Troy High School AP Calculus Summer Packet

As instructors of AP Calculus, we have extremely high expectations of students taking our courses. We expect a certain level of independence to be demonstrated by the students taking AP Calculus. This summer packet is your first opportunity to demonstrate your capabilities and resourcefulness to us through completion of this packet. It is designed for you to retain, relearn, and review topics of Algebra, Trigonometry, and Pre-Calculus. Without mastering these topics, you will find that you will consistently get problems incorrect even though you may understand the calculus topics.

Work needs to be shown, when possible, in a neat and organized manner. Since you can only use a calculator on half of the AP exam, you should not always rely on your calculator. You must be familiar with certain built-in calculator functions such as finding maximum and minimum values, intersection points, and zeros of a function.

A list of topical understandings represented in this summer packet is listed below. Please be familiar with all of them and ready to apply them to a higher level.

- Complex Fractions
- Simplifying Expressions
- Functions
- Intercepts and Points of Intersection
- Interval Notation
- Domain and Range
- Inverses
- Equations of Lines

- Radian and Degree Measure
- Reference Triangles
- Unit Circle
- Graphing Trigonometric Functions
- Graphing Calculator Usage
- Limits
- Asymptotes

Finally, it is not suggested to wait until the week before school starts to begin the packet. If you spread it out, you will more likely retain the information better. A test over this material will be given within the first two weeks of school.

Best of Luck!

Troy High AP Calculus Teachers

Summer Review Packet for Students Entering Calculus (all levels)

Complex Fractions

When simplifying complex fractions, multiply by a fraction equal to 1 which has a numerator and denominator composed of the common denominator of all the denominators in the complex fraction.

Example:

$$\frac{-7 - \frac{6}{x+1}}{\frac{5}{x+1}} = \frac{-7 - \frac{6}{x+1}}{\frac{5}{x+1}} \cdot \frac{x+1}{x+1} = \frac{-7(x+1) - 6}{5} = \frac{-7x - 13}{5}$$

$$\frac{\frac{-2}{x} + \frac{3x}{x-4}}{5 - \frac{1}{x-4}} = \frac{\frac{-2}{x} + \frac{3x}{x-4}}{5 - \frac{1}{x-4}} \cdot \frac{x(x-4)}{x(x-4)} = \frac{-2(x-4) + 3x(x)}{5(x)(x-4) - 1(x)} = \frac{-2x + 8 + 3x^2}{5x^2 - 20x - x} = \frac{3x^2 - 2x + 8}{5x^2 - 21x}$$

Simplify each of the following.

$$1. \frac{\frac{25}{a} - a}{5 + a}$$

$$2. \frac{2 - \frac{4}{x+2}}{5 + \frac{10}{x+2}}$$

3.
$$\frac{4 - \frac{12}{2x - 3}}{5 + \frac{15}{2x - 3}}$$

4.
$$\frac{\frac{x}{x+1} - \frac{1}{x}}{\frac{x}{x+1} + \frac{1}{x}}$$

$$5. \ \frac{1 - \frac{2x}{3x - 4}}{x + \frac{32}{3x - 4}}$$

Simplifying Expressions

Make sure you are very comfortable manipulating exponents, positive/negative, fractional. Also, know the relationship between exponents and radicals; the appropriate radical will "undo" an exponent.

Examples:

$$\sqrt[3]{(2)^3} = 2$$

$$\sqrt[3]{8} = 8^{1/3} = 2$$

$$\frac{\sqrt[3]{(2)^{3}}}{\sqrt[3]{8}} = 2$$

$$\frac{\sqrt[3]{8}}{\sqrt[3]{8}} = 8^{\frac{1}{3}} = 2$$

$$(\sqrt[10]{25})^{5} = (25^{\frac{1}{10}})^{5} = 25^{\frac{5}{10}} = 25^{\frac{1}{2}} = \sqrt{25} = 5$$

$$(3x)^{-2} = \frac{1}{(3x)^{2}} = \frac{1}{9x^{2}}$$

$$(x^{2})^{3} = x^{6}$$

$$x^{-4} = \frac{1}{x^4}$$

$$\frac{1}{x^3} = x^3$$

$$\frac{1}{x^{-3}} = x^3$$

$$(3x)^{-2} = \frac{1}{(3x)^2} = \frac{1}{9x^2}$$

$$x^6x^5 = x^{11}$$

$$\frac{x^3}{x^9} = x^{-6} = \frac{1}{x^6}$$

$$\left(x^2\right)^3 = x^6$$

Simplify each expression. Write answers with positive exponents where applicable.

A.

$$\frac{1}{x+h} - \frac{1}{x}$$

F.
$$\left(4a^{\frac{5}{3}}\right)^{\frac{3}{2}}$$

B.

$$\frac{\frac{2}{x^2}}{\frac{10}{x^3}}$$

$$\frac{\frac{1}{2} - \frac{5}{4}}{\frac{3}{8}}$$

C.

$$\frac{12x^{-3}y^2}{18xv^{-1}}$$

3

$$\frac{5-x}{x^2-25}$$

D.

$$\frac{15x^2}{5\sqrt{x}}$$

E.

$$(5a^3)(4a^2)$$

Functions

To evaluate a function for a given value, simply plug the value into the function for ${f x}.$

Recall: $(f \circ g)(x) = f(g(x)) OR f[g(x)]$ read " $f \circ g \circ f x$ " means: plug the inside function (in this case g(x)) in for x in the outside function (in this case, f(x)).

Example: Given $f(x) = 2x^2 + 1$ and g(x) = x - 4 find f(g(x)).

$$f(g(x)) = f(x-4)$$

$$= 2(x-4)^{2} + 1$$

$$= 2(x^{2} - 8x + 16) + 1$$

$$= 2x^{2} - 16x + 32 + 1$$

$$f(g(x)) = 2x^{2} - 16x + 33$$

Let f(x) = 2x+1 and $g(x) = 2x^2-1$. Find each.

6.
$$f(2) =$$
 8. $f(t+1) =$

8.
$$f(t+1) =$$

9.
$$f[g(-2)] =$$

10.
$$g[f(m+2)] =$$

9.
$$f[g(-2)] = \underline{\qquad}$$
 10. $g[f(m+2)] = \underline{\qquad}$ 11. $\frac{f(x+h)-f(x)}{h} = \underline{\qquad}$

Let $f(x) = \sin x$ Find each exactly.

12.
$$f\left(\frac{\pi}{2}\right) =$$

13.
$$f\left(\frac{2\pi}{3}\right) =$$

Let $f(x) = x^2$, g(x) = 2x + 5, and $h(x) = x^2 - 1$. Find each.

14.
$$h[f(-2)] =$$

15.
$$f[g(x-1)] =$$

4

14.
$$h[f(-2)] =$$
 15. $f[g(x-1)] =$ 16. $g[h(x^3)] =$

Find $\frac{f(x+h)-f(x)}{h}$ for the given function f.

17.
$$f(x) = 9x + 3$$

18.
$$f(x) = 5 - 2x$$

Intercepts and Points of Intersection

To find the x-intercepts, let y = 0 in your equation and solve. To find the y-intercepts, let x = 0 in your equation and solve.

Example: $y = x^2 - 2x - 3$

$$\frac{x - \text{int. } (Let \ y = 0)}{0 = x^2 - 2x - 3}$$

$$0 = x^2 - 2x - 3$$

$$0 = (x-3)(x+1)$$
$$x = -1 \text{ or } x = 3$$

$$x = -1 \text{ or } x = 3$$

x-i ntercepts (-1,0) and (3,0)

$$y-int. (Let x = 0)$$

$$y = 0^2 - 2(0) - 3$$

$$y = -3$$

$$y-intercept (0, -3)$$

$$y = 0^2 - 2(0) - 3$$

$$y = -3$$

Find the x and y intercepts for each.

19.
$$y = 2x - 5$$

20.
$$y = x^2 + x - 2$$

21.
$$y = x\sqrt{16 - x^2}$$

22.
$$y^2 = x^3 - 4x$$

Use substitution or elimination method to solve the system of equations.

Example:

$$x^2 + y^2 - 16x + 39 = 0$$

$$x^2 - y^2 - 9 = 0$$

Elimination Method

$$2x^2 - 16x + 30 = 0$$

$$x^2 - 8x + 15 = 0$$

$$(x-3)(x-5) = 0$$

$$x = 3$$
 and $x = 5$

Plug x = 3 and x = 5 into one original

$$3^{2} - y^{2} - 9 = 0$$

$$-y^{2} = 0$$

$$y = 0$$

$$y = \pm 4$$

$$5^{2} - y^{2} - 9 = 0$$

$$16 = y^{2}$$

$$y = \pm 4$$

$$5^2 - y^2 - 9 = 0$$

$$-y^2 = 0$$

$$16 = v^{2}$$

$$y = 0$$

$$y = \pm 4$$

Points of Intersection (5,4), (5,-4) and (3,0)

$$y^2 = -x^2 + 16x - 39$$

Substitution Method
Solve one equation for one variable.

$$y^{2} = -x^{2} + 16x - 39$$

$$x^{2} - (-x^{2} + 16x - 39) - 9 = 0$$
(1st equation solved for y)
$$x^{2} - (-x^{2} + 16x - 39) - 9 = 0$$
Plug what y^{2} is equal to into second equation.
$$2x^{2} - 16x + 30 = 0$$

$$x^{2} - 8x + 15 = 0$$

$$x^{2} - 8x + 15 = 0$$

$$(x - 3)(x - 5) = 0$$

$$x = 3 \text{ or } x - 5$$

$$2x^2 - 16x + 30 = 0$$

$$x^2 - 8x + 15 = 0$$

$$x = 3 \text{ or } x - 5$$

Find the point(s) of intersection of the graphs for the given equations.

$$23. \qquad \begin{array}{c} x+y=8\\ 4x-y=7 \end{array}$$

$$24. \qquad x^2 + y = 6$$
$$x + y = 4$$

25.
$$2x - 3y = 5$$
$$5x - 4y = 6$$

Interval Notation

26. Complete the table with the appropriate notation or graph.

Solution	Interval Notation	Graph
$-2 < x \le 4$		
	[-1,7)	
		8

Solve each equation. State your answer in BOTH interval notation and graphically.

27.
$$2x-1 \ge 0$$

28.
$$-4 \le 2x - 3 < 4$$

29.
$$\frac{x}{2} - \frac{x}{3} > 5$$

Domain and Range

Find the domain and range of each function. Write your answer in INTERVAL notation.

30.
$$f(x) = x^2 - 5$$

30.
$$f(x) = x^2 - 5$$
 31. $f(x) = -\sqrt{x+3}$ 32. $f(x) = 3\sin x$

$$32. \quad f(x) = 3\sin x$$

33.
$$f(x) = \frac{2}{x-1}$$

Inverses

To find the inverse of a function, simply switch the x and the y and solve for the new "y" value.

Example:

$$f(x) = \sqrt[3]{x+1}$$
 Rewrite f(x) as y
 $y = \sqrt[3]{x+1}$ Switch x and y
 $x = \sqrt[3]{y+1}$ Solve for your new y

$$(x)^3 = (\sqrt[3]{y+1})^3$$
 Cube both sides

$$x^3 = y + 1$$
 Simplify

$$y = x^3 - 1$$
 Solve for y

$$f^{-1}(x) = x^3 - 1$$
 Rewrite in inverse notation

Find the inverse for each function.

34.
$$f(x) = 2x + 1$$

35.
$$f(x) = \frac{x^2}{3}$$

Also, recall that to PROVE one function is an inverse of another function, you need to show that: f(g(x)) = g(f(x)) = x

Example:

If: $f(x) = \frac{x-9}{4}$ and g(x) = 4x+9 show f(x) and g(x) are inverses of each other.

$$f(g(x)) = 4\left(\frac{x-9}{4}\right) + 9$$

$$= x - 9 + 9$$

$$= x$$

$$= x$$

$$g(f(x)) = \frac{(4x+9)-9}{4}$$

$$= \frac{4x+9-9}{4}$$

$$= \frac{4x}{4}$$

$$= x$$

f(g(x)) = g(f(x)) = x therefore they are inverses of each other.

Prove f and g are inverses of each other.

36.
$$f(x) = \frac{x^3}{2}$$
 $g(x) = \sqrt[3]{2x}$

37.
$$f(x) = 9 - x^2, x \ge 0$$
 $g(x) = \sqrt{9 - x}$

Equation of a line

Slope intercept form: y = mx + b **Vertical line:** x = c (slope is undefined)

Point-slope form: $y - y_1 = m(x - x_1)$ **Horizontal line:** y = c (slope is 0)

- 38. Use slope-intercept form to find the equation of the line having a slope of 3 and a y-intercept of 5.
- 39. Determine the equation of a line passing through the point (5, -3) with an undefined slope.
- 40. Determine the equation of a line passing through the point (-4, 2) with a slope of 0.
- 41. Use point-slope form to find the equation of the line passing through the point (0, 5) with a slope of 2/3.
- 42. Find the equation of a line passing through the point (2, 8) and parallel to the line $y = \frac{5}{6}x 1$.
- 43. Find the equation of a line perpendicular to the y- axis passing through the point (4, 7).
- 44. Find the equation of a line passing through the points (-3, 6) and (1, 2).
- 45. Find the equation of a line with an x-intercept (2, 0) and a y-intercept (0, 3).

Radian and Degree Measure

To convert radian to degrees, make use of the fact that π radian equals one half of a circle, or 180°. SO, divide radians by π , and you'll get the # of half circle, Multiply by 180 will give you the answer in degrees.

$$degrees = radians \times \frac{180}{\pi}$$

To convert degrees to radians, first find the # of half circles in the answer by dividing by 180°. Since each half circle equals π radians, multiply the # of half circles by π get the answer in radian.

$$radians = degrees \times \frac{\pi}{180}$$

- 46. Convert to degrees:
- a. $\frac{5\pi}{6}$
- b. $\frac{4\pi}{5}$

c. 2.63 radians

- 47. Convert to radians:
- a. 45°
- b. -17°

to the terminal side.

c. 237°

Angle is in standard position if its vertex is located at the origin and

one ray is on the positive x-axis (initial side). Other ray is the terminal side. Angle is measured by the amount of rotation from the initial side

Angles in Standard Position

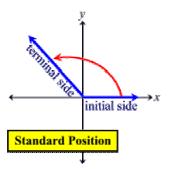
48. Sketch the angle in standard position.

a. $\frac{11\pi}{6}$

b. 230°

c. $-\frac{5\pi}{3}$

d. 1.8 radians



Reference Triangles (If you don't remember how to do this, google "reference triangles")

- 49. Sketch the angle in standard position. Draw the reference triangle and label the sides, if possible.
- a. $\frac{2}{3}\pi$

b. 225°

c. $-\frac{\pi}{4}$

d. 30°

Unit Circle

You can determine the sine or cosine for basic angles by using the unit circle. The x-coordinate of the circle is the cosine and the y-coordinate is the sine of the angle. See Unit Circle worksheet for more practice.

Example: $\sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}$

 $\cos\frac{4\pi}{3} = -\frac{1}{2}$

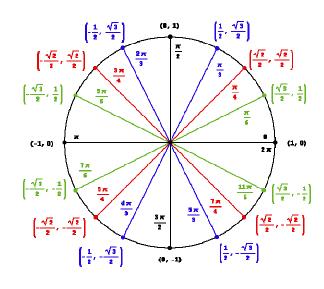
50. a.) $\sin \pi =$

 $b.) \cos \frac{5\pi}{4}$

- $c.) \sin(-\frac{\pi}{2}) =$
- $d.) \sin \frac{11\pi}{6} =$

e.) $\cos 2\pi =$

f.) $\cos(-\pi) =$



Graphing Trig Functions

y = sin x and y = cos x have a period of 2π and an amplitude of 1. Use the parent graphs above to help you sketch a graph of the functions below. For $f(x) = A\sin(Bx + C) + K$, A = amplitude, $\frac{2\pi}{B}$ = period,

 $\frac{C}{B}$ = phase shift (positive C/B shift left, negative C/B shift right) and K = vertical shift.

Graph two complete periods of the function.

$$51. \quad f(x) = 5\sin x$$

52.
$$f(x) = \sin 2x$$

$$53. \ f(x) = -\cos\left(x - \frac{\pi}{4}\right)$$

$$54. \ f(x) = \cos x - 3$$

Using the Graphing Calculator

+pend some time getting comfortable with your graphing calculator, if you are not already. For calculus, you should be comfortable (1) graphing an arbitrary function, (2) finding zeros (or roots) of a function, (3) and finding the intersection between 2 functions.

55. Given: $f(x) = x^4-3x^3+2x^2-7x-11$ Find all roots to the nearest 0.001

[You can solve for f(x)=0 by graphing f(x), then going to Calc menu and #2 zero function]

56. Given: $f(x) = 3\sin 2x - 4x + 1$ from $[-2\pi, 2\pi]$ Find all roots to the nearest 0.001 [NOTE: all trig functions are done in radian mode]

- 57. Given $f(x) = 0.7x^2 + 3.2x + 1.5$ Find all roots to the nearest 0.001
- 58. Given: $f(x) = x^4 8x^2 + 5$ Find all roots to the nearest 0.001

59. Given $f(x) = x^2 - 5x + 2$ and g(x) = 3 - 2xFind the coordinates of any points of intersection

Limits

Finding limits numerically.

Complete the table and use the result to estimate the limit.

60.
$$\lim_{x \to 4} \frac{x - 4}{x^2 - 3x - 4}$$

х	3.9	3.99	3.999	4.001	4.01	4.1
f(x)						

61.
$$\lim_{x \to -5} \frac{\sqrt{4-x}-3}{x+5}$$

х	-5.1	-5.01	-5.001	-4.999	-4.99	-4.9
f(x)						

Finding limits graphically.

Find each limit graphically. Use your calculator to assist in graphing.

62.
$$\lim_{x \to 0} \cos x$$

63.
$$\lim_{x\to 5} \frac{2}{x-5}$$

64.
$$\lim_{x \to 1} f(x)$$

$$f(x) = \begin{cases} x^2 + 3, & x \neq 1 \\ 2, & x = 1 \end{cases}$$

Evaluating Limits Analytically

Solve by direct substitution whenever possible. If needed, rearrange the expression so that you can do direct substitution.

14

65.
$$\lim_{x\to 2} (4x^2+3)$$

66.
$$\lim_{x \to 1} \frac{x^2 + x + 2}{x + 1}$$

67.
$$\lim_{x\to 0} \sqrt{x^2 + 4}$$

68.
$$\lim_{x\to\pi}\cos x$$

$$69. \lim_{x\to 1} \left(\frac{x^2-1}{x-1}\right)$$

69. $\lim_{x \to 1} \left(\frac{x^2 - 1}{x - 1} \right)$ HINT: Factor and simplify.

70.
$$\lim_{x \to -3} \frac{x^2 + x - 6}{x + 3}$$

71.
$$\lim_{x\to 0} \frac{\sqrt{x+1}-1}{x}$$

71. $\lim_{x\to 0} \frac{\sqrt{x+1}-1}{x}$ HINT: Multiply numerator & denominator by the conjugate.

72.
$$\lim_{x \to 3} \frac{3 - x}{x^2 - 9}$$

73.
$$\lim_{h\to 0} \frac{2(x+h)-2x}{h}$$

One-Sided Limits

Find the limit if it exists. First, try to solve for the overall limit. If an overall limit exists, then the one-sided limit will be the same as the overall limit. If not, use the graph and/or a table of values to evaluate one-sided limits.

74.
$$\lim_{x \to 5^+} \frac{x - 5}{x^2 - 25}$$

75.
$$\lim_{x \to -3^{-}} \frac{x}{\sqrt{x^2 - 9}}$$

76.
$$\lim_{x \to 10^+} \frac{|x - 10|}{x - 10}$$

$$77. \lim_{x\to 5^-} \left(-\frac{3}{x+5}\right)$$

Vertical Asymptotes

Determine the vertical asymptotes for the function. Set the denominator equal to zero to find the x-value for which the function is undefined. That will be the vertical asymptote.

78.
$$f(x) = \frac{1}{x^2}$$

79.
$$f(x) = \frac{x^2}{x^2 - 4}$$

80.
$$f(x) = \frac{2+x}{x^2(1-x)}$$

Horizontal Asymptotes

Determine the horizontal asymptotes using the three cases below.

Case I. Degree of the numerator is less than the degree of the denominator. The asymptote is y = 0.

Case II. Degree of the numerator is the same as the degree of the denominator. The asymptote is the ratio of the lead coefficients.

Case III. Degree of the numerator is greater than the degree of the denominator. There is no horizontal asymptote. The function increases without bound. (If the degree of the numerator is exactly 1 more than the degree of the denominator, then there exists a slant asymptote, which is determined by long division.)

Determine all Horizontal Asymptotes.

81.
$$f(x) = \frac{x^2 - 2x + 1}{x^3 + x - 7}$$

82.
$$f(x) = \frac{5x^3 - 2x^2 + 8}{4x - 3x^3 + 5}$$

83.
$$f(x) = \frac{4x^5}{x^2 - 7}$$

Determine each limit as x goes to infinity.

RECALL: This is the same process you used to find Horizontal Asymptotes for a rational function.

** In a nutshell

- 1. Find the highest power of x.
- 2. How many of that type of x do you have in the numerator?
- 3. How many of that type of x do you have in the denominator?
- **4.** If highest power in numerator = highest power in denominator, that ratio is your limit!

$$\lim_{x \to \infty} \left(\frac{2x - 5 + 4x^2}{3 - 5x + x^2} \right)$$

$$\lim_{x \to \infty} \left(\frac{2x - 5 + 4x^2}{3 - 5x + x^2} \right) \qquad \lim_{x \to \infty} \left(\frac{2x - 5}{3 - 5x + 3x^2} \right)$$

$$\lim_{x \to \infty} \left(\frac{7x + 6 - 2x^3}{3 + 14x + x^2} \right)$$

Limits to Infinity

A rational function does not have a limit if it goes to $\pm \infty$, however, you can state the direction the limit is headed if both the left and right hand side go in the same direction.

Determine each limit if it exists. If the limit approaches ∞ or $-\infty$, please state which one the limit approaches.

87.
$$\lim_{x \to -1^+} \frac{1}{x+1} =$$
 88. $\lim_{x \to 1^+} \frac{2+x}{1-x} =$

88.
$$\lim_{x \to 1^+} \frac{2+x}{1-x} =$$

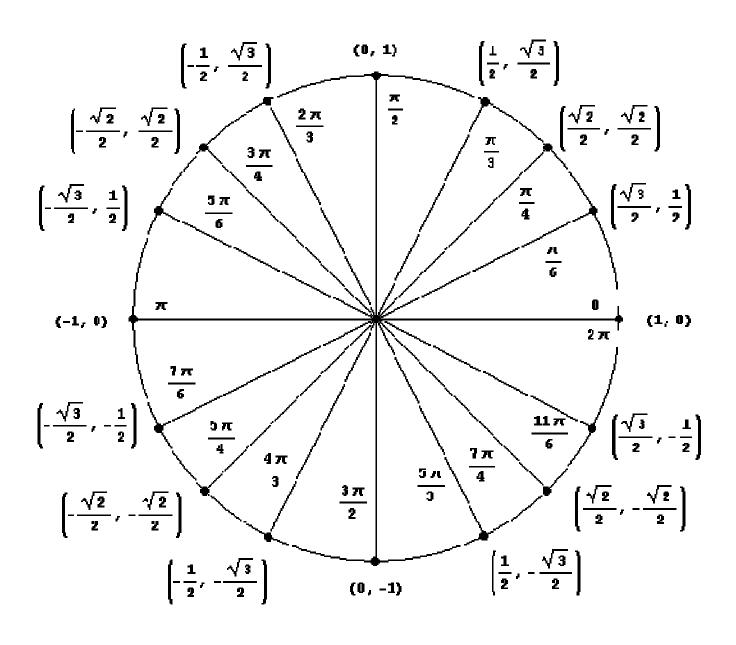
89.
$$\lim_{x\to 0} \frac{2}{\sin x} =$$

Circle with Radius 1

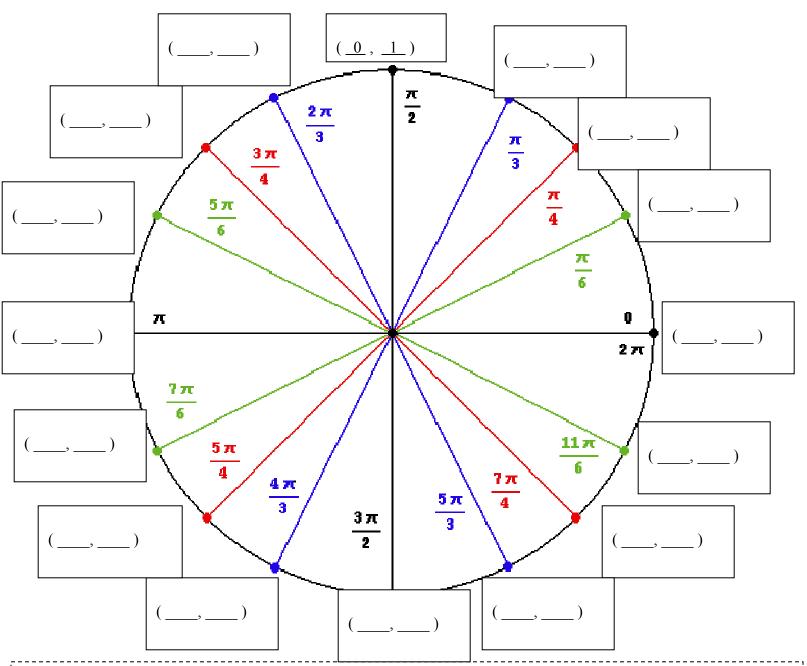
otherwise known as unit circle

$$(x,y) = (\cos\theta, \sin\theta)$$

You can determine the sine or cosine of an angle by using the unit circle. The x coordinate of the circle is cosine, and the y-coordinate is the sine.



Unit Circle Worksheet



DIRECTIONS: Please fill in the (x, y) coordinates above for the Unit Circle. Then proceed by filling in the values of the appropriate sin, cos and tan functions below.

Formula Sheet

$$\csc x = \frac{1}{\sin x}$$

$$\csc x = \frac{1}{\sin x}$$
 $\sec x = \frac{1}{\cos x}$ $\cot x = \frac{1}{\tan x}$

$$\cot x = \frac{1}{\tan x}$$

$$\tan x = \frac{\sin x}{\cos x}$$

$$\tan x = \frac{\sin x}{\cos x} \qquad \cot x = \frac{\cos x}{\sin x}$$

$$\sin^2 x + \cos^2 x = 1$$

$$\tan^2 x + 1 = \sec^2 x$$

$$\sin^2 x + \cos^2 x = 1$$
 $\tan^2 x + 1 = \sec^2 x$ $1 + \cot^2 x = \csc^2 x$

$$\sin 2x = 2\sin x \cos x$$

$$\tan 2x = \frac{2\tan x}{1 - \tan^2 x}$$

$$\cos 2x = \cos^2 x - \sin^2 x$$
$$= 1 - 2\sin^2 x$$

$$= 1 - 2\sin x$$
$$= 2\cos^2 x - 1$$

Logarithms:

$$y = \log_a x$$
 is equivalent to

$$x = a^y$$

Product property:

$$\log_b mn = \log_b m + \log_b n$$

$$\log_b \frac{m}{n} = \log_b m - \log_b n$$

$$\log_b m^p = p \log_b m$$

If
$$\log_b m = \log_b n$$
, then $m = n$

$$\log_a n = \frac{\log_b n}{\log_b a}$$

Slope of a tangent line to a curve or the derivative:
$$\lim_{h\to 0} \frac{f(x+h) - f(x)}{h}$$

Slope-intercept form: y = mx + b

Point-slope form:
$$y - y_1 = m(x - x_1)$$

Standard form:
$$Ax + By = C$$

AP Calculus Summer Packet Answer Key

1)
$$\frac{5-a}{a}$$

$$2) \qquad \frac{2x}{5(x+4)}$$

$$\frac{4(x-3)}{5x}$$

4)
$$\frac{x^2 - x - 1}{x^2 + x + 1}$$

3)
$$\frac{4(x-3)}{5x}$$
 4) $\frac{x^2-x-1}{x^2+x+1}$ 5) $\frac{x-4}{3x^2-4x+32}$

A)
$$\frac{-h}{x(x+h)}$$

B)
$$\frac{x}{5}$$

B)
$$\frac{x}{5}$$
 C) $\frac{2y^3}{3x^4}$

D)
$$3\sqrt{x^3}$$

E)
$$20a^5$$

F)
$$8a^{\frac{5}{2}}$$
 G) -2

H)
$$\frac{-1}{x+5}$$

8)
$$2t+3$$

10)
$$8m^2 + 40m + 49$$

13)
$$\frac{\sqrt{3}}{2}$$

15)
$$4x^2 + 12x + 9$$

16)
$$2x^6 + 3$$

$$19) \quad \left(\frac{5}{2},0\right)$$

$$(1,0)$$
 $(-2,0)$

$$(0,-5)$$

$$(0,-2)$$

$$(4,0)$$

 $(-4,0)$

$$\begin{array}{cc} 22) & (-2,0) \\ & (2,0) \end{array}$$

23) (3,5)

24)
$$(2,2)$$
 $(-1,5)$ 25) $\left(\frac{-2}{7}, \frac{-13}{7}\right)$

26)

	(-2,4]	<>
-1 ≤ x < 7		← E
<i>x</i> ≤ 8	$(-\infty, 8]$	•

27)
$$\left[\frac{1}{2},\infty\right)$$

27)
$$\left[\frac{1}{2},\infty\right)$$
 28) $\left[\frac{-1}{2},\frac{7}{2}\right)$ 29) $(30,\infty)$

30)
$$\frac{D:(-\infty,\infty)}{R:[-5,\infty)}$$
 31) $\frac{D:[-3,\infty)}{R:(-\infty,0]}$

31)
$$\frac{D:[-3,\infty)}{R:(-\infty,0]}$$

32)
$$\frac{D:(-\infty,\infty)}{R:[-3,3]}$$

33)
$$\frac{D:(-\infty,1)\cup(1,\infty)}{R:(-\infty,0)\cup(0,\infty)}$$

34)
$$f^{-1}(x) = \frac{x-1}{2}$$

35)
$$f^{-1}(x) = \pm \sqrt{3x}$$

38)
$$y = 3x + 5$$

39)
$$x = 5$$

40)
$$y = 2$$

41)
$$y-5=\frac{2}{3}x$$

42)
$$y-8=\frac{5}{6}(x-2)$$

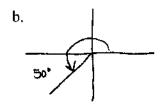
43)
$$y = 7$$

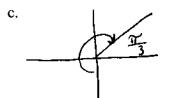
44)
$$y - 6 = -(x + 3)$$

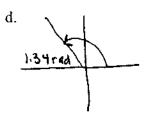
45)
$$y = -\frac{3}{2}x + 3$$

47)
$$b.\frac{-17\pi}{180}$$

$$c.\frac{79\pi}{60}$$



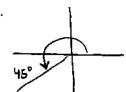






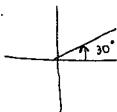


b.



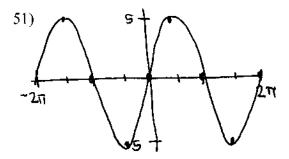


d.

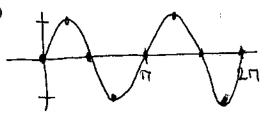


b.
$$-\frac{\sqrt{2}}{2}$$
 c. -1

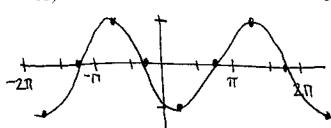
d.
$$-\frac{1}{2}$$



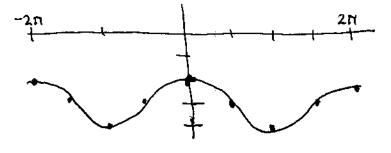








54)



$$55) \qquad \begin{array}{c} x = 3.329 \\ x = -0.911 \end{array}$$

56)
$$x = 0.957$$

$$57) \quad \begin{array}{c} x = -0.530 \\ x = -4.041 \end{array}$$

58)
$$x = \pm 0.827$$

 $x = \pm 2.705$

61)
$$\frac{1}{6}$$

71)
$$\frac{1}{2}$$

72)
$$-\frac{1}{6}$$

74)
$$\frac{1}{10}$$

77)
$$-\frac{3}{10}$$

78)
$$x = 0$$

79)
$$x = \pm 2$$

80)
$$x = 0$$

81)
$$y = 0$$

82)
$$y = -\frac{5}{3}$$

86) DNE or
$$-\infty$$

UNIT CIRCLE WORKSHEET BOXED ANSWERS:

0	$\frac{1}{2}$
1	$-\frac{\sqrt{3}}{2}$
-1	undefined
-1	$\frac{\sqrt{2}}{2}$
1	$\frac{\sqrt{3}}{2}$
0	0