

Junior School Calculation Policy

Concrete Pictorial Abstract Approach

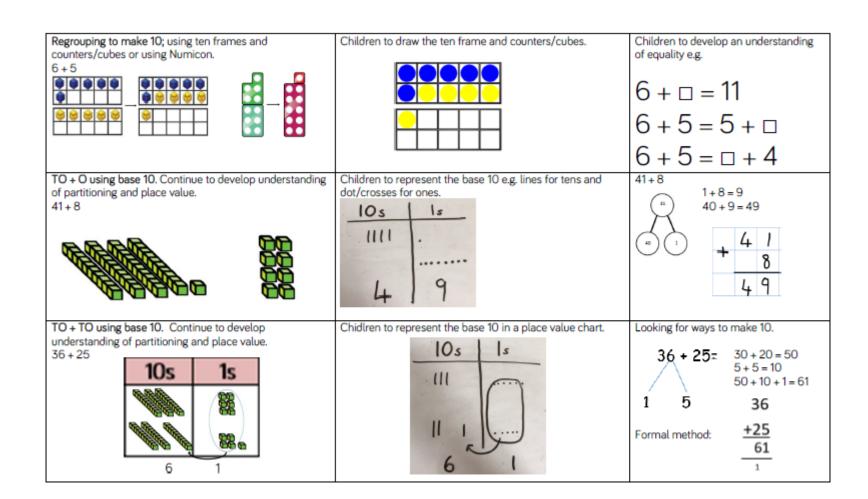
The Concrete Pictorial Abstract (CPA) approach is a system of learning that uses physical and visual aids to build a child's understanding of abstract topics. Pupils are introduced to a new mathematical concept through the use of concrete resources online. When they are comfortable solving problems with physical aids, they are given problems with pictures – usually pictorial representations of the concrete objects they were using. Then, they are asked to solve problems where they only have the abstract i.e. numbers or other symbols. Building these steps across a lesson can help pupils better understand the relationship between numbers and the real world, and therefore helps secure their understanding of the mathematical concept they are learning.

	Year 3	Year 4	Year 5	Year 6
Addition	Column method- regrouping. Using place value counters (up to 3 digits).	Column method- regrouping. (up to 4 digits)	Column method- regrouping. Use of place value counters for adding decimals.	Column method- regrouping. Abstract methods. Place value counters to be used for adding decimal numbers.
Subtraction	Column method with regrouping. (up to 3 digits using place value counters)	Column method with regrouping. (up to 4 digits)	Column method with regrouping. Abstract for whole numbers. Start with place value counters for decimals- with the same amount of decimal places.	Column method with regrouping. Abstract methods. Place value counters for decimalswith different amounts of decimal places
Multiplication	Arrays 2d × 1d using base 10	Column multiplication- introduced with place value counters. (2 and 3 digit multiplied by 1 digit)	Column multiplication Abstract only but might need a repeat of year 4 first(up to 4 digit numbers multiplied by 1 or 2 digits)	Column multiplication Abstract methods (multi-digit up to 4 digits by a 2 digit number)
Division	Division with a remainder-using lollipop sticks, times tables facts and repeated subtraction. 2d divided by 1d using base 10 or place value counters	Division with a remainder Short division (up to 3 digits by 1 digit- concrete and pictorial)	Short division (up to 4 digits by a 1 digit number including remainders)	Short division Long division with place value counters (up to 4 digits by a 2 digit number) Children should exchange into the tenths and hundredths column too

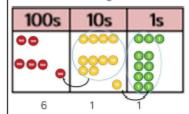
Calculation policy: Addition

Key language: sum, total, parts and wholes, plus, add, altogether, more, 'is equal to' 'is the same as'.

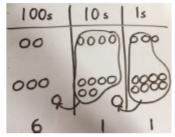
Concrete	Pictorial	Abstract
Combining two parts to make a whole (use other resources too e.g. eggs, shells, teddy bears, cars).	Children to represent the cubes using dots or crosses. They could put each part on a part whole model too.	4+3=7 Four is a part, 3 is a part and the whole is seven.
Counting on using number lines using cubes or Numicon.	A bar model which encourages the children to count on, rather than count all.	The abstract number line: What is 2 more than 4? What is the sum of 2 and 4? What is the total of 4 and 2? 4+2



Use of place value counters to add HTO + TO, HTO + HTO etc. When there are 10 ones in the 1s column- we exchange for 1 ten, when there are 10 tens in the 10s column- we exchange for 1 hundred.



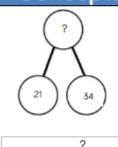
Chidren to represent the counters in a place value chart, circling when they make an exchange.



243

+368 611

Conceptual variation; different ways to ask children to solve 21 + 34



? 21 34

Word problems:

In year 3, there are 21 children and in year 4, there are 34 children. How many children in total?

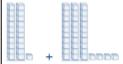
21 + 34 = 55. Prove it



____ 21 + 34 =



Calculate the sum of twenty-one and thirty-four.



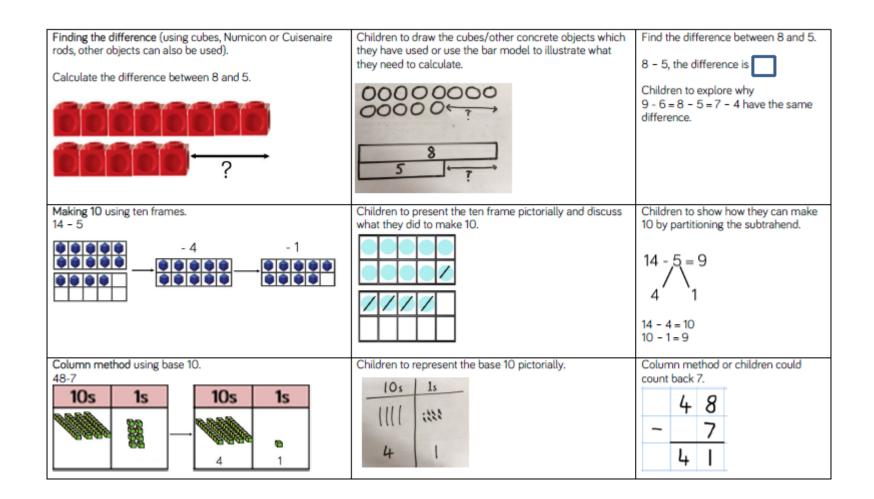
Missing digit problems:

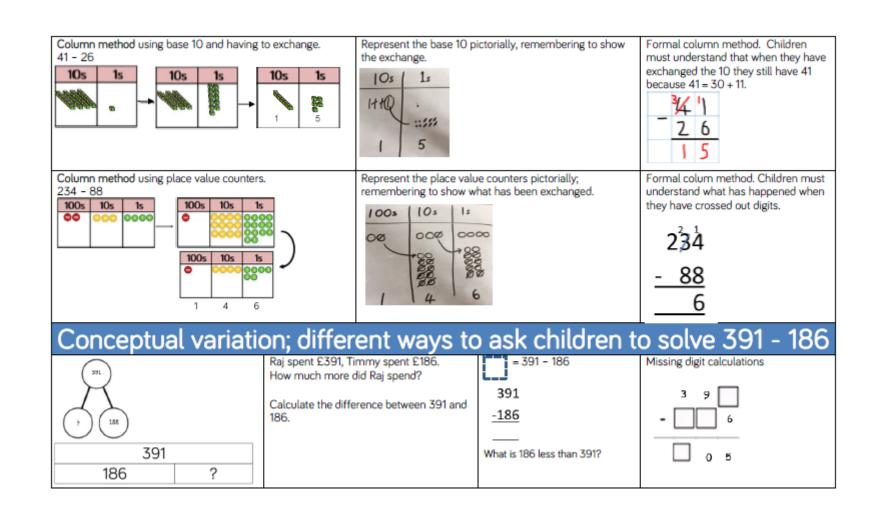
10s	1 s
0	0
000	?
?	5 -

Calculation policy: Subtraction

Key language: take away, less than, the difference, subtract, minus, fewer, decrease.

Concrete	Pictorial	Abstract
Physically taking away and removing objects from a whole (ten frames, Numicon, cubes and other items such as beanbags could be used).	Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used.	4-3=
4 - 3 = 1	Ø Ø Ø Ø	4 3 ?
Counting back (using number lines or number tracks) children start with 6 and count back 2. 6 - 2 = 4	Children to represent what they see pictorially e.g.	Children to represent the calculation on a number line or number track and show their jumps. Encourage children to use an empty number line
1 2 3 4 5 6 7 8 9 10	12345678910	0 1 2 3 4 5 6 7 8 9 10

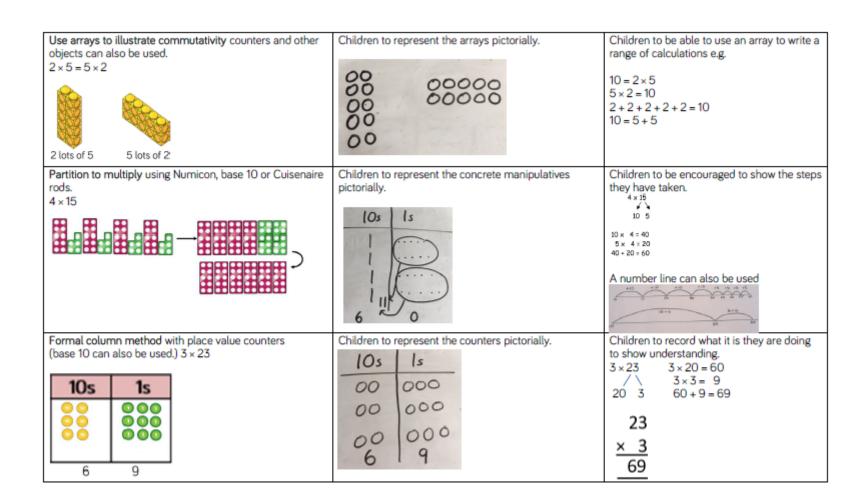


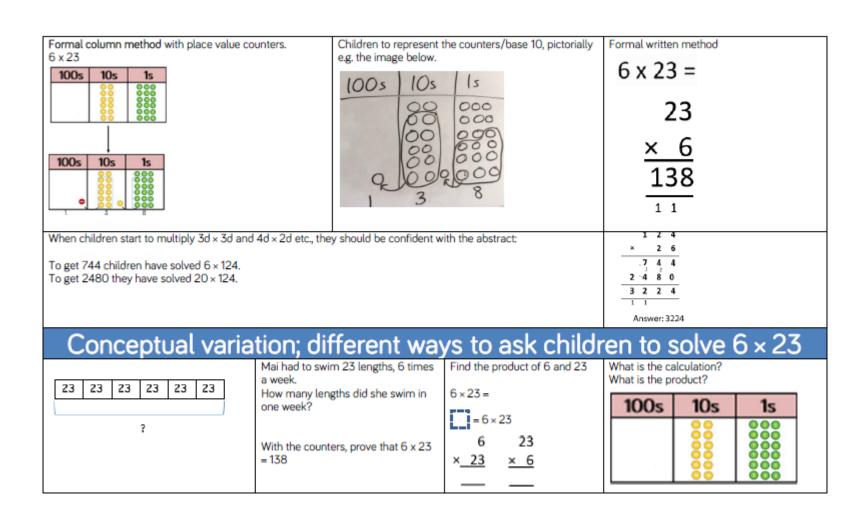


Calculation policy: Multiplication

Key language: double, times, multiplied by, the product of, groups of, lots of, equal groups.

Concrete	Pictorial	Abstract
Repeated grouping/repeated addition 3 × 4 4 + 4 + 4	Children to represent the practical resources in a picture and use a bar model.	3 × 4 = 12 4 + 4 + 4 = 12
There are 3 equal groups, with 4 in each group.	88 88 88	
Number lines to show repeated groups- 3 × 4	Represent this pictorially alongside a number line e.g.:	Abstract number line showing three jumps of four.
Cuisenaire rods can be used too.	0000100001000012	3×4=12

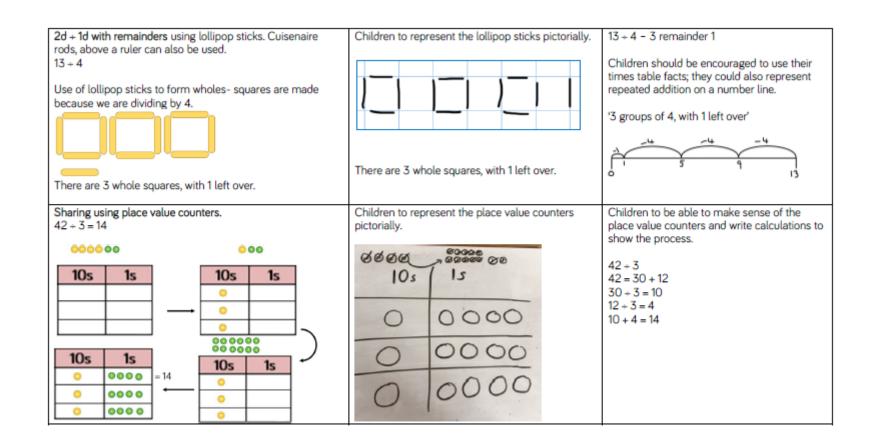




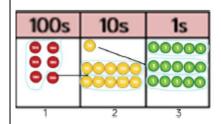
Calculation policy: Division

Key language: share, group, divide, divided by, half.

Concrete	Pictorial	Abstract
Sharing using a range of objects. 6 + 2	Represent the sharing pictorially.	6+2=3
		Children should also be encouraged to use their 2 times tables facts.
Repeated subtraction using Cuisenaire rods above a ruler. 6+2	Children to represent repeated subtraction pictorially.	Abstract number line to represent the equal groups that have been subtracted.
0 1 2 3 4 5 6 7 8 9 10	00000000	-Z -2 -2 -2 3 4 5 6 3 groups
3 groups of 2		

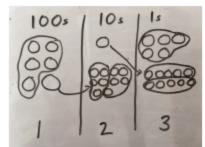


Short division using place value counters to group. $615 \div 5$



- 1. Make 615 with place value counters.
- 2. How many groups of 5 hundreds can you make with 6 hundred counters?
- 3. Exchange 1 hundred for 10 tens.
- 4. How many groups of 5 tens can you make with 11 ten counters?
- 5. Exchange 1 ten for 10 ones.
- 6. How many groups of 5 ones can you make with 15 ones?

Represent the place value counters pictorially.



Children to the calculation using the short division scaffold.

Long division using place value counters 2544 + 12



We can't group 2 thousands into groups of 12 so will exchange them.

We can group 24 hundreds into groups of 12 which leaves with 1 hundred.

