

## FUNCTIONS

To evaluate a function for a given value, simply plug the value into the function for  $x$ .

**Recall:**  $(f \circ g)(x) = f(g(x))$  OR  $f[g(x)]$  read "f of g of x" Means to plug the inside function (in this case  $g(x)$ ) in for  $x$  in the outside function (in this case,  $f(x)$ ).

**Example:** Given  $f(x) = 2x^2 + 1$  and  $g(x) = x - 4$  find  $f(g(x))$ .

$$\begin{aligned} f(g(x)) &= f(x-4) \\ &= 2(x-4)^2 + 1 \\ &= 2(x^2 - 8x + 16) + 1 \\ &= 2x^2 - 16x + 32 + 1 \\ f(g(x)) &= 2x^2 - 16x + 33 \end{aligned}$$

Let  $f(x) = 2x + 1$  and  $g(x) = 2x^2 - 1$ . Find each.

1.  $f(2) = \underline{5}$       2.  $g(-3) = \underline{17}$       3.  $f(t+1) = \underline{2t+3}$

$$4 + 1$$

$$2(-3)^2 - 1$$

$$2(t+1) + 1$$

$$2t + 3$$

4.  $f[g(-2)] = \underline{15}$

$$2(-2)^2 - 1$$

$$f(7)$$

5.  $g[f(m+2)] = \underline{\frac{8m^2 + 40m + 49}{4}}$

$$2(m+2) + 1$$

$$2m + 5$$

$$2(2m+5)^2 - 1$$

$$2(4m^2 + 20m + 25) - 1$$

6.  $[f(x)]^2 - 2g(x) = \underline{4x + 3}$

$$4x^2 + 4x + 1 - 4x^2 + 2$$

Let  $f(x) = \sin(2x)$  Find each exactly.

7.  $f\left(\frac{\pi}{4}\right) = \underline{1}$

$$\sin\left(\frac{\pi}{2}\right)$$

8.  $f\left(\frac{2\pi}{3}\right) = \underline{\frac{-\sqrt{3}}{2}}$

$$\sin\left(\frac{4\pi}{3}\right)$$

Let  $f(x) = x^2$ ,  $g(x) = 2x + 5$ , and  $h(x) = x^2 - 1$ . Find each.

9.  $h[f(-2)] = \underline{15}$

$$h(-4)$$

$$16 - 1$$

10.  $f[g(x-1)] = \underline{4x^2 + 12x + 9}$

$$2(x-1) + 5$$

$$(2x+3)^2$$

$$4x^2 + 12x + 9$$

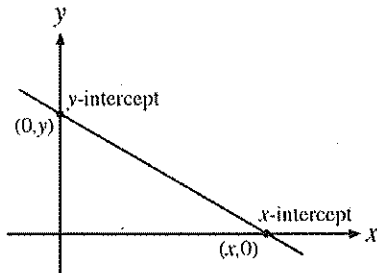
11.  $g[h(x^3)] = \underline{2x^6 + 3}$

$$g(x^6 - 1) = 2(x^6 - 1) + 5$$

$$2x^6 - 2 + 5$$

## INTERCEPTS OF A GRAPH

To find the x-intercepts, let  $y = 0$  in your equation and solve.  
 To find the y-intercepts, let  $x = 0$  in your equation and solve.



**Example:** Given the function  $y = x^2 - 2x - 3$ , find all intercepts.

x-int. (Let  $y = 0$ )

$$0 = x^2 - 2x - 3$$

$$0 = (x-3)(x+1)$$

$$x = -1 \text{ or } x = 3$$

x-i intercepts  $(-1, 0)$  and  $(3, 0)$

y-int. (Let  $x = 0$ )

$$y = 0^2 - 2(0) - 3$$

$$y = -3$$

y-intercept  $(0, -3)$

Find the x and y intercepts for each.

12.  $y = 2x - 5$

$$x = \frac{5}{2}$$

$$\left(\frac{5}{2}, 0\right)$$

$$(0, -5)$$

13.  $y = x^2 + x - 2$

$$(x+2)(x-1)$$

$$x = -2, 1$$

$$(-2, 0)$$

$$(1, 0)$$

$$(0, -2)$$

14.  $y = x\sqrt{16-x^2}$

$$16 - x^2 = 0$$

$$16 = x^2$$

$$(0, 0)$$

$$(\pm 4, 0)$$

15.  $y^2 = x^3 - 4x$

$$(0, 0)$$

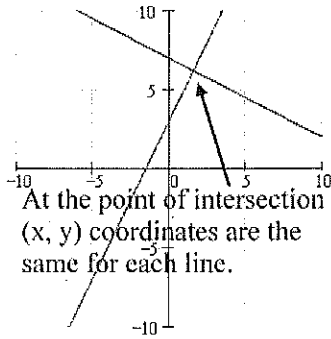
$$x(x^2 - 4)$$

$$(\pm 2, 0)$$

## POINTS OF INTERSECTION

Use substitution or elimination method to solve the system of equations.

Remember: You are finding a POINT OF INTERSECTION so your answer is an ordered pair.



### CALCULATOR TIP

Remember you can use your calculator to verify your answers below. Graph the two lines then go to CALC (2<sup>nd</sup> Trace) and hit INTERSECT.

**Example:** Find all points of intersection of  $x^2 - y = 3$   
 $x - y = 1$

#### ELIMINATION METHOD

Subtract to eliminate  $y$

$$x^2 - x = 2$$

$$x^2 - x - 2 = 0$$

$$(x-2)(x+1) = 0$$

$$x = 2 \text{ or } x = -1$$

Plug in  $x=2$  and  $x=-1$  to find  $y$

Points of Intersection:  $(2, 1)$  and  $(-1, -2)$

#### SUBSTITUTION METHOD

Solve one equation for one variable.

$$y = x^2 - 3$$

$$y = x - 1$$

Therefore by substitution  $x^2 - 3 = x - 1$

$$x^2 - x - 2 = 0$$

From here it is the same as the other example

Find the point(s) of intersection of the graphs for the given equations.

16.  $x + y = 8$   
 $4x - y = 7$

$$y = 8 - x$$

$$4x - (8 - x) = 7$$

$$4x - 8 + x = 7$$

$$5x - 8 = 7$$

$$5x = 15$$

$$x = 3$$

$$y = 5$$

$$(3, 5)$$

17.  $x^2 + y = 6$   
 $x + y = 4$

$$y = 4 - x$$

$$x^2 + 4 - x = 6$$

$$x^2 - x - 2 = 0$$

$$(x-2)(x+1) = 0$$

$$x = 2, -1$$

$$(2, 2) \text{ } ^6 \text{ } (-1, 5)$$

18.  $2 =$   
 $x = 3 - y^2$      $-1 = 3 - 4$   
 $y = x - 1$      $x - y = 1$

$$x = 3 - (x-1)^2$$

$$x = 3 - (x^2 - 2x + 1)$$

$$x = 3 - x^2 + 2x - 1$$

$$x^2 - x - 2 = 0$$

$$(x-2)(x+1) = 0$$

$$x = 2, -1$$

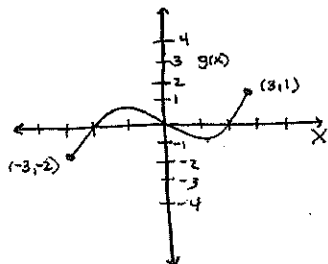
$$(2, 1) \text{ } (-1, -2)$$

# DOMAIN AND RANGE

Domain – All  $x$  values for which a function is defined (input values)

Range – Possible  $y$  or Output values

### EXAMPLE 1



a) Find Domain & Range of  $g(x)$ .

The domain is the set of inputs (x) of the function. Input values run along the horizontal axis. The furthest left input value associated with a pt. on the graph is  $-3$ . The furthest right input values associated with a pt. on the graph is  $3$ . So Domain is  $[-3, 3]$ , that is all reals from  $-3$  to  $3$ .

The range represents the set of output values for the function. Output values run along the vertical axis. The lowest output value of the function is  $-2$ . The highest is  $1$ . So the range is  $[-2, 1]$ , all reals from  $-2$  to  $1$ .

### EXAMPLE 2

Find the domain and range of  $f(x) = \sqrt{4-x^2}$   
Write answers in interval notation.

#### DOMAIN

For  $f(x)$  to be defined  $4-x^2 \geq 0$ .

This is true when  $-2 \leq x \leq 2$

Domain:  $[-2, 2]$

#### RANGE

The solution to a square root must always be positive thus  $f(x)$  must be greater than or equal to  $0$ .

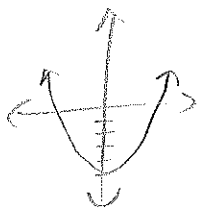
Range:  $[0, \infty)$

Find the domain and range of each function. Write your answer in INTERVAL notation.

19.  $f(x) = x^2 - 5$

D:  $x = \mathbb{R}$

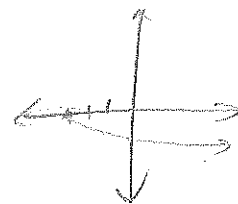
R:  $y \geq -5$



20.  $f(x) = -\sqrt{x+3}$

D:  $x \geq -3$

R:  $y \leq 0$



21.  $f(x) = 3 \sin x$

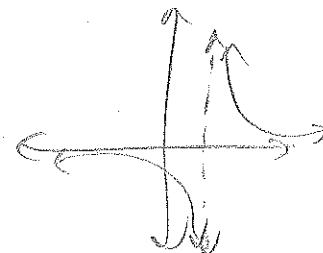
D:  $x = \mathbb{R}$

R:  $-3 \leq y \leq 3$

22.  $f(x) = \frac{2}{x-1}$

D:  $x \neq 1$

R:  $y \neq 0$

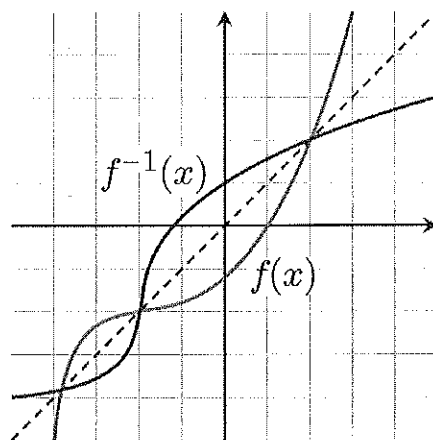


## INVERSES

To find the inverse of a function, simply switch the  $x$  and the  $y$  and solve for the new "y" value. Recall  $f^{-1}(x)$  is defined as the inverse of  $f(x)$

### Example 1:

|                             |                             |
|-----------------------------|-----------------------------|
| $f(x) = \sqrt[3]{x+1}$      | Rewrite $f(x)$ as $y$       |
| $y = \sqrt[3]{x+1}$         | Switch $x$ and $y$          |
| $x = \sqrt[3]{y+1}$         | Solve for your new $y$      |
| $(x)^3 = (\sqrt[3]{y+1})^3$ | Cube both sides             |
| $x^3 = y+1$                 | Simplify                    |
| $y = x^3 - 1$               | Solve for $y$               |
| $f^{-1}(x) = x^3 - 1$       | Rewrite in inverse notation |



Find the inverse for each function.

23.  $f(x) = 2x + 1$        $f^{-1}(x) = \frac{x-1}{2}$

$$y = 2x + 1$$

$$x = 2y + 1$$

$$x - 1 = 2y$$

$$\frac{x-1}{2} = y$$

25.  $g(x) = \frac{5}{x-2}$        $f^{-1}(x) = \frac{5}{x} + 2$

$$y = \frac{5}{x-2}$$

$$x = \frac{5}{y-2}$$

$$y-2 = \frac{5}{x}$$

24.  $f(x) = \frac{x^2}{3}$  only if  $x \geq 0$

$$y = \frac{x^2}{3}$$

$$3x = y^2$$

$$\sqrt{3x} = y$$

$$f^{-1}(x) = \sqrt{3x}$$

26.  $y = \sqrt{4-x} + 1$        $f^{-1}(x) = 4 - (x-1)^2$

$$y-1 = \sqrt{4-x}$$

$$x-1 = \sqrt{4-y}$$

$$(x-1)^2 = 4-y$$

$$y = 4 - (x-1)^2$$

$x \geq 1$

27. If the graph of  $f(x)$  has the point  $(2, 7)$  then what is one point that will be on the graph of  $f^{-1}(x)$ ?

$$(7, 2)$$

28. Explain how the graphs of  $f(x)$  and  $f^{-1}(x)$  compare.

reflections over  $y = x$   
(identity)  
line

## EQUATION OF A LINE

**Slope intercept form:**  $y = mx + b$

**Vertical line:**  $x = c$  (slope is undefined)

**Point-slope form:**  $y - y_1 = m(x - x_1)$

**Horizontal line:**  $y = c$  (slope is 0)

\* LEARN! We will use this formula frequently!

**Example:** Write a linear equation that has a slope of  $\frac{1}{2}$  and passes through the point (2, -6)

**Slope intercept form**

$$y = \frac{1}{2}x + b$$

Plug in  $\frac{1}{2}$  for  $m$

$$-6 = \frac{1}{2}(2) + b$$

Plug in the given ordered

$$b = -7$$

Solve for  $b$

$$y = \frac{1}{2}x - 7$$

**Point-slope form**

$$y + 6 = \frac{1}{2}(x - 2)$$

Plug in all variables

$$y = \frac{1}{2}x - 7$$

Solve for  $y$

29. Determine the equation of a line passing through the point (5, -3) with an undefined slope.

$$x = 5$$

30. Determine the equation of a line passing through the point (-4, 2) with a slope of 0.

$$y = 2$$

31. Use point-slope form to find the equation of the line passing through the point (0, 5) with a slope of  $\frac{2}{3}$ .

$$y = \frac{2}{3}x + 5$$

$$y - 5 = \frac{2}{3}(x - 0)$$

32. Use point-slope form to find a line passing through the point (2, 8) and parallel to the line  $y = \frac{5}{6}x - 1$ .  $m = \frac{5}{6}$

$$\frac{48}{6} - \frac{10}{6} = \frac{38}{6} \quad y - 8 = \frac{5}{6}(x - 2)$$

$$y = \frac{5}{6}x + \frac{19}{3}$$

33. Use point-slope form to find a line perpendicular to  $y = -2x + 9$  passing through the point (4, 7).

$$m = \frac{1}{2}$$

$$y - 7 = \frac{1}{2}(x - 4)$$

$$y = \frac{1}{2}x + 5$$

34. Find the equation of a line passing through the points (-3, 6) and (1, 2).

$$m = \frac{6 - 2}{-3 - 1} = \frac{4}{-4} = -1$$

$$y - 2 = -1(x - 1) \quad y = -x + 3$$

$$y - 2 = -x + 1$$

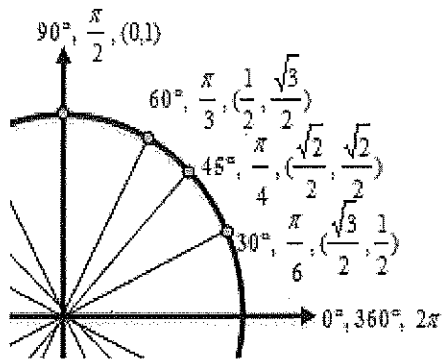
35. Find the equation of a line with an x-intercept (2, 0) and a y-intercept (0, 3)

$$m = \frac{0 - 3}{2 - 0} = \frac{-3}{2}$$

9

$$y = \frac{-3}{2}x + 3$$

## UNIT CIRCLE



You can determine the sine or the cosine of any standard angle on the unit circle. The x-coordinate of the circle is the cosine and the y-coordinate is the sine of the angle. Recall tangent is defined as  $\sin/\cos$  or the slope of the line.

**Examples:**

$$\sin \frac{\pi}{2} = 1 \qquad \cos \frac{\pi}{2} = 0 \qquad \tan \frac{\pi}{2} = \text{und}$$

\*You must have these memorized OR know how to calculate their values without the use of a calculator.

36. a.)  $\sin \pi = 0$       b.)  $\cos \frac{3\pi}{2} = 0$       c.)  $\sin\left(-\frac{\pi}{2}\right) = -1$       d.)  $\sin\left(\frac{5\pi}{4}\right) = \frac{-\sqrt{2}}{2}$

e.)  $\cos \frac{\pi}{4} = \frac{\sqrt{2}}{2}$       f.)  $\cos(-\pi) = -1$       g.)  $\cos \frac{\pi}{3} = \frac{1}{2}$       h.)  $\sin \frac{5\pi}{6} = \frac{1}{2}$

i.)  $\cos \frac{2\pi}{3} = -\frac{1}{2}$       j.)  $\tan \frac{\pi}{4} = 1$       k.)  $\tan \pi = \frac{0}{1} = 0$       l.)  $\tan \frac{\pi}{3} = \frac{\sqrt{3}/2}{1/2} = \sqrt{3}$

m.)  $\cos \frac{4\pi}{3} = -\frac{1}{2}$       n.)  $\sin \frac{11\pi}{6} = -\frac{1}{2}$       o.)  $\tan \frac{7\pi}{4} = -1$       p.)  $\sin\left(-\frac{\pi}{6}\right) = -\frac{1}{2}$

## TRIGONOMETRIC EQUATIONS

Solve each of the equations for  $0 \leq x < 2\pi$ .

37.  $\sin x = -\frac{1}{2}$

$$x = \frac{11\pi}{6}, \frac{7\pi}{6}$$

38.  $2 \cos x = \sqrt{3}$

$$\cos x = \frac{\sqrt{3}}{2}$$

$$x = \frac{\pi}{6}, \frac{11\pi}{6}$$

39.  $4 \sin^2 x = 3$

\*\*Recall  $\sin^2 x = (\sin x)^2$

\*\*Recall if  $x^2 = 25$  then  $x = \pm 5$

$$\sin^2 x = \frac{3}{4}$$

$$\sin x = \pm \frac{\sqrt{3}}{2}$$

$$x = \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$$

40.  $2 \cos^2 x - 1 - \cos x = 0$  \*Factor

$$2 \cos^2 x - \cos x - 1 = 0$$

$$(2 \cos x + 1)(\cos x - 1) = 0$$

$$\cos x = -\frac{1}{2} \quad \cos x = 1$$

$$x = \frac{2\pi}{3}, \frac{4\pi}{3}$$

$$x = 0\pi$$

$$2x^2 - x - 1 = 0$$

$$(2x+1)(x-1)$$

## TRANSFORMATION OF FUNCTIONS

$$h(x) = f(x) + c$$

Vertical shift  $c$  units up

$$h(x) = f(x - c)$$

Horizontal shift  $c$  units right

$$h(x) = f(x) - c$$

Vertical shift  $c$  units down

$$h(x) = f(x + c)$$

Horizontal shift  $c$  units left

$$h(x) = -f(x)$$

Reflection over the x-axis

41. Given  $f(x) = x^2$  and  $g(x) = (x-3)^2 + 1$ . How does the graph of  $g(x)$  differ from  $f(x)$ ?

up 1  
right 3

42. Write an equation for the function that has the shape of  $f(x) = x^3$  but moved six units to the left and reflected over the x-axis.

$$g(x) = -(x+6)^3$$

43. If the ordered pair  $(2, 4)$  is on the graph of  $f(x)$ , find one ordered pair that will be on the following functions:

a)  $f(x) - 3$

$$(2, 1)$$

b)  $f(x-3)$

$$(5, 4)$$

c)  $2f(x)$

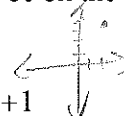
$$(2, 8)$$

d)  $f(x-2) + 1$

$$(4, 5)$$

e)  $-f(x)$

$$(2, -4)$$





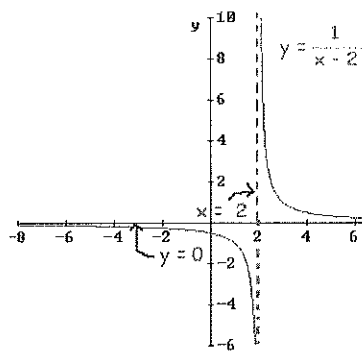
## VERTICAL ASYMPTOTES

Determine the vertical asymptotes for the function. Set the denominator equal to zero to find the x-value for which the function is undefined. That will be the vertical asymptote given the numerator does not equal 0 also (Remember this is called removable discontinuity).

Write a vertical asymptotes as a line in the form  $x =$

Example: Find the vertical asymptote of  $y = \frac{1}{x-2}$

Since when  $x = 2$  the function is in the form  $1/0$  then the vertical line  $x = 2$  is a vertical asymptote of the function.



44.  $f(x) = \frac{1}{x^2}$

$x = 0$

45.  $f(x) = \frac{x^2}{x^2 - 4}$

$x = 2, x = -2$

46.  $f(x) = \frac{2+x}{x^2(1-x)}$

$x = 0, x = 1$

47.  $f(x) = \frac{4-x}{x^2-16} \frac{\cancel{(x-4)}}{\cancel{(x-4)}(x+4)}$

$x = -4$

48.  $f(x) = \frac{x-1}{x^2+x-2} \frac{x-1}{(x+2)(x-1)}$

$x = -2$

49.  $f(x) = \frac{5x+20}{x^2-16} \frac{5(x+4)}{(x+4)(x-4)}$

$x = 4$

## HORIZONTAL ASYMPTOTES

Determine the horizontal asymptotes using the three cases below.

**Case I.** Degree of the numerator is less than the degree of the denominator. The asymptote is  $y = 0$ .

Example:  $y = \frac{1}{x-1}$  (As  $x$  becomes very large or very negative the value of this function will approach 0). Thus there is a horizontal asymptote at  $y = 0$ .

**Case II.** Degree of the numerator is the same as the degree of the denominator. The asymptote is the ratio of the lead coefficients.

Example:  $y = \frac{2x^2 + x - 1}{3x^2 + 4}$  (As  $x$  becomes very large or very negative the value of this function will approach  $2/3$ ). Thus there is a horizontal asymptote at  $y = \frac{2}{3}$ .

**Case III.** Degree of the numerator is greater than the degree of the denominator. There is no horizontal asymptote. The function increases without bound. (If the degree of the numerator is exactly 1 more than the degree of the denominator, then there exists a slant asymptote, which is determined by long division.)

Example:  $y = \frac{2x^2 + x - 1}{3x - 3}$  (As  $x$  becomes very large the value of the function will continue to increase and as  $x$  becomes very negative the value of the function will also become more negative).

**Determine all Horizontal Asymptotes.**

50.  $f(x) = \frac{x^2 - 2x + 1}{x^3 + x - 7}$

$y = 0$

51.  $f(x) = \frac{5x^3 - 2x^2 + 8}{4x - 3x^3 + 5}$

$y = -\frac{5}{3}$

52.  $f(x) = \frac{4x^2}{3x^2 - 7}$

$y = \frac{4}{3}$

53.  $f(x) = \frac{(2x-5)^2}{x^2-x}$   $\frac{4x^2 - 20x + 25}{x^2 - x}$  54.  $f(x) = \frac{-3x+1}{\sqrt{x^2+x}}$  \* Remember  $\sqrt{x^2} = \pm x$

$y = 4$

$y = -3$   
 $y = 3$

\*This is very important in the use of limits.\*

## EXPONENTIAL FUNCTIONS

**Example: Solve for x**

$$4^{x+1} = \left(\frac{1}{2}\right)^{3x-2}$$

$$(2^2)^{x+1} = (2^{-1})^{3x-2} \quad \text{Get a common base}$$

$$2^{2x+2} = 2^{-3x+2} \quad \text{Simplify}$$

$$2x+2 = -3x+2 \quad \text{Set exponents equal}$$

$$x = 0 \quad \text{Solve for x}$$

**Solve for x:**

55.  $3^{3x+5} = 9^{2x+1}$

$$3^{3x+5} = 3^{2(2x+1)}$$

$$3x+5 = 4x+2$$

$$3 = x$$

56.  $\left(\frac{1}{9}\right)^x = 27^{2x+4}$

$$9^{-x} = 27^{2x+4}$$

$$3^{-2x} = 3^{3(2x+4)}$$

$$-2x = 6x + 12$$

$$-8x = 12 \quad x = -\frac{3}{2}$$

57.  $\left(\frac{1}{6}\right)^x = 216$

$$6^{-x} = 6^3$$

$$-x = 3$$

$$x = -3$$

$$\frac{36}{6} = 216$$

## LOGARITHMS

The statement  $y = b^x$  can be written as  $x = \log_b y$ . They mean the same thing.

**REMEMBER: A LOGARITHM IS AN EXPONENT**

Recall  $\ln x = \log_e x$

The value of  $e$  is 2.718281828... or  $\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^x$

**Example: Evaluate the following logarithms**

$$\log_2 8 = ?$$

In exponential for this is  $2^? = 8$

Therefore  $? = 3$

Thus  $\log_2 8 = 3$

**Evaluate the following logarithms**

58.  $\log_7 7 = 1$

59.  $\log_3 27 = 3$

60.  $\log_2 \frac{1}{32} = -5$

61.  $\log_{25} 5 = \frac{1}{2}$

62.  $\log_9 1 = 0$

63.  $\log_4 8 = \frac{3}{2}$

$$4^x = 8 \quad 2^{2x} = 2^3$$

64.  $\ln \sqrt{e} = \frac{1}{2}$

65.  $\ln \frac{1}{e} = -1$

$$\ln e^{\frac{1}{2}}$$

$$\ln e^{-1}$$

## PROPERTIES OF LOGARITHMS

$$\log_b xy = \log_b x + \log_b y$$

$$\log_b \frac{x}{y} = \log_b x - \log_b y$$

$$\log_b x^y = y \log_b x$$

$$b^{\log_b x} = x$$

Examples:

Expand  $\log_4 16x$

$$\log_4 16 + \log_4 x$$

$$2 + \log_4 x$$

Condense  $\ln y - 2 \ln R$

$$\ln y - \ln R^2$$

$$\ln \frac{y}{R^2}$$

Expand  $\log_2 7x^5$

$$\log_2 7 + \log_2 x^5$$

$$\log_2 7 + 5 \log_2 x$$

Use the properties of logarithms to evaluate the following

66.  $\log_2 2^5 = 5$

67.  $\ln e^3 = 3$

68.  $\log_2 8^3 = 9$

$$2^x = 8^3$$

$$2^x = 2^9$$

69.  $\log_3 \sqrt[3]{9} = \frac{2}{3}$

$$3^x = 9^{\frac{1}{3}}$$

$$3^x = 3^{\frac{2}{3}}$$

70.  $2^{\log_2 10} = 10$

71.  $e^{\ln 8} = 8$

72.  $9 \ln e^2 = 18$

73.  $\log_9 9^3 = 3$

74.  $\log_{10} 25 + \log_{10} 4 = 2$

$$\log_{10} 100$$

75.  $\log_2 40 - \log_2 5 = 3$

$$\log_2 \frac{40}{5} = \log_2 8$$

76.  $\log_2 (\sqrt{2})^5 = \frac{5}{2}$

$$5 \log_2 2^{\frac{1}{2}}$$

## EVEN AND ODD FUNCTIONS

**Recall:**

**Even functions** are functions that are symmetric over the y-axis.

To determine algebraically we find out if  $f(x) = f(-x)$

(\*Think about it what happens to the coordinate  $(x, f(x))$  when reflected across the y-axis\*)

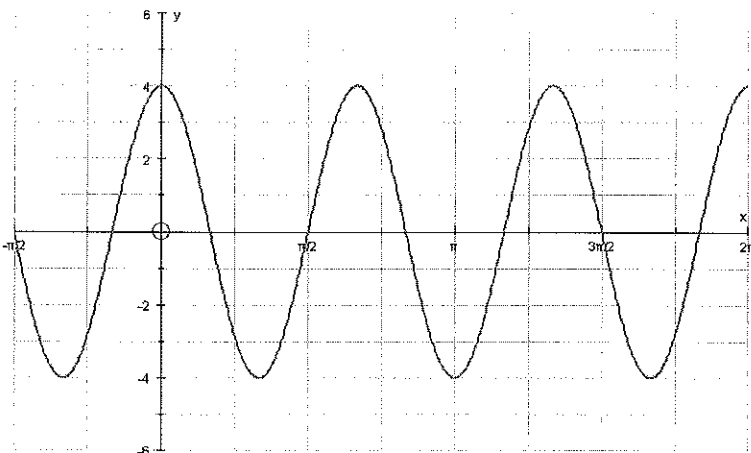
**Odd functions** are functions that are symmetric about the origin.

To determine algebraically we find out if  $f(-x) = -f(x)$

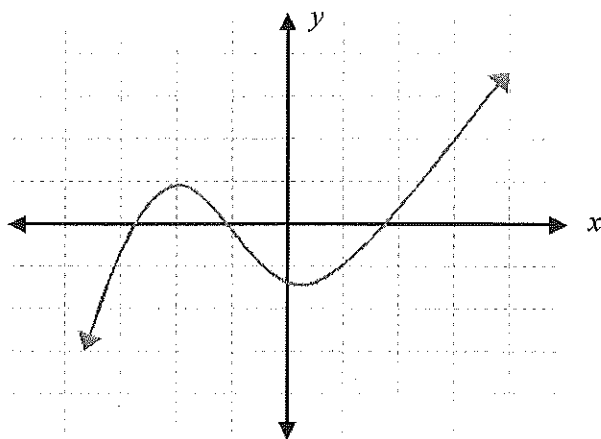
(\*Think about it what happens to the coordinate  $(x, f(x))$  when reflected over the origin\*)

State whether the following graphs are even, odd or neither, show ALL work.

77. even



78. neither



79. even  
 $f(x) = 2x^4 - 5x^2$

80. odd  
 $g(x) = x^5 - 3x^3 + x$

81. neither  
 $h(x) = 2x^2 - 5x + 3$

82. even  
 $j(x) = 2 \cos x$   
 $\cos(-x) = \cos x$

83. neither  
 $k(x) = \sin x + 4$   
 $\sin(-x) = -\sin x$

84. even  
 $l(x) = \cos x - 3$