Negative Exponents:</p> $x^0 = 1$ $x^{-n} = \frac{1}{x^n}$ $\frac{1}{x^{-n}} = x^n$ <p>Notice the Difference: $-3^2 \neq (-3)^2$ because $-3^2 = -9$ yet $(-3)^2 = +9$</p> <p>Adding/Subtracting Polynomials: Only combine the "LIKE TERMS" (same variable and same exponent) Ex) $9x^3 + 7y^3 - x^3 - 6x^2 + 4y^3 = 8x^3 + 13y^3 - 6x^2$</p> <p>"Subtract/From" Problems: The "from" expression goes first followed by a subtraction symbol and then the "subtract" expression in parentheses</p> <p>Ex) Subtract $2x^2 + 3x - 1$ from $x^2 - 5x - 7$</p> $= (x^2 - 5x - 7) - (2x^2 + 3x - 1) = x^2 - 5x - 7 - 2x^2 - 3x + 1$ $= -x^2 - 8x - 6$ <p>Multiplying Polynomials: Each term in the first () multiplies each term in the 2nd (). To mult binomial by binomial use FOIL (first, outer, inner, last)</p> <p>Ex) Find the product of $3x - 4$ and $x + 5$.</p> $= (3x - 4)(x + 5) = 3x^2 + 15x - 4x - 20 = 3x^2 + 11x - 20$	Multiplying Problems:	Coefficients Multiply	Exponents ADD	Ex) $6x^6 \cdot 2x^2 = 12x^8$	Dividing Problems:	Coefficients Divide	Exponents SUBTRACT	Ex) $6x^6 \div 2x^2 = 3x^4$	Adding/Subtracting Problems:	Coefficients Add/Subtract	Exponents STAY THE SAME	Ex) $6x^6 + 2x^6 = 8x^6$	Ex) $6x^6 + 2x^2 = 6x^6 + 2x^2$
Multiplying Problems:														
Coefficients Multiply														
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Dividing Problems:														
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Exponents STAY THE SAME														
Ex) $6x^6 + 2x^6 = 8x^6$														
Ex) $6x^6 + 2x^2 = 6x^6 + 2x^2$														
<p>PROPORTION</p>	<p>Proportion: when two fractions (ratios) are equal to one another</p> <p>If $\frac{a}{b} = \frac{c}{d}$ $\xrightarrow[\text{multiply}]{\text{cross}}$ $a \cdot d = b \cdot c$</p> <p>Direct Variation:</p> <p>If x varies directly as y, then: $\frac{x}{y} = \frac{x}{y}$</p> <p>Ex) If x varies directly as y and $x = 4$ when $y = 6$, find y when $x = 10$.</p> $\frac{4}{6} = \frac{10}{y}$ $4 \cdot y = 6 \cdot 10$ $y = 15$													

QUADRATIC EQUATIONS

Quadratic Equation: an equation that has x^2 in it. There are 3 ways to solve a quadratic equation.

TO SOLVE BY FACTORING

Step 1: Get one side equal to ZERO (try to get x^2 to the side where it's positive)

Step 2: FACTOR (by GCF, DOTs, or TRInomial)

Step 3: Set each factor equal to zero and solve for x.


TO SOLVE USING QUADRATIC FORMULA

Step 1: Get one side equal to ZERO

Step 2: Determine "a", "b", "c" then use the formula below

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

TO SOLVE BY COMPLETING THE SQUARE:

Step 1: Divide by the number in front of x^2 . Step 2: Keep all terms with x on the left and move constant to right side of =. Step 3: Set up a place 

holder on each side to fill in with the missing number $\left(\frac{b}{2}\right)^2$. Step 4:

Rewrite the left side as $\left(x + \frac{b}{2}\right)^2$. Step 5: Square root both sides - this will get rid of the "squared" on left side. **Include a "+" on right side.** Step 6: Get x alone and simplify if possible.

Ex) Solve by completing the square: $2x^2 - 6x - 7 = 0$

$$x^2 - 3x - \frac{7}{2} = 0 \quad (\text{Divide by 2})$$

$$x^2 - 3x = \frac{7}{2} \quad (\text{Move constant})$$

$$x^2 - 3x + \heartsuit = \frac{7}{2} + \heartsuit \quad (\text{place holder})$$

$$x^2 - 3x + \frac{9}{4} = \frac{7}{2} + \frac{9}{4} \quad (b = -3 \rightarrow \left(\frac{-3}{2}\right)^2 = +\frac{9}{4})$$

$$\left(x - \frac{3}{2}\right)^2 = \frac{7}{2} + \frac{9}{4} \quad (\text{left side is perfect square})$$

$$\left(x - \frac{3}{2}\right)^2 = \frac{23}{4} \quad (\text{simplify})$$

$$\sqrt{\left(x - \frac{3}{2}\right)^2} = \pm \sqrt{\frac{23}{4}} \quad (\text{square root- don't forget } \pm \text{ on right})$$

$$x - \frac{3}{2} = \pm \sqrt{\frac{23}{4}} \quad (\text{drop the squared on left})$$

$$x = \frac{3}{2} \pm \sqrt{\frac{23}{4}} = \frac{3}{2} \pm \frac{\sqrt{23}}{2} \text{ or } \frac{3 \pm \sqrt{23}}{2}$$

Every quadratic equation has two solutions. The graph of a quadratic equation is a parabola and the solutions represent its ROOTS.

Ex) Solve: $x^2 - 2x = 2x^2 + 3x - 6$

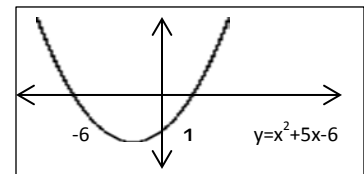
$$\frac{-x^2 + 2x}{0} = \frac{-x^2 + 2x}{0} + 6$$

$$0 = x^2 + 5x - 6$$

$$0 = (x + 6)(x - 1)$$

$$x + 6 = 0 \quad | \quad x - 1 = 0$$

$$x = -6 \quad | \quad x = 1$$



QUADRATIC EQUATIONS

(continued)

Nature (Type) of Roots: to determine the type of roots a quadratic eqn. has (without actually finding them), use the **Discriminant** = $b^2 - 4ac$

Discriminant $b^2 - 4ac$ is...	Roots would be...
NEGATIVE	Imaginary
ZERO	Equal (Real, Rational, & Equal)
POSITIVE PERFECT SQUARE	Rational & Unequal (Real, Rational, & Unequal)
POSITIVE but NOT a PERFECT SQUARE	Irrational (Real, Irrational, & Unequal)

Vertex Form of a Parabola: $y = a(x - h)^2 + k$

where vertex = (h, k)

NOTE: If equation is NOT in this form, complete the square

Range of Quadratics Using Vertex Form:

Identify the vertex from the equation, identify whether the vertex is a minimum or maximum point and write an inequality of the range.

Ex) Identify the range of the function $g(x) = 5(x - 2)^2 - 7$

The vertex is (2, -7). It is a minimum because the leading coefficient is positive. -7 is the lowest y-value so, the range is $y \geq -7$ or written in interval notation $[-7, \infty)$

Ex) Identify the range of the function $f(x) = -2(x + 4)^2 + 6$

The vertex is (-4, 6). It is a maximum because the leading coefficient is negative. 6 is the highest y-value so, the range is $y \leq 6$ or written in interval notation $(-\infty, 6]$

RADICALS

Perfect Squares: 1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169...

Simplifying Radicals: find two numbers that multiply to the number under the radical where one number must be a *perfect square*. (If there is a coefficient, it will multiply) Ex) $7\sqrt{54} = 7\sqrt{9}\sqrt{6} = 7 \cdot 3\sqrt{6} = 21\sqrt{6}$

Adding/Subtracting: Two radicals must have the SAME number under the radical. If so, add/subtract coefficients and leave common radical alone. Ex) $\sqrt{27} - 5\sqrt{12} = \sqrt{9}\sqrt{3} - 5\sqrt{4}\sqrt{3} = 3\sqrt{3} - 5 \cdot 2\sqrt{3} = -7\sqrt{3}$

Multiplying/Dividing: Any two radicals can mult/divide (do not have to be the same). Mult/divide the coefficients and mult/divide the radicands.

Ex) Multiply and express result in simplest radical form:

$$9\sqrt{6} \cdot 7\sqrt{3} = 63\sqrt{18} = 63\sqrt{9}\sqrt{2} = 63 \cdot 3\sqrt{2} = 189\sqrt{2}$$

Ex) Divide: $\frac{6\sqrt{32}}{2\sqrt{2}} = 3\sqrt{16} = 3 \cdot 4 = 12$

SEQUENCES

Arithmetic Sequence: when the pattern is ADDING.

- d = difference b/w terms
- a₁ = first term
- n = number of term asked for

To find the nth ARITHMETIC term:

$$a_n = a_1 + (n - 1)d$$

Ex) Find the 100th term of: 3, 7, 11, 15, 19, ...

Here: n = 100, a₁ = 3, d = 4 ⇒ a₁₀₀ = 3 + (100-1)(4) = 399

Geometric Sequence: when the pattern is MULTIPLYING.

- r = ratio b/w terms (if not obvious - divide any term by the previous one)
- a₁ = first term
- n = number of term asked for

To find the nth GEOMETRIC term:

$$a_n = a_1(r)^{n - 1}$$

Ex) Find the 7th term of: 6, 4, $\frac{8}{3}$, $\frac{16}{9}$, ...

Here: n = 7, a₁ = 6, r = 2/3 ⇒ a₇ = 6($\frac{2}{3}$)⁷⁻¹ = $\frac{128}{243}$

Recursive Sequences: a term is found by knowing the term before it
 The first term "a₁" will be given along with a formula to find "a_n" given "a_{n-1}"

Ex) If a₁ = 2 and a_n = 5a_{n-1} + 3, find the first 4 terms.

Need to find a₁, a₂, a₃, and a₄

- a₁ = 2
- a₂ = plug in n to be 2 = 5a₂₋₁ + 3 = 5a₁ + 3 = 5(2) + 3 = 13
- a₃ = plug in n to be 3 = 5a₃₋₁ + 3 = 5a₂ + 3 = 5(13) + 3 = 68
- a₄ = plug in n to be 4 = 5a₄₋₁ + 3 = 5a₃ + 3 = 5(68) + 3 = 343

2, 13, 68, 343

SETS

U = UNION = combine the sets together (put in order, don't repeat)

∩ = INTERSECTION = what both sets have in common (if nothing, write ∅)

\bar{A} = COMPLEMENT of SET A = everything that set A is missing from the Universe "U"

Ex) If U = {1, 2, 3, 4, 5, 6}

A = {2, 5}

B = {3, 5, 6}

Then A ∪ B = {2, 3, 5, 6}

A ∩ B = { 5 }

\bar{B} = {1, 2, 4}

SPEED

Formula:

$$d = rt$$

where...

d = distance (possible units = miles)

r = rate (possible units = $\frac{\text{miles}}{\text{hour}}$)

t = time (possible units = hours)

"r and t" vary inversely

STATISTICS

Mean: the average

To find the Mean: add all the numbers that divide by how many ("n").

To find missing data: Use the fact that $(\text{Mean}) \cdot (n) = \text{SUM}$

To find the missing number, see what's missing to get this sum.

Ex) 78, 92, 85, 97, ? Find ? if mean is 90.

$$(90) \cdot (5) = 450 = \text{SUM (of all 5 numbers)}$$

$$78 + 92 + 85 + 97 = 352 \text{ (so far, of the 4 known numbers)}$$

$$450 - 352 = 98$$

Median: the middle number (once the data is arranged in order). If there are two numbers in the middle, find the average of them.

Mode: the number that appears MOST often

(there can be no mode or even more than 1 mode)

Range: HIGHEST - LOWEST

Outlier: any number that is far away from the rest. When there are outliers, the MEDIAN best represents the data.

Quantitative vs. Qualitative: QUANTITATIVE = data is numbers
QUALITATIVE = data isn't numbers

Univariate vs. Bivariate: UNI = one set of #'s; BI = two sets of #'s

Causal Relationship: where one thing actually causes the other.

Correlation: three types
POSITIVE - as one increases, so does the other
NEGATIVE - as one increases, the other decreases
NONE - scatter plot does NOT look like a line

Stem and Leaf Plot: the first digit(s) go in front of the line, the last digit goes after the line. DON'T FORGET A KEY!

Ex) If data were: 83, 88, 88, 92, 100 then plot would look like...

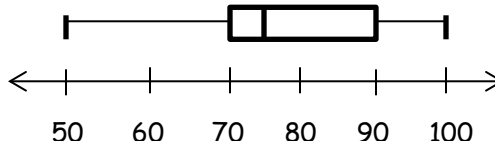
8		3 8 8
9		2
10		0

Key: 9 | 2 = 92

Box and Whiskers Plot: Include an equally spaced number line on Bottom then show MIN, Q1, Q2 (same as median), Q3, and MAX.

(see calculator instructions below)

Ex) If MIN = 50, Q1 = 70, Q2 = 75, Q3 = 90, MAX = 100 plot looks like



Note: between any 2 of these scores 25% of data lie

STATISTICS

(continued)

Mean, Median, Range, & Standard Deviation on Calculator:

Step 1: Enter all data under L_1 and frequencies (if there are any) under L_2 using **STAT** **EDIT**

Step 2: Calculate these measures of central tendency and dispersion by

STAT **CALC** **1 - VAR STATS** L_1 , L_2 (only if frequencies)

Mean: \bar{X}

Median: Med

Range: $\max X - \min X$

Interquartile Range: $Q_3 - Q_1$

Standard Deviation: σ_x (if it is a population)

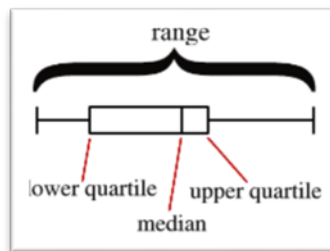
s_x (if it is a sample)

To create a Box and Whiskers Plot on Calculator:

Find the 5 calculations (MIN, Q1, MED, Q3, MAX) using steps 1 and 2 above. To create plot: **2nd** **STATPLOT** **PLOT 1**

Choose: **ON**

Type: choose the 5th graph, then graph by hitting **ZOOM** **ZOOMSTAT**



Regressions: used to find the equation of the line of "best fit" given data

Step 1: Enter data **STAT** **EDIT**

Step 2: Create the scatterplot (Make sure x's are in L_1 and y's are in L_2)

2nd **STATPLOT** **PLOT 1** Choose: **ON**

For type choose 1st graph

Step 3: Graph **ZOOM** **ZOOMSTAT**

Step 4: To write the equation of the line

STAT **→** **CALC** **LinReg (ax + b)** **ENTER**

Note that "a" is the slope (m)
and b is the y-intercept

Residuals: Residuals help to determine if a curve (shape) is appropriate for the data. (linear versus non-linear)

A residual plot is a scatter plot that shows the residuals on the vertical axis and the independent variable on the horizontal axis. The plot will help you to decide on whether a linear model is appropriate for your data.

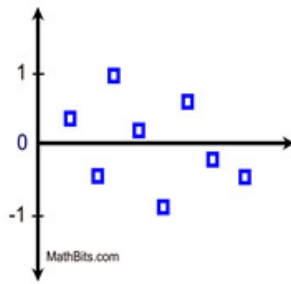
STATISTICS

(continued)

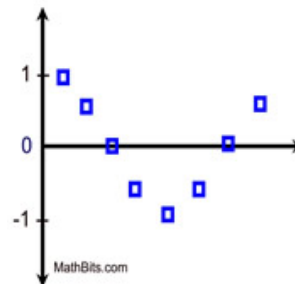
Appropriate linear model:

when plots are randomly placed, above and below x -axis ($y = 0$)

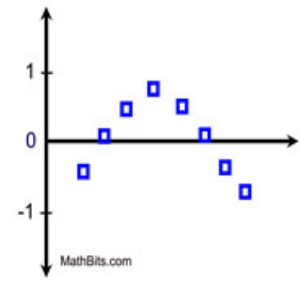
Appropriate non-linear model: when plots follow a pattern, resembling a curve



Random, No Pattern
"Linear Appropriate"



U-shaped Pattern
"Non-Linear Appropriate"



Inverted U-shaped Pattern
"Non-Linear Appropriate"

SYSTEMS

of Equations (=)
or Inequalities (<)

Two Inequalities: Graph lines on xy -plane then shade according to rules listed under "INEQUALITIES". The solution set is the region on the graph that was shaded by both inequalities. Label it "S".

Two Equations: Three ways to solve...

Graphically: graph each equation and find the point(s) of intersection
It could be a parabola and a line (if there's x^2) or two lines (if no x^2)

Algebraically using SUBSTITUTION: used when the system is Quadratic/Linear (one equation has x^2) or whenever one equations has either x or y alone. Substitute whatever it is equal to into the other equation, then solve. Remember to find both x and y .

Algebraically using ELIMINATION: (not used in Quadratic/Linear)
Multiply each equation by a number that will get the coefficients of either x or y to be the **same number but with opposite signs**. Then add the two equations and one variable will cancel. Remember to find both x and y .

Ex) The algebraic method that would work best on each example is...

$$\begin{array}{l} 2x + 3y = 5 \\ x = 4y + 8 \end{array}$$

use Substitution
since x is alone

$$\begin{array}{l} y = x^2 + 2x - 3 \\ 3y - 2x = 5 \end{array}$$

use Substitution
since Quadratic

$$\begin{array}{l} 7(2x + 3y = 5) \\ -3(5x + 7y = 10) \end{array}$$

use Elimination
to get y to cancel

WORD PROBLEMS

Always start with a "Let" statement that states what x represents.

Consecutive Integer Problems: *Consecutive* *Consecutive Even / Odd*

$$\begin{aligned} \text{Let } x &= 1^{\text{st}} \\ x + 1 &= 2^{\text{nd}} \\ x + 2 &= 3^{\text{rd}} \end{aligned}$$

$$\begin{aligned} \text{Let } x &= 1^{\text{st}} \\ x + 2 &= 2^{\text{nd}} \\ x + 4 &= 3^{\text{rd}} \end{aligned}$$

Deciding "who" is x : whenever two quantities are compared to one another, the one at the END OF THE SENTENCE is " x ".

Ex) The larger of two numbers is 3 less than twice the smaller. If their sum is 27, find each number.

$x = \text{smaller \#}$ $2x - 3 = \text{larger \#}$	$\text{SUM} = 27$ $x + (2x - 3) = 27$ $3x - 3 = 27$ $3x = 30$ $x = 10$	$10 = \text{smaller \#}$ $2(10) - 3 = 17 = \text{larger \#}$
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Ex) The width of a rectangle is 4 more than the length. If the perimeter is 36 cm., find the dimensions of the rectangle.

$x = \text{length}$ $x + 4 = \text{width}$	$\text{PERIMETER} = 36$ $2L + 2W = 36$ $2(x) + 2(x + 4) = 36$ $2x + 2x + 8 = 36$	$4x + 8 = 36$ $4x = 28$ $x = 7$ $7 = \text{length}; 11 = \text{width}$
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